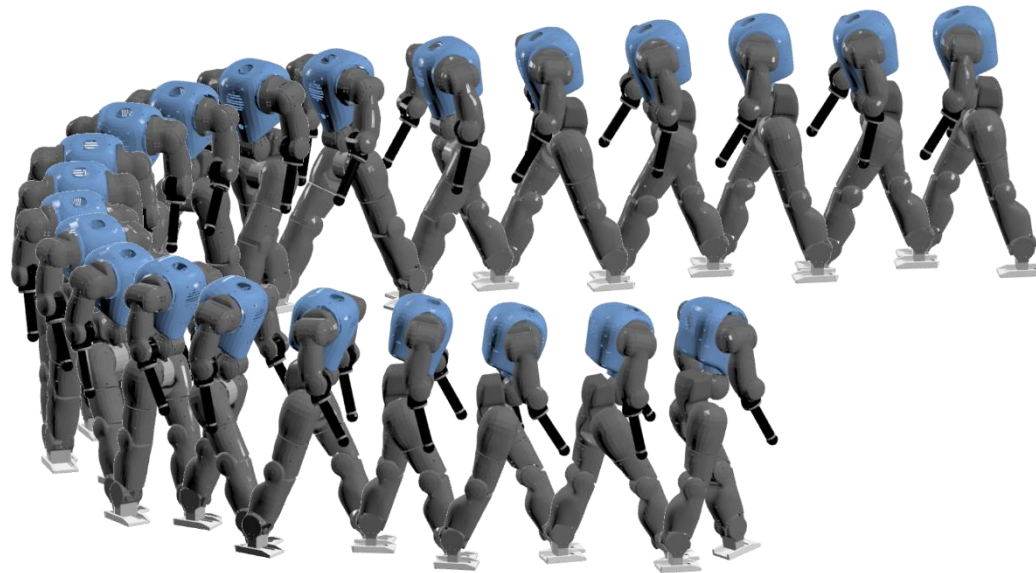


Rich and Robust Bio-Inspired Locomotion Control for Humanoid Robots



Ph.D. thesis – Public defense
Nicolas Van der Noot

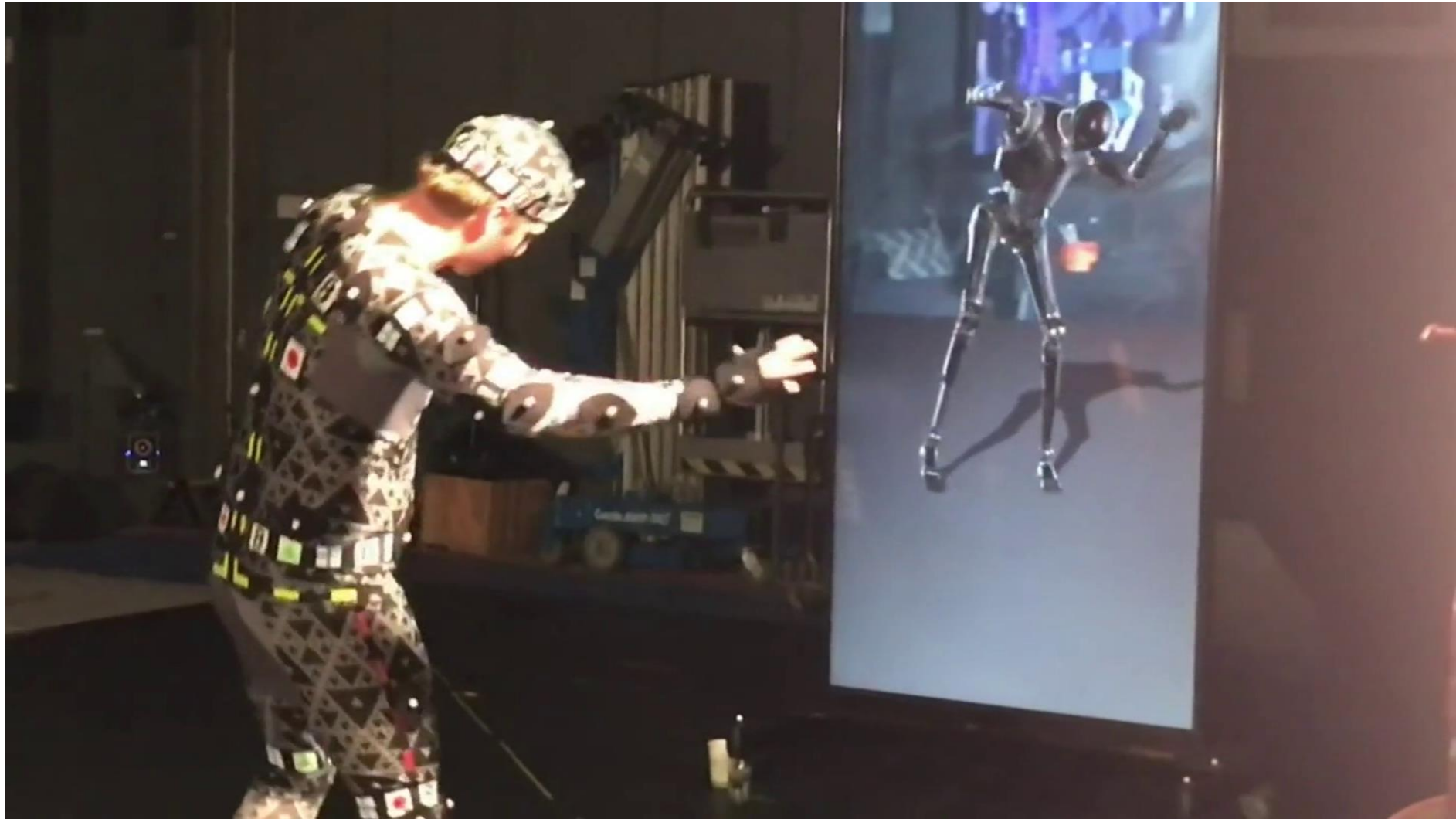
Prof Kamiar Aminian	president
Prof Renaud Ronsse	thesis director
Prof Auke Jan Ijspeert	thesis director
Prof Paul Fisette	examiner
Prof Hartmut Geyer	examiner
Prof Silvestro Micera	examiner

Robots capable to adapt to our environment



© Star Wars : Episode VII – The Force Awakens

Humanoid robots in movies



© Rogue One – A Star Wars Story

DARPA Robotics Challenge



© IEEE Spectrum – DRC compilation

Introduction & Methods

Reflex-based controller

Forward gait modulation in 2D scenarios

Steering control in 3D scenarios

Conclusion

Introduction & Methods

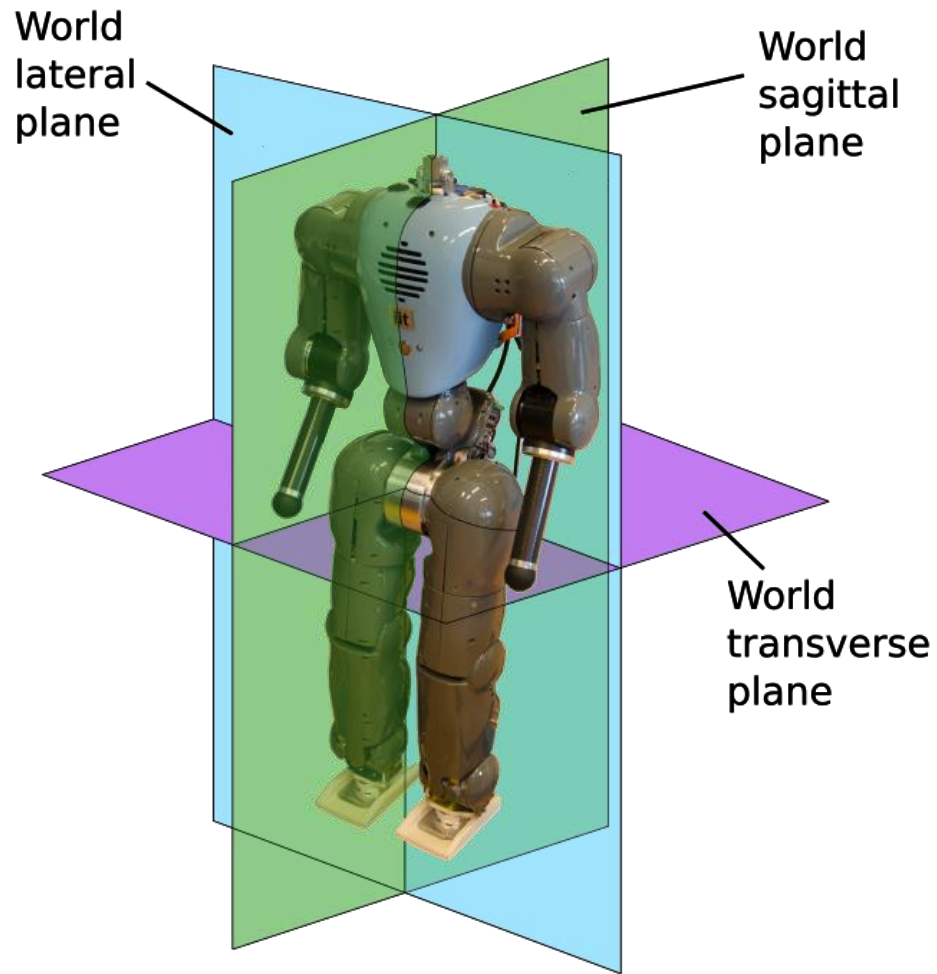
Reflex-based controller

Forward gait modulation in 2D scenarios

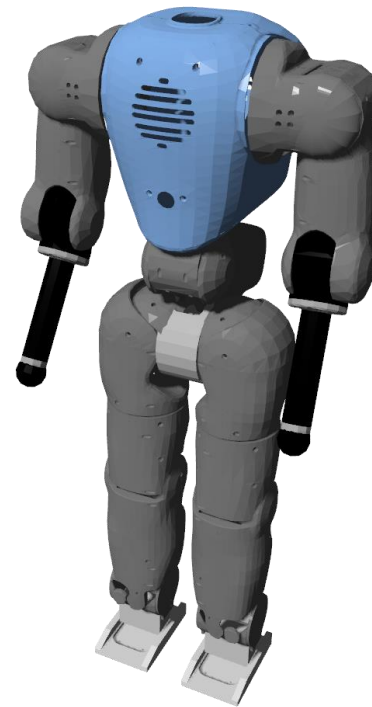
Steering control in 3D scenarios

Conclusion

Biped embodiment: the COMAN robot



real COMAN



simulated COMAN

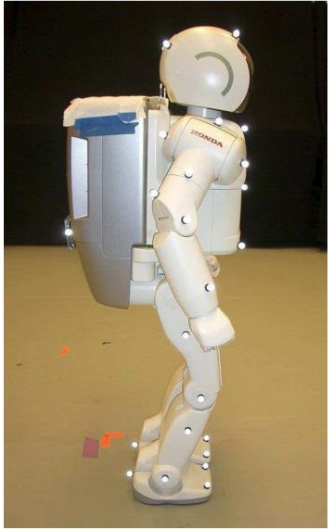
2D gait

waist motion only in
the world sagittal plane

3D gait

no motion constraint

Human walking skills for robots



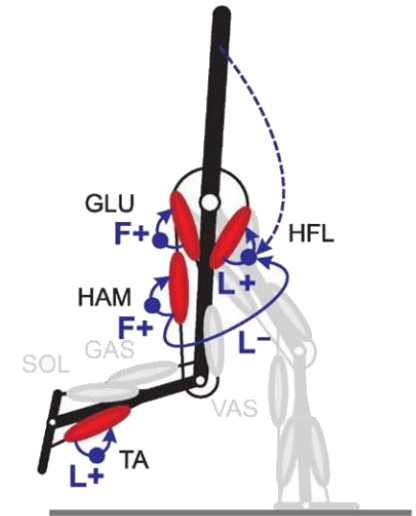
© Chestnutt, 2005

Traditional approaches

- versatile and well known
- energy inefficiency
- non human-like features

Bio-inspired limit cycle walkers

- energy efficiency
- human-like features
- many parameters to optimize
- mainly in simulation

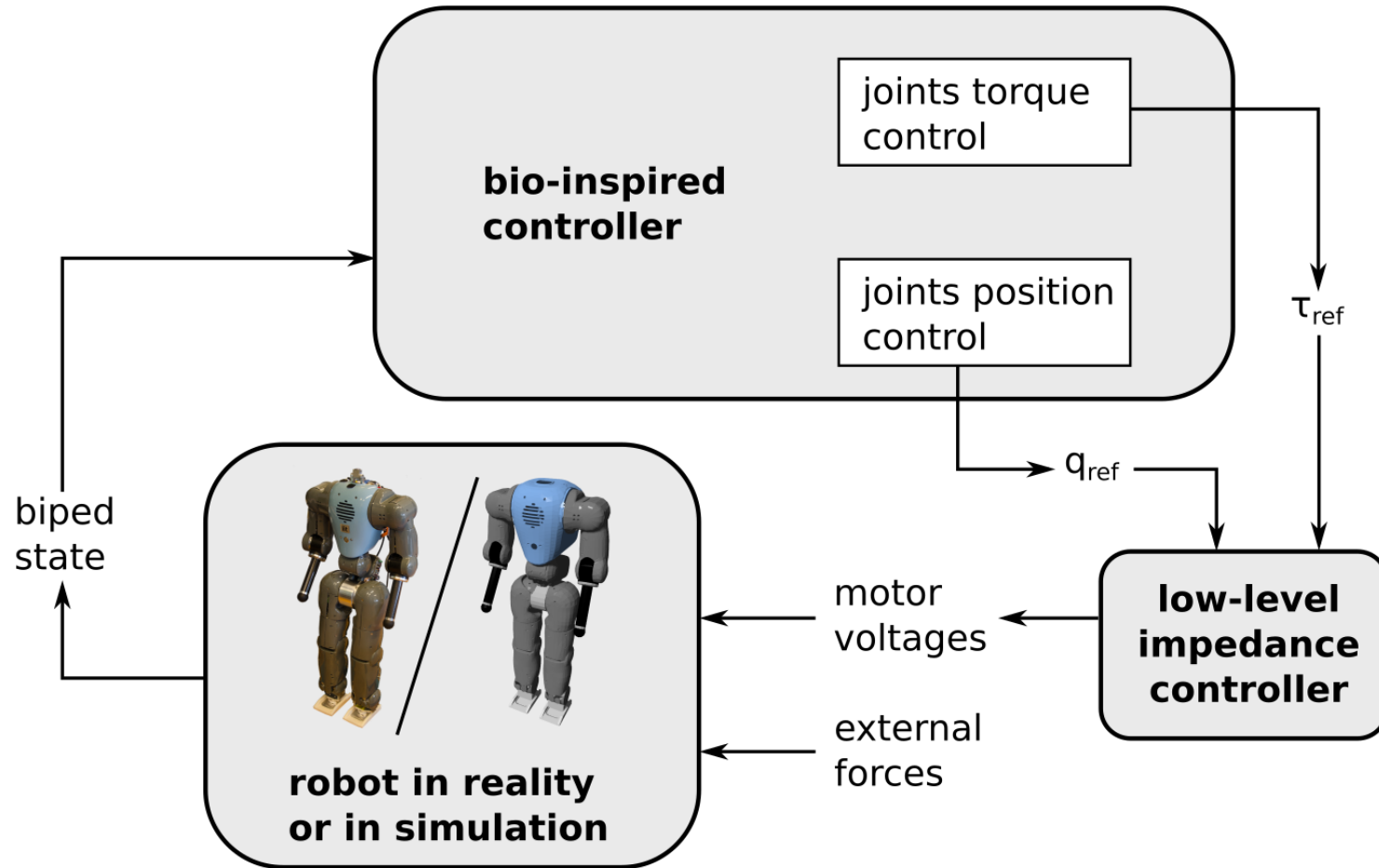


© Geyer, 2010

“A muscle-reflex model that encodes principles of legged mechanics produces human walking dynamics and muscle activities”, H. Geyer and H. Herr, 2010

➔ Port bio-inspired controllers with **steering capabilities** to **humanoid robots**

General control framework



Introduction & Methods

Reflex-based controller

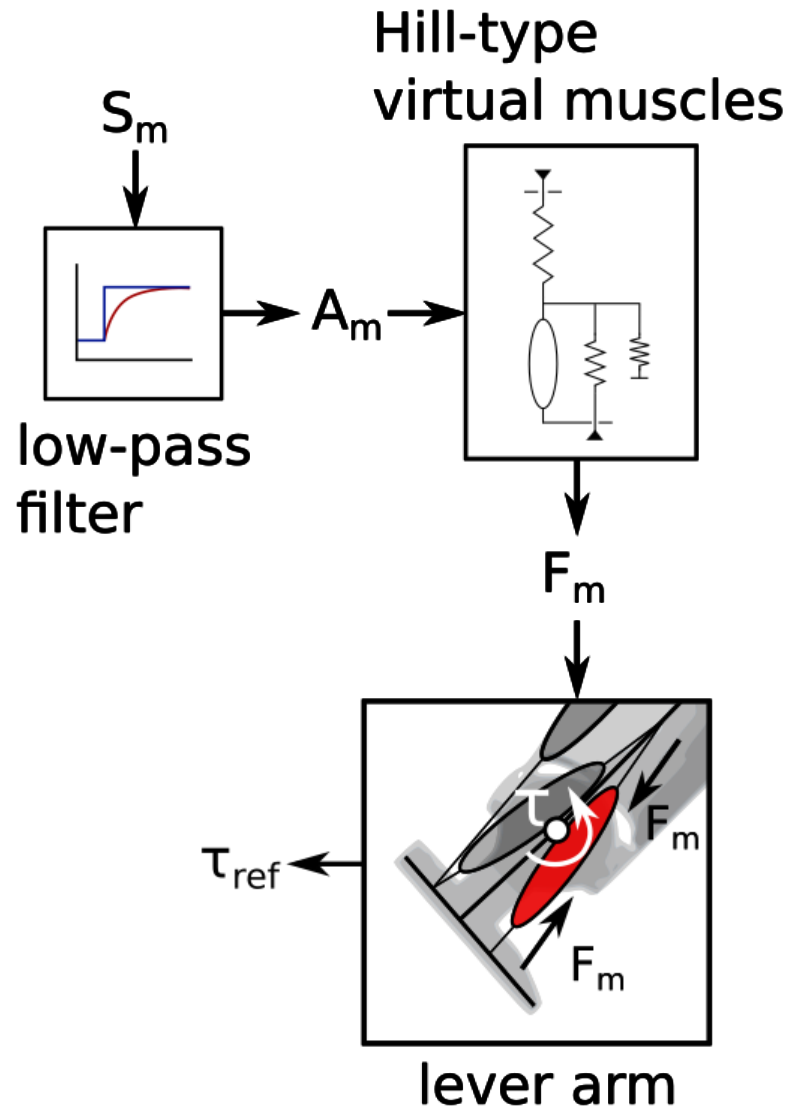
- Neuromuscular model
- Experimental validation
- Adaptation to different robots

Forward gait modulation in 2D scenarios

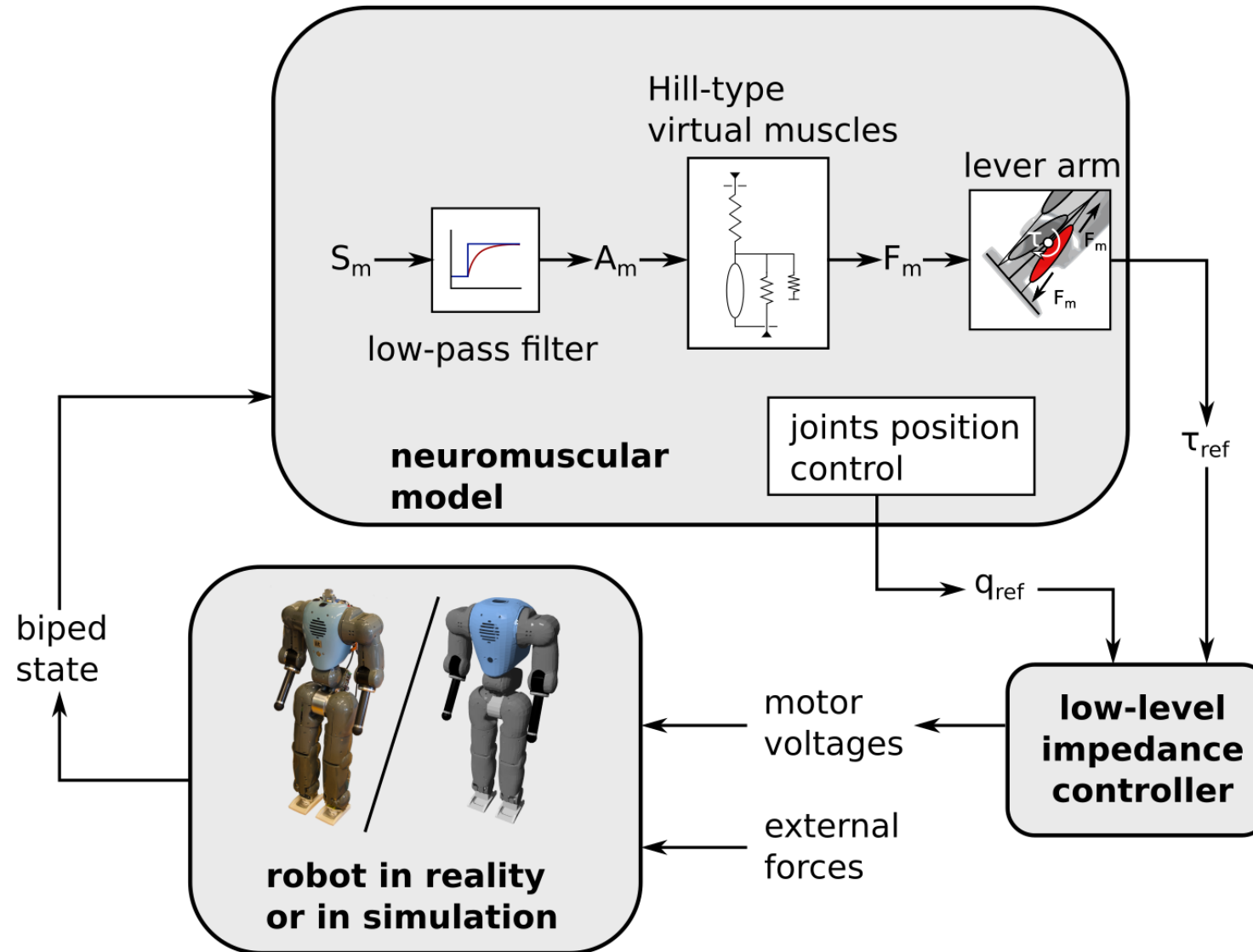
Steering control in 3D scenarios

Conclusion

Muscle-based control



General control framework

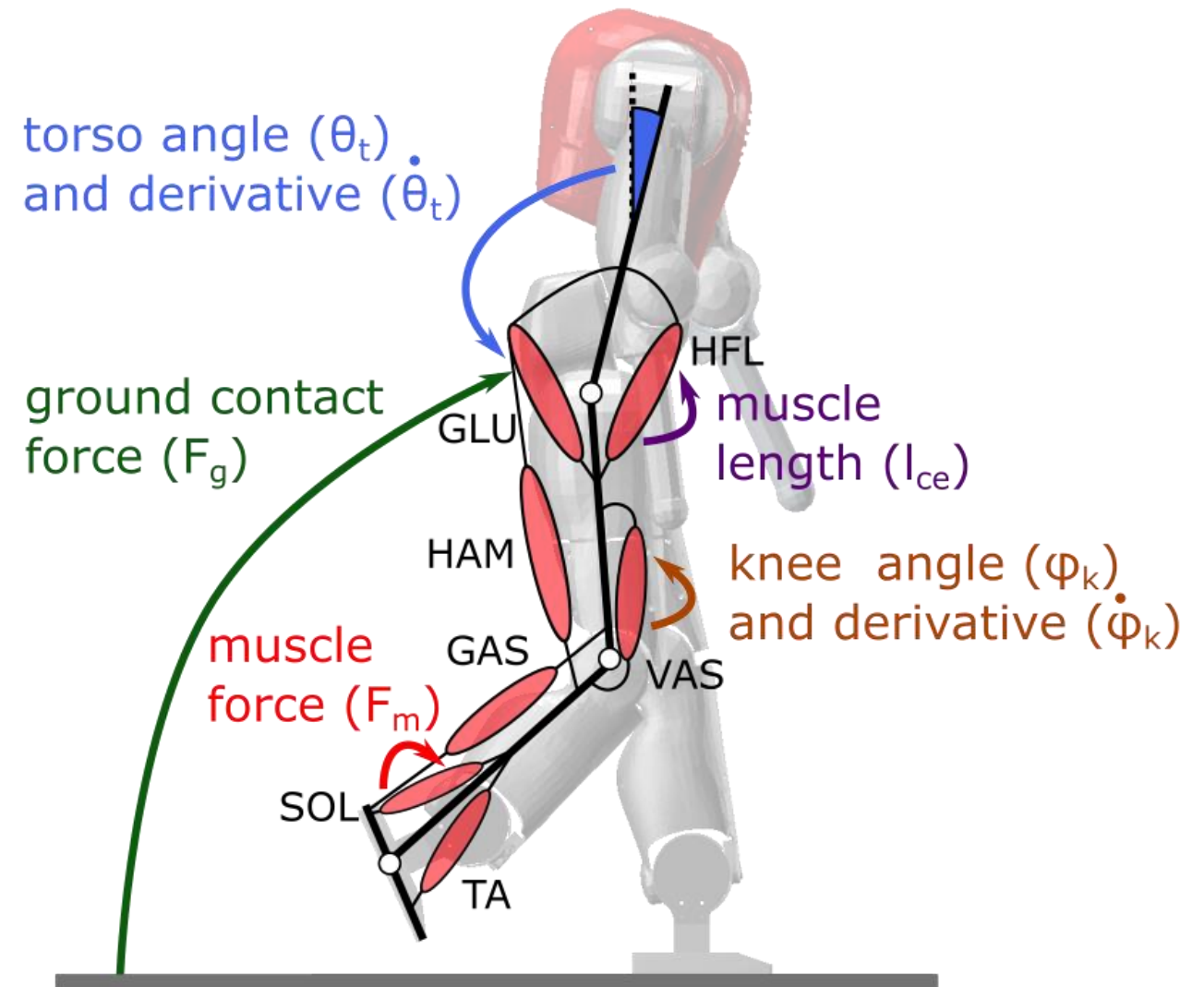


Reflex-based control

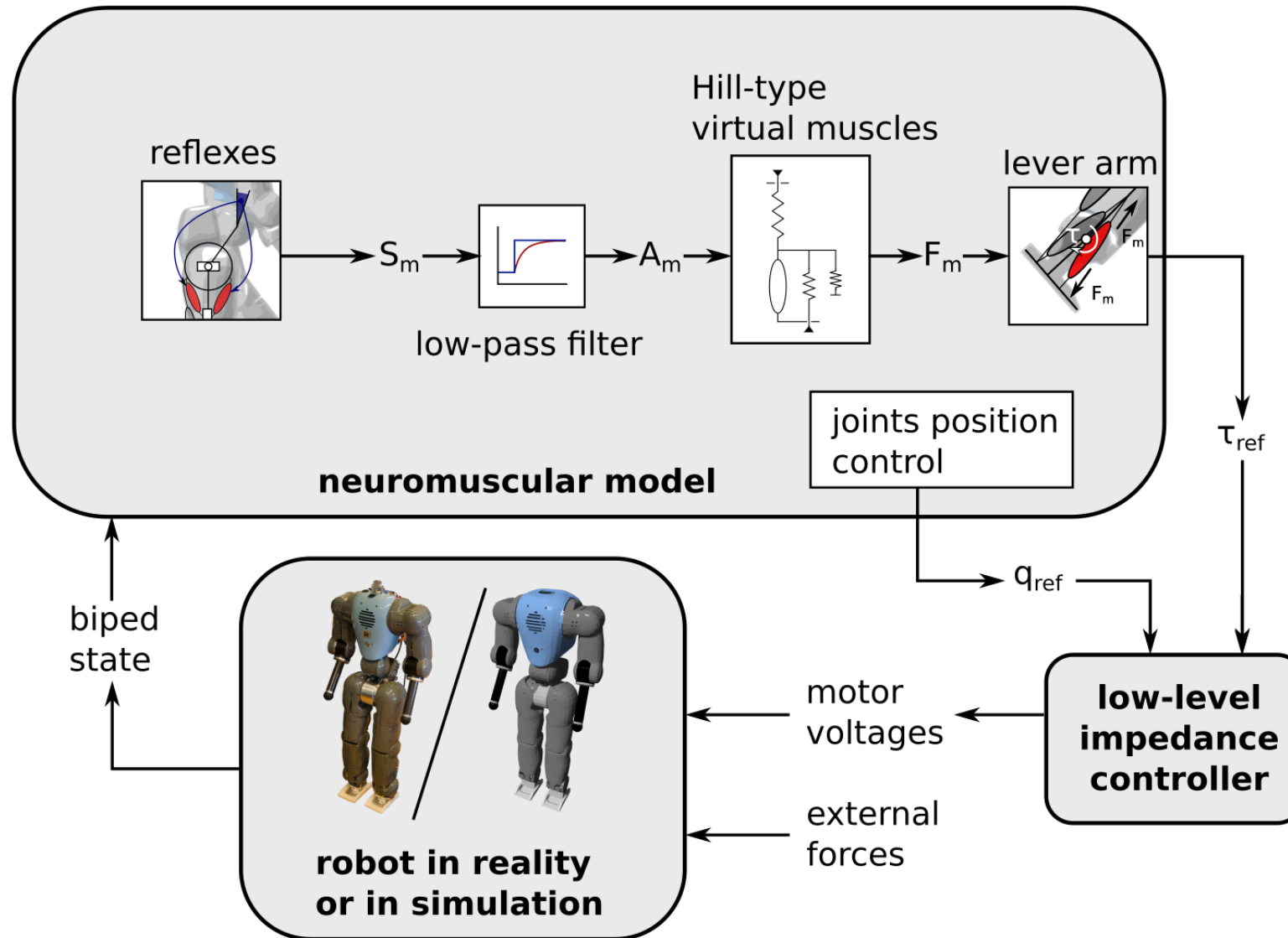
The biped is equipped with virtual **Hill-type muscles** in each leg.

Stimulation signals are computed based on **reflex rules**.

These rules are adapted from [Geyer and Herr, 2010].



General control framework

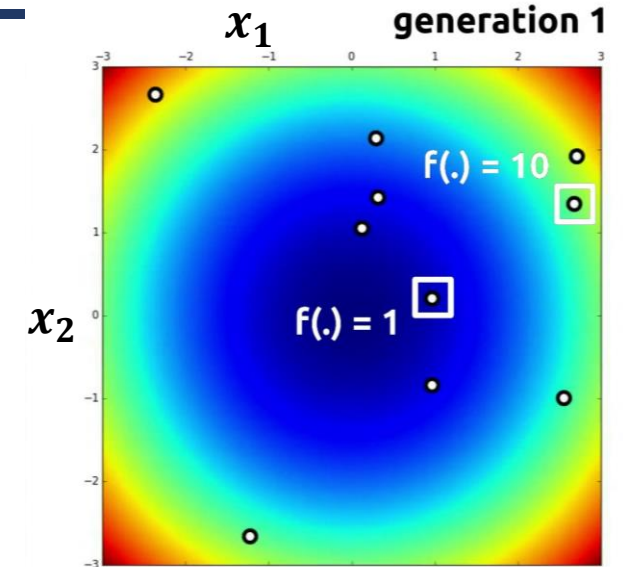
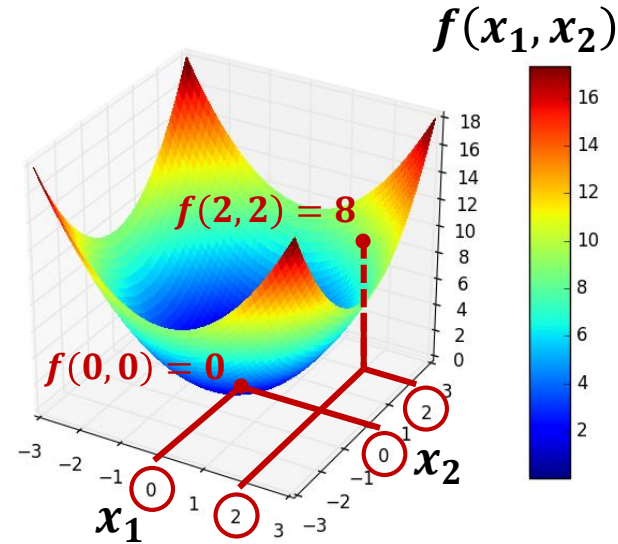


Particle Swarm Optimization (PSO)

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \text{ minimizing } f(x_1, x_2)$$

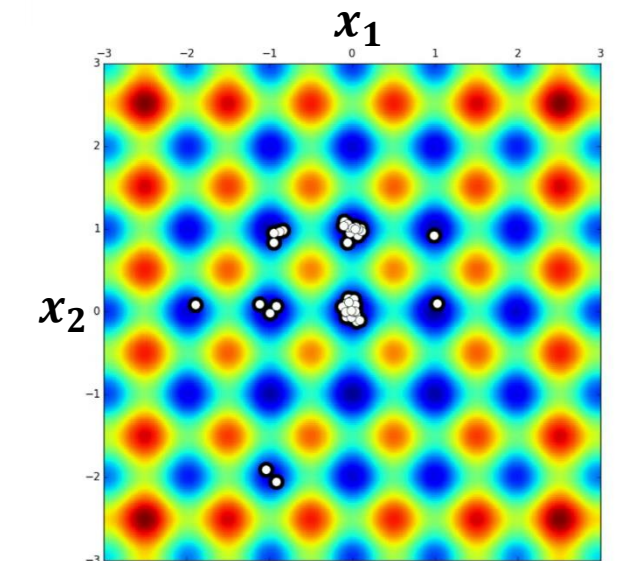
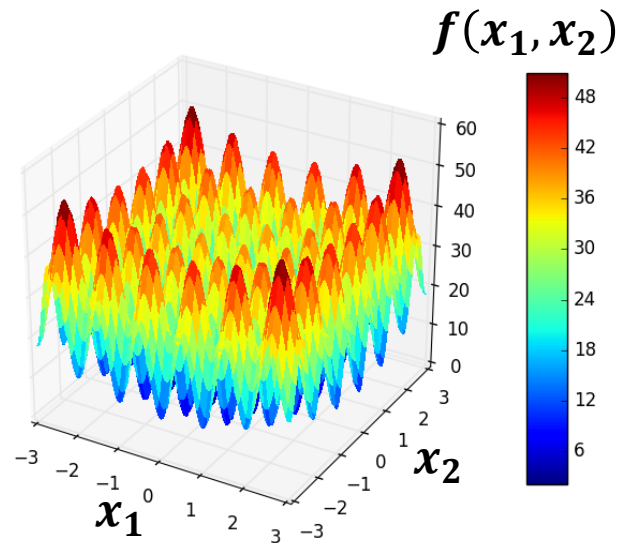
$$f(x_1, x_2) = x_1^2 + x_2^2$$

(Sphere function)

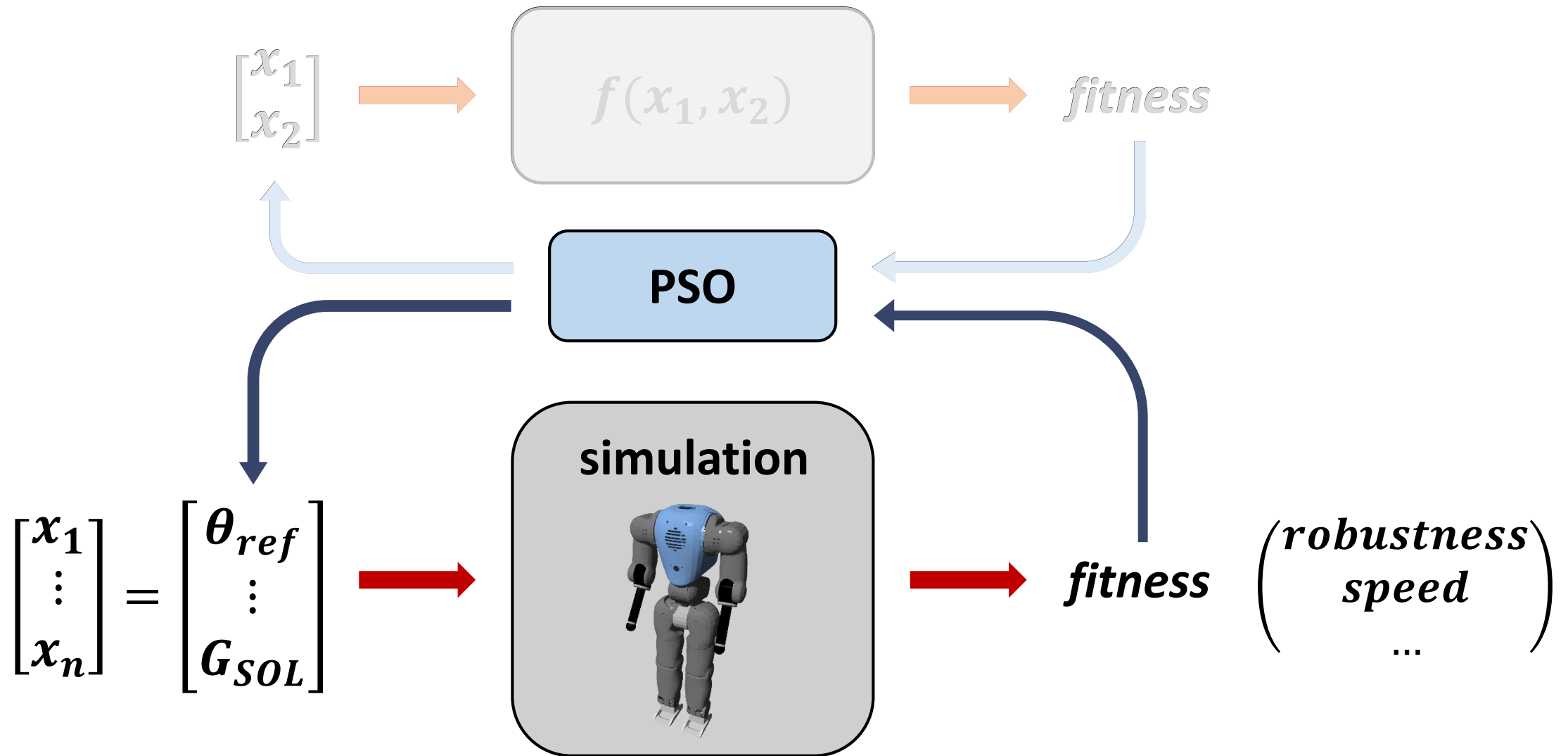


$$f(x_1, x_2) = 20 + \sum_{i=1}^2 [x_i^2 - 10 \cos(2 \pi x_i)]$$

(Rastrigin function)

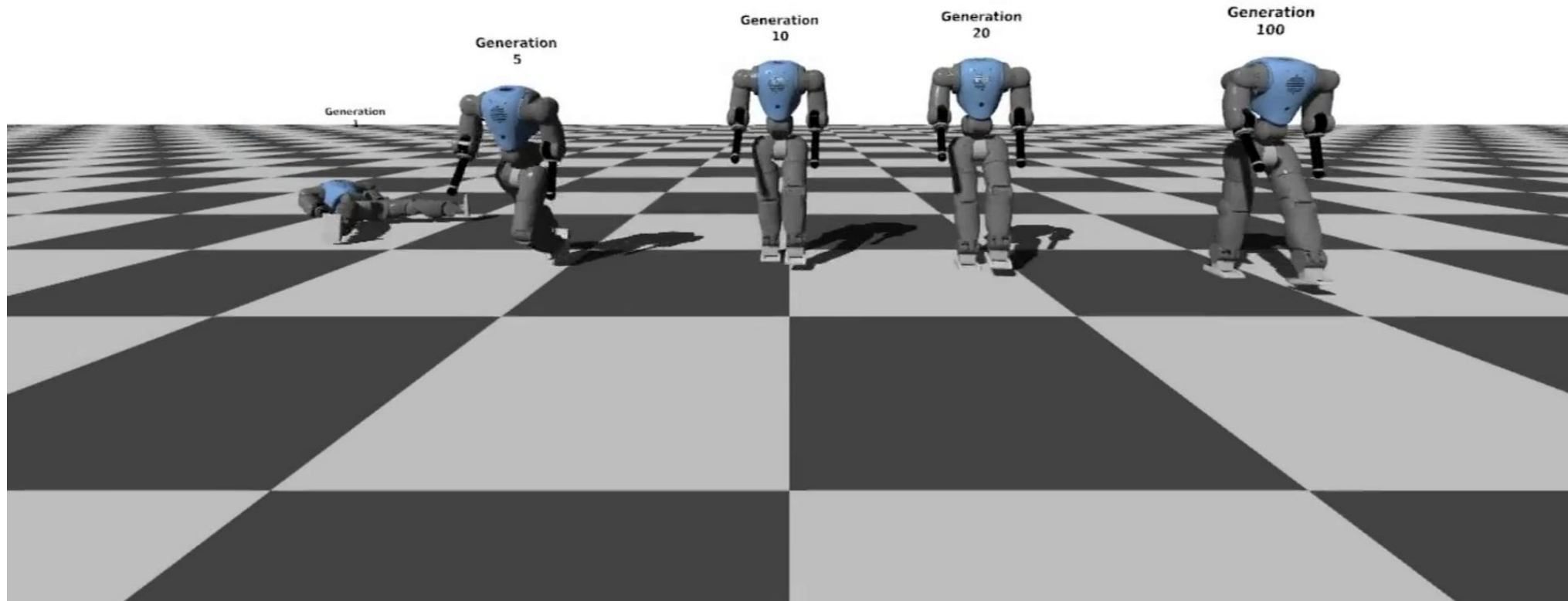


Particle Swarm Optimization (PSO)



Learning through optimization

The optimizer rewards robust walkers.



Introduction & Methods

Reflex-based controller

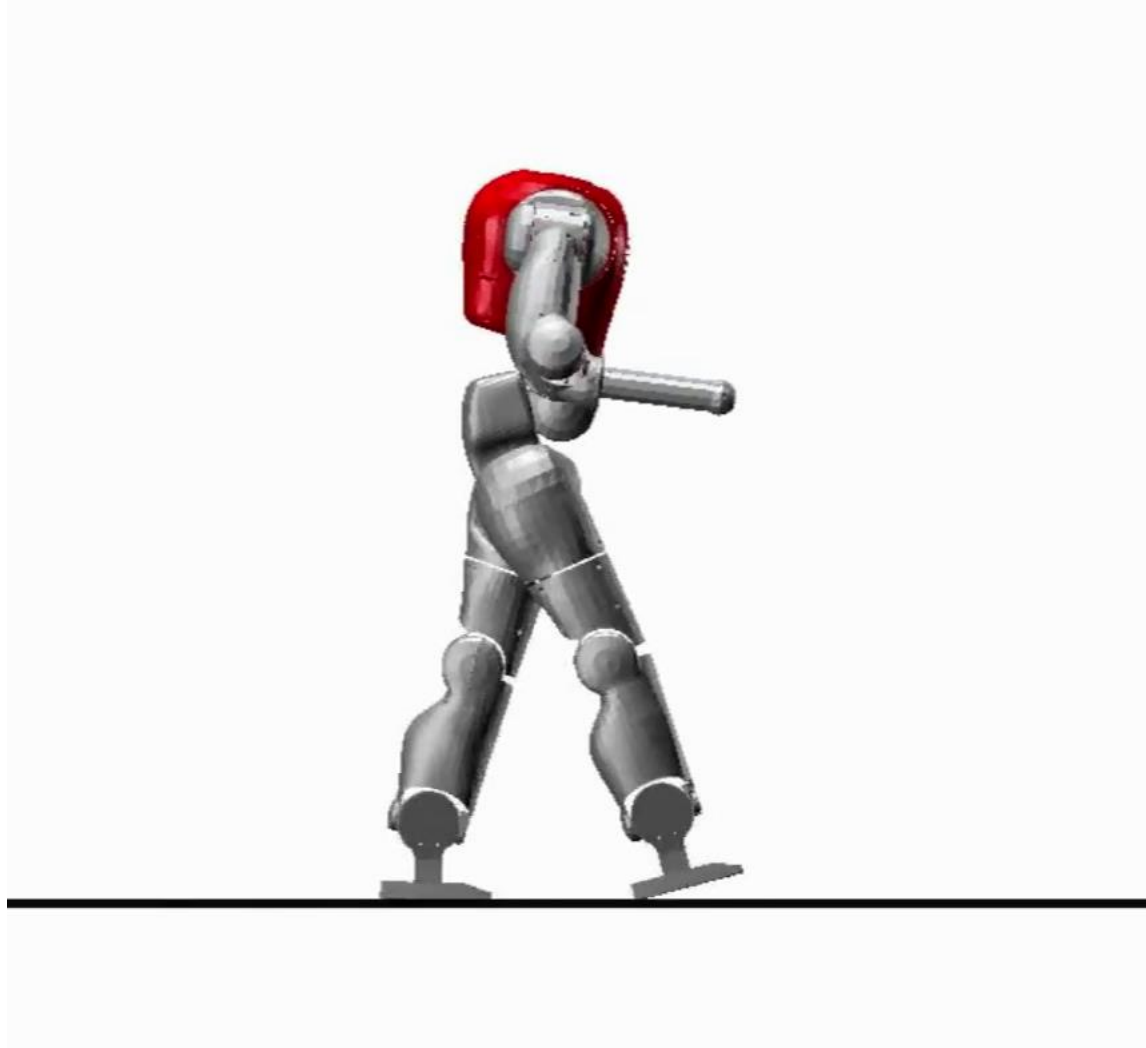
- Neuromuscular model
- Experimental validation
- Adaptation to different robots

Forward gait modulation in 2D scenarios

Steering control in 3D scenarios

Conclusion

Optimized simulation gait for 2D scenarios



The reflex-based controller of [Geyer and Herr, 2010] is optimized in a **2D simulation environment**.

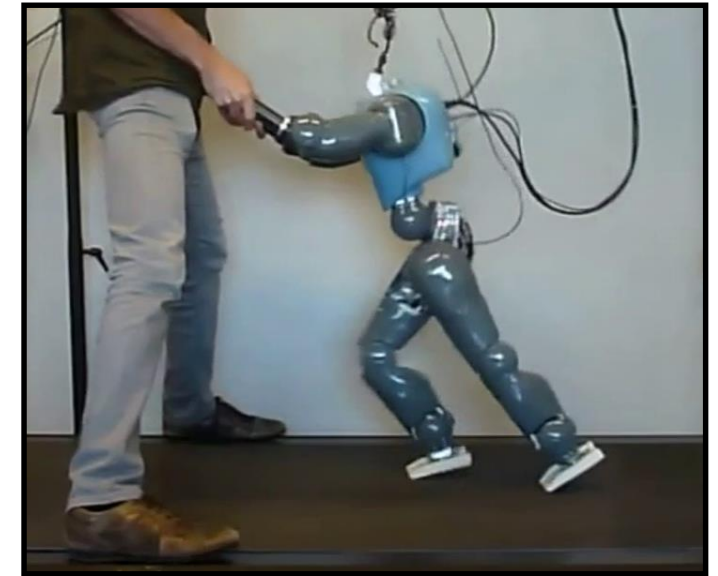
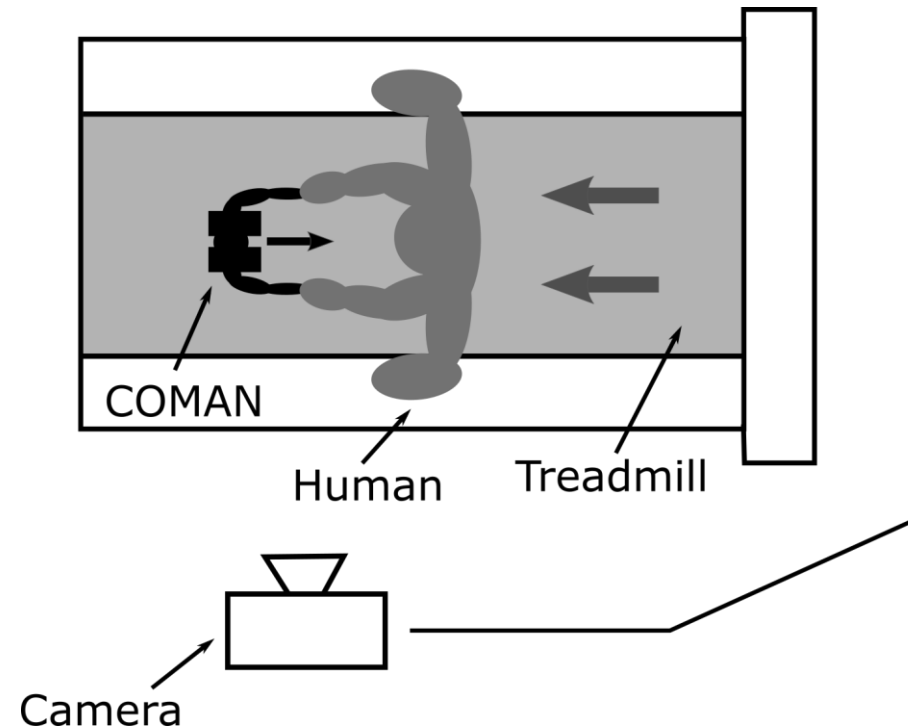
➔ The **exact same controller** is ported to the real robot.

Lateral balance – experimental setup

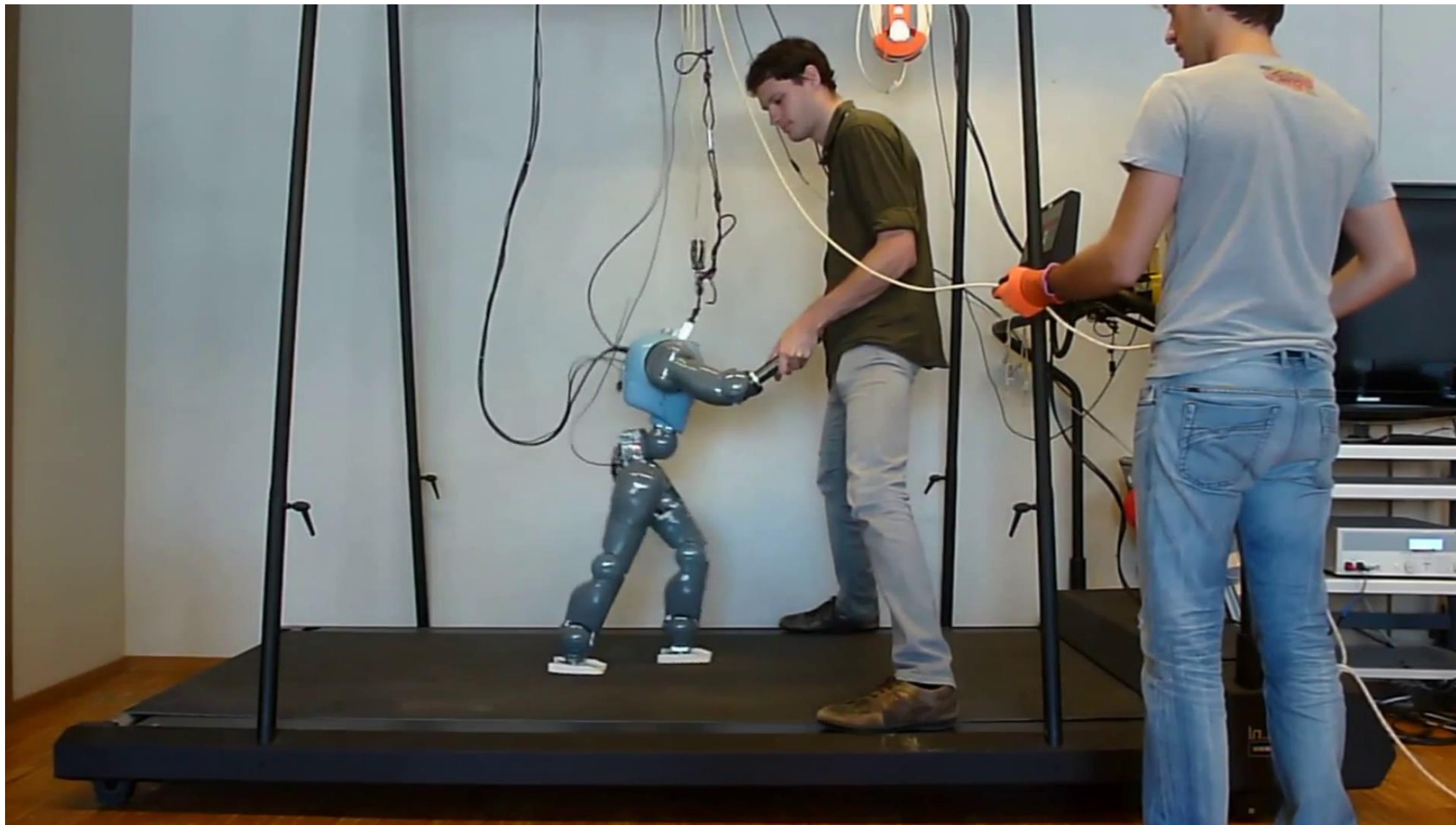
Lateral balance

- constraints in simulation
- upper-body control on the real robot

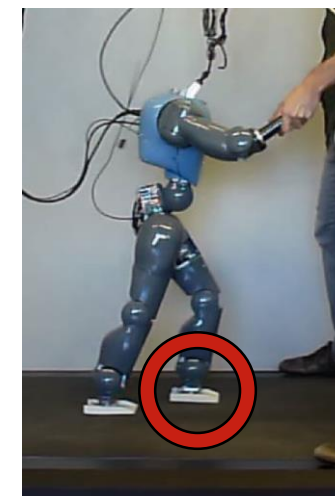
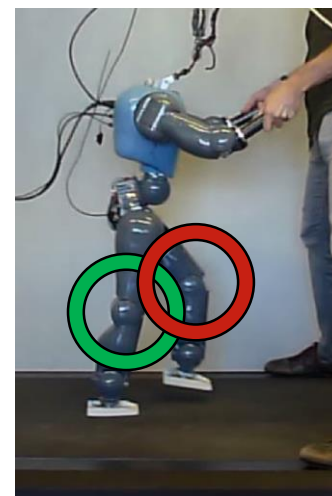
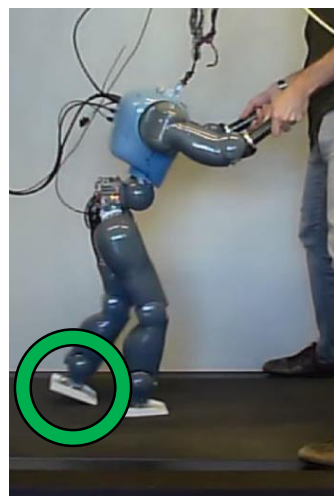
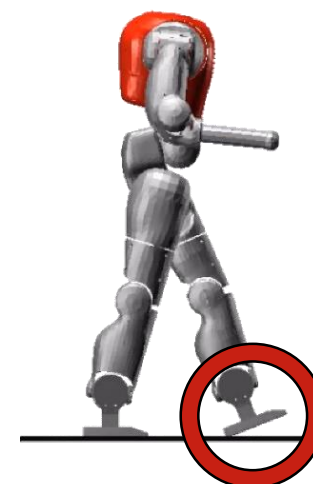
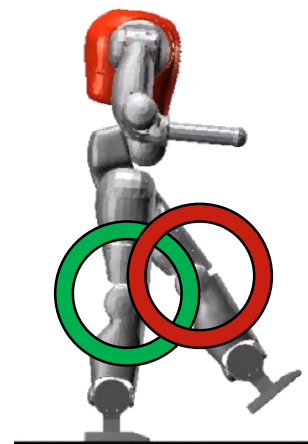
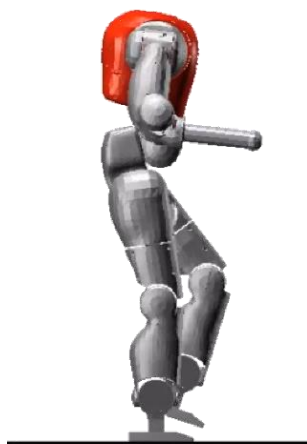
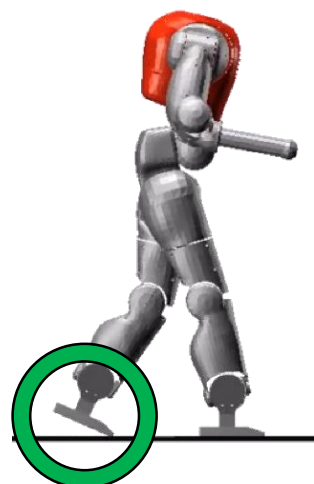
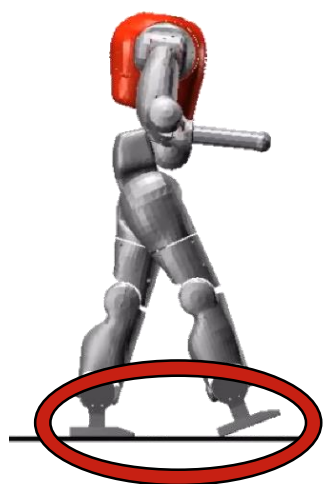
→ Help from a human operator



Experimental validation on a treadmill



Simulation and experimental gaits



Introduction & Methods

Reflex-based controller

- Neuromuscular model
- Experimental validation
- Adaptation to different robots

Forward gait modulation in 2D scenarios

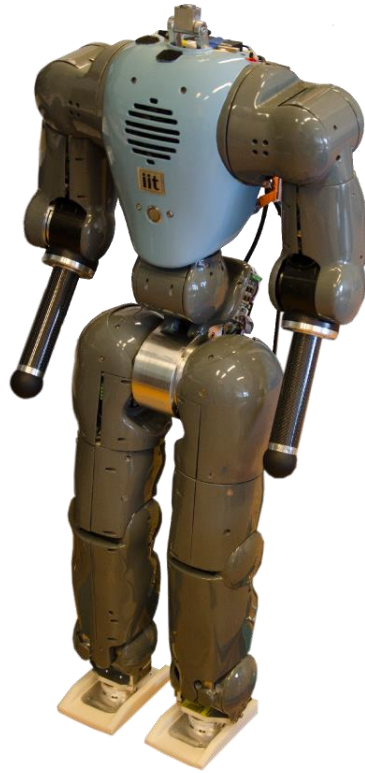
Steering control in 3D scenarios

Conclusion

Adaptation to different robots



NAO



COMAN



WALK-MAN

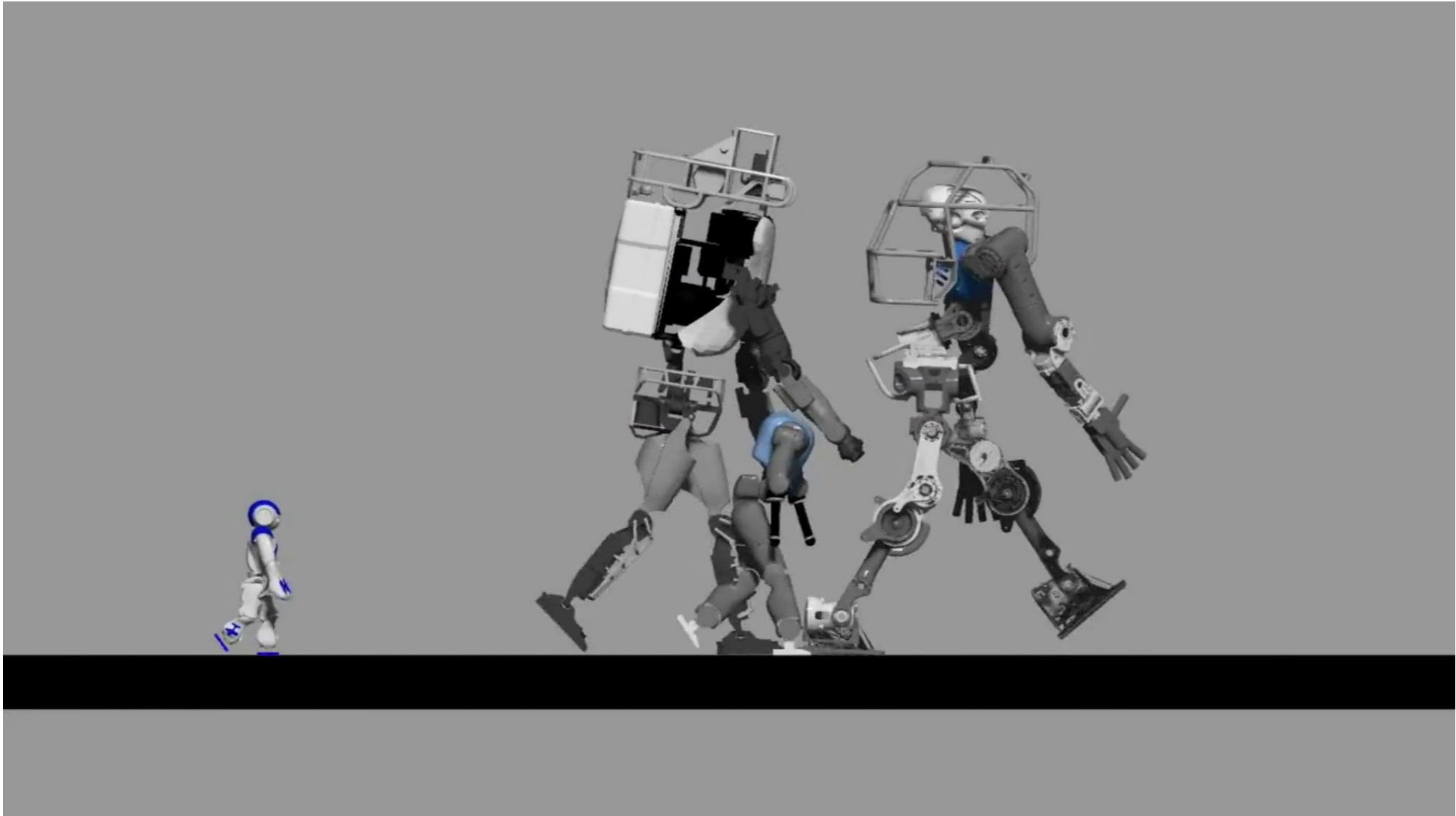


ATLAS



Adrien De Coninck

2D walking with different robots



Introduction & Methods

Reflex-based controller

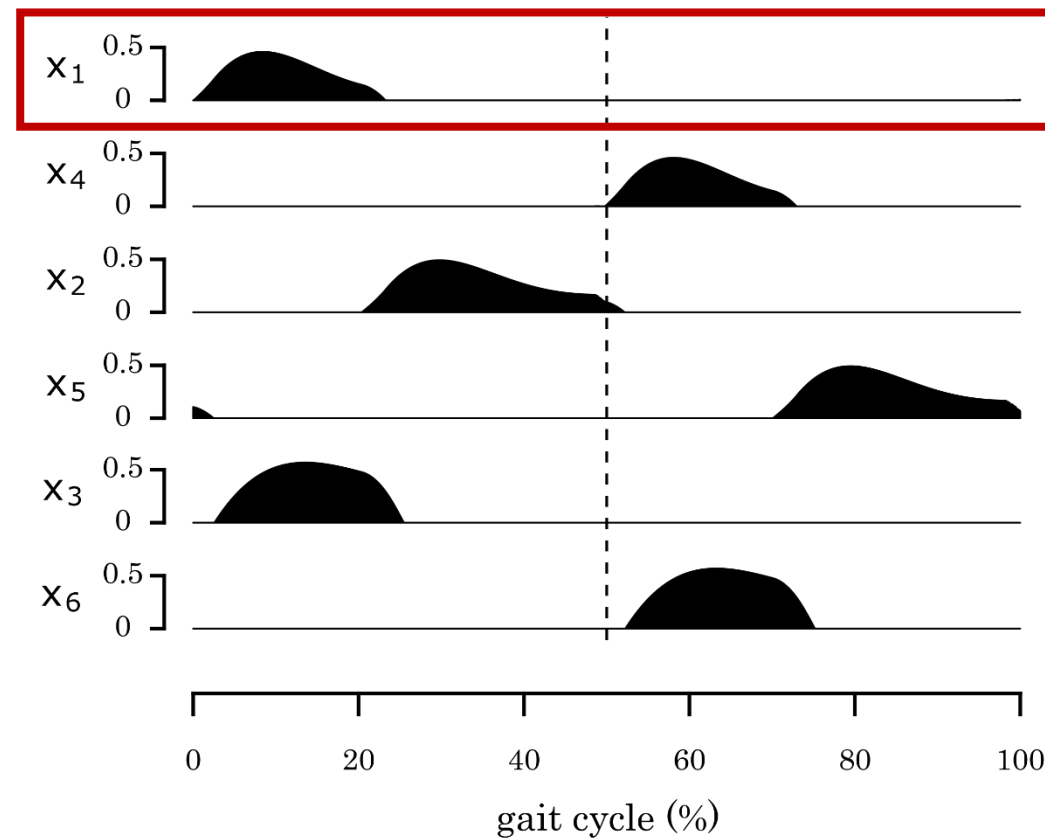
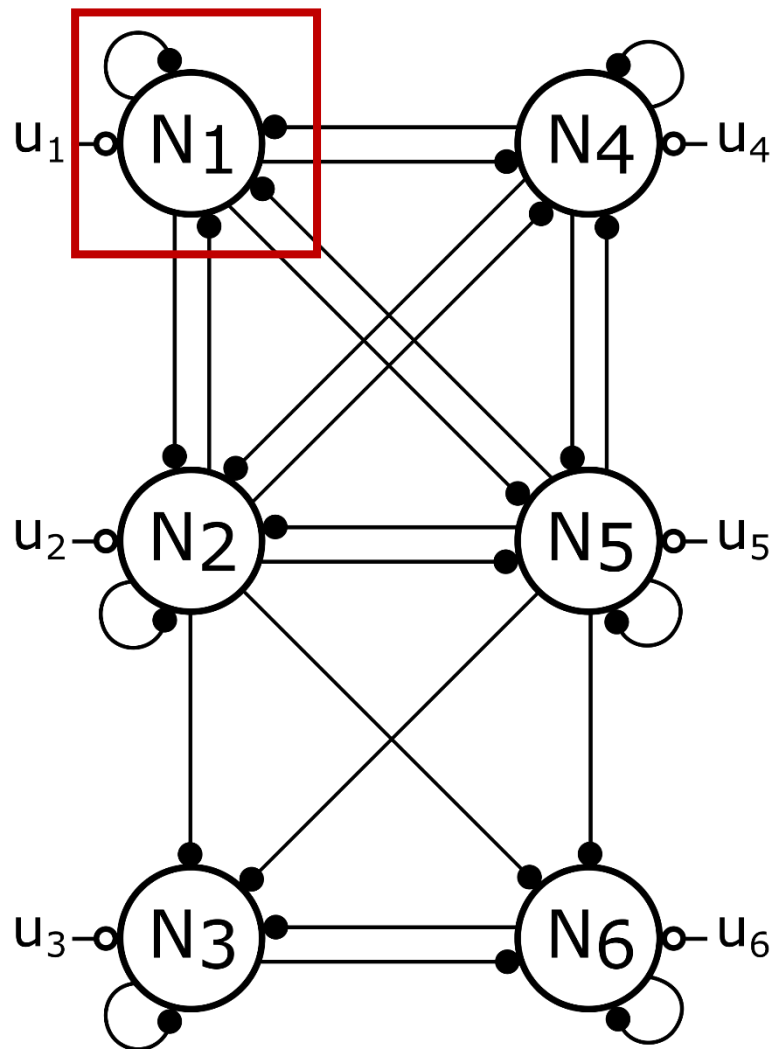
Forward gait modulation in 2D scenarios

- Walking gaits
- Running gaits

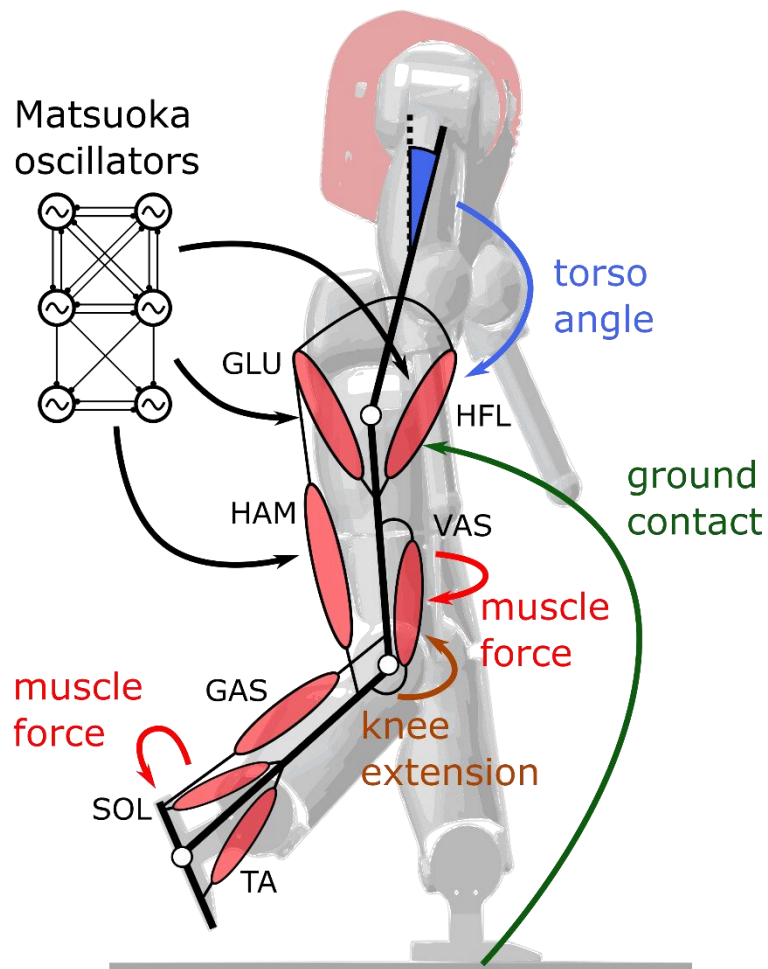
Steering control in 3D scenarios

Conclusion

Central pattern generator (CPG)



2D walking gaits



Combining reflexes with a CPG

- Proximal muscles mainly driven by **CPG**
- Distal muscles mainly driven by **reflexes**

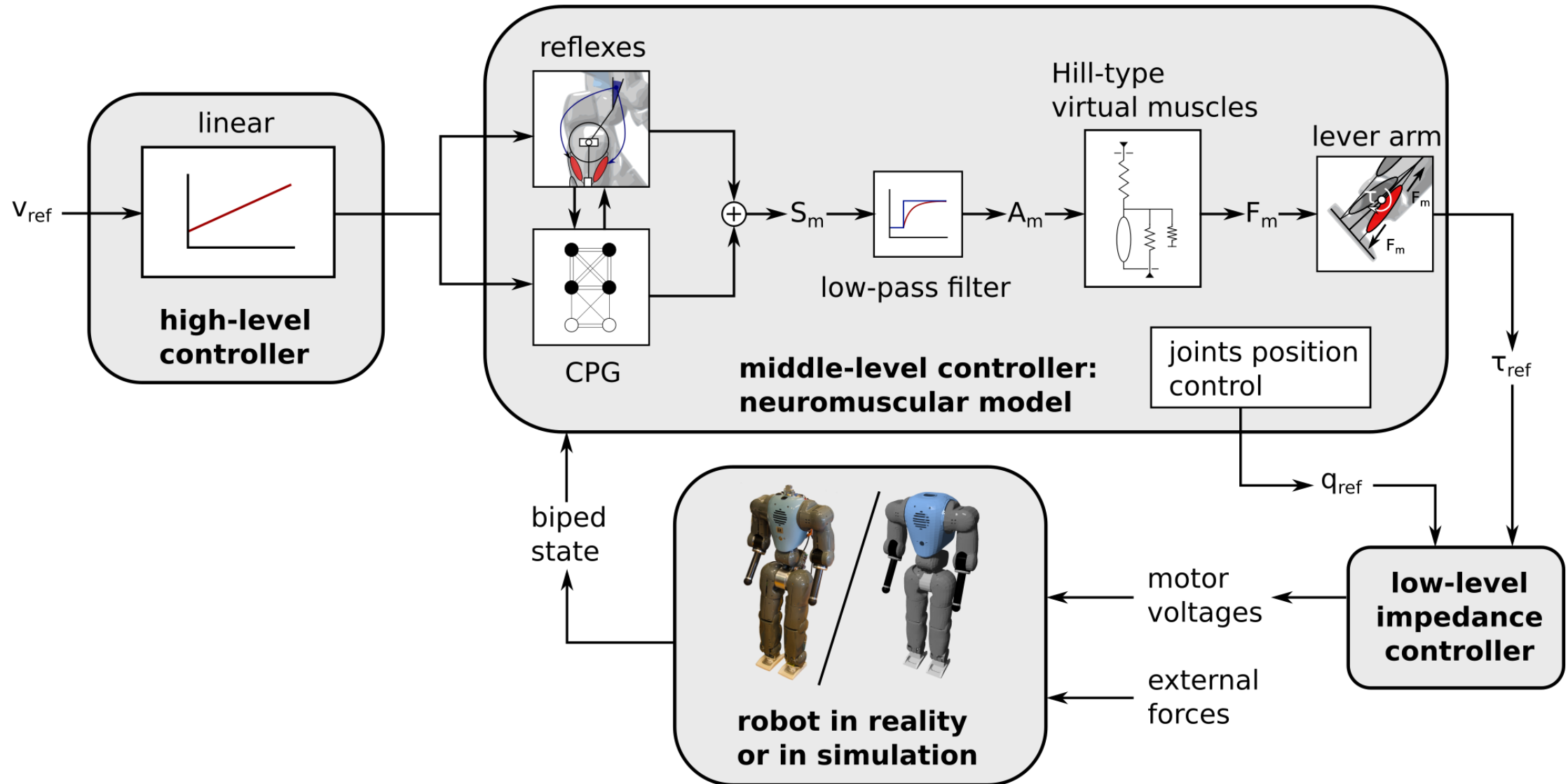
High-level parameters adapted as linear functions of the target speed

- 4 CPG parameters
- 1 reflex parameter

Getting different gaits

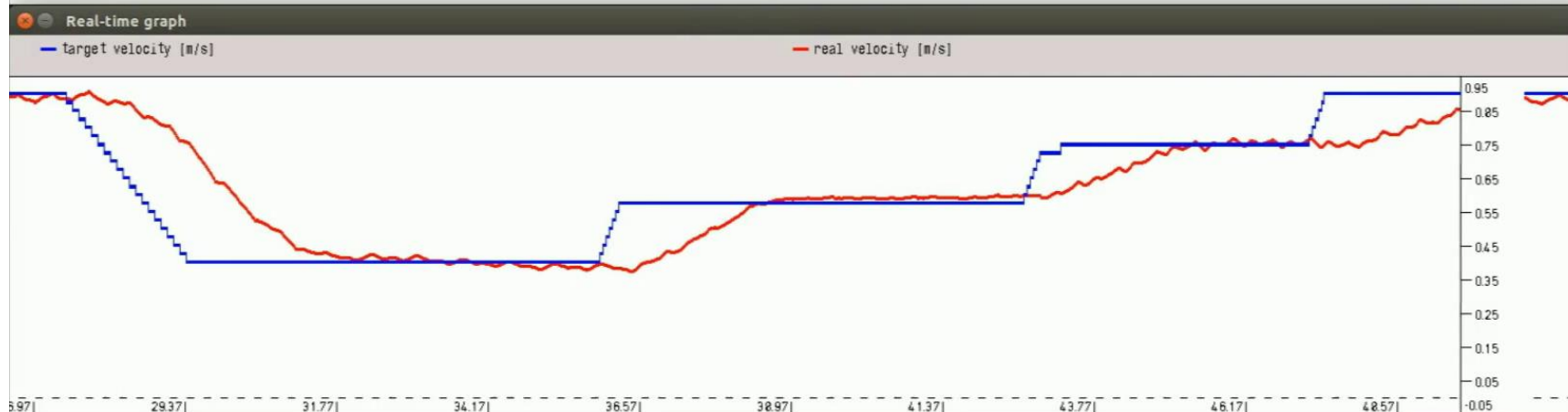
- Speeds ranging from **0.4 m/s to 0.9 m/s**
- All parameters **co-optimized** in one single optimization

General control framework

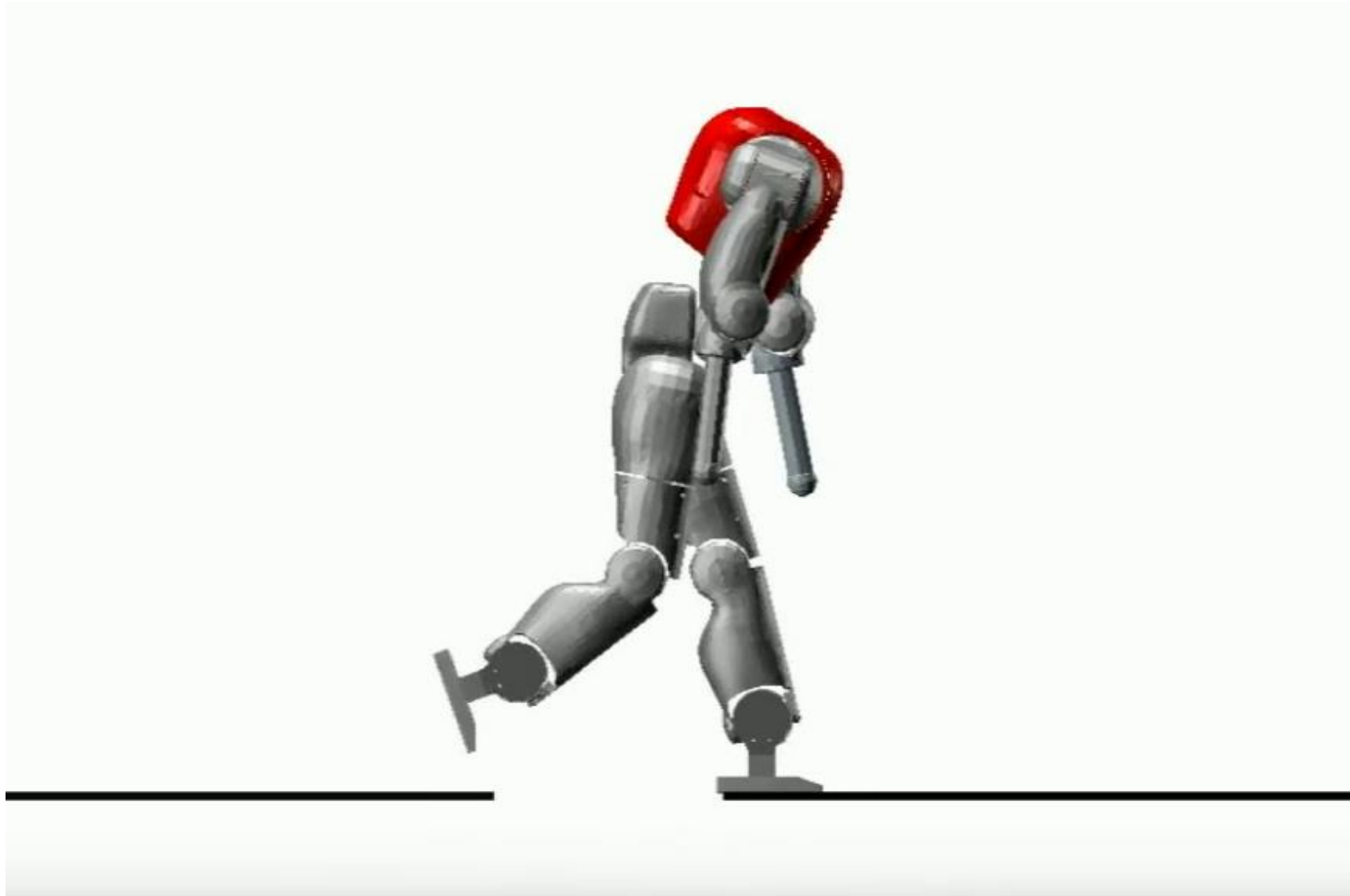


Forward speed modulation during 2D walking

stride length and
stride frequency
continuously adapted

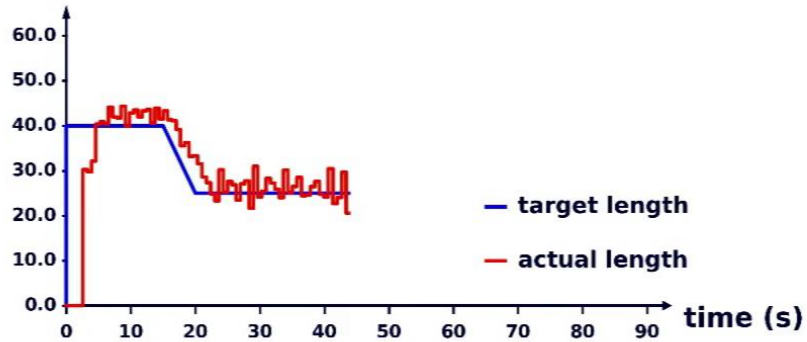


Crossing a hole with step length modulation

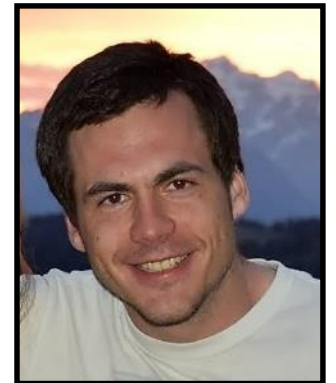
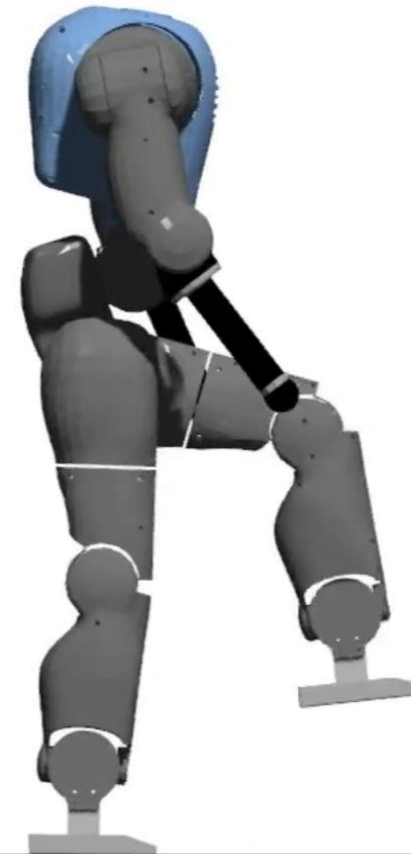
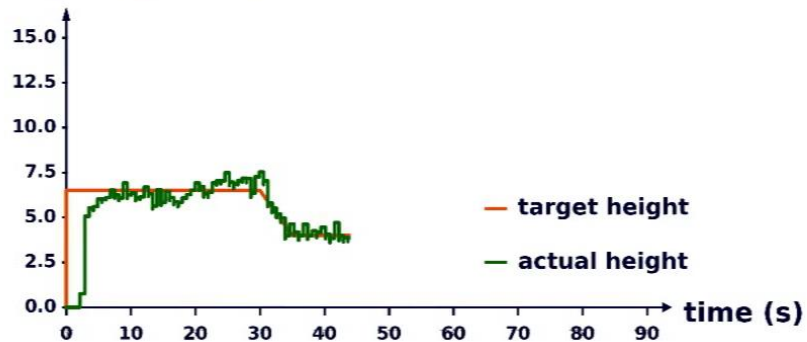


Step height and length adaptations

step length (cm)



step height (cm)



Philippe Greiner

Introduction & Methods

Reflex-based controller

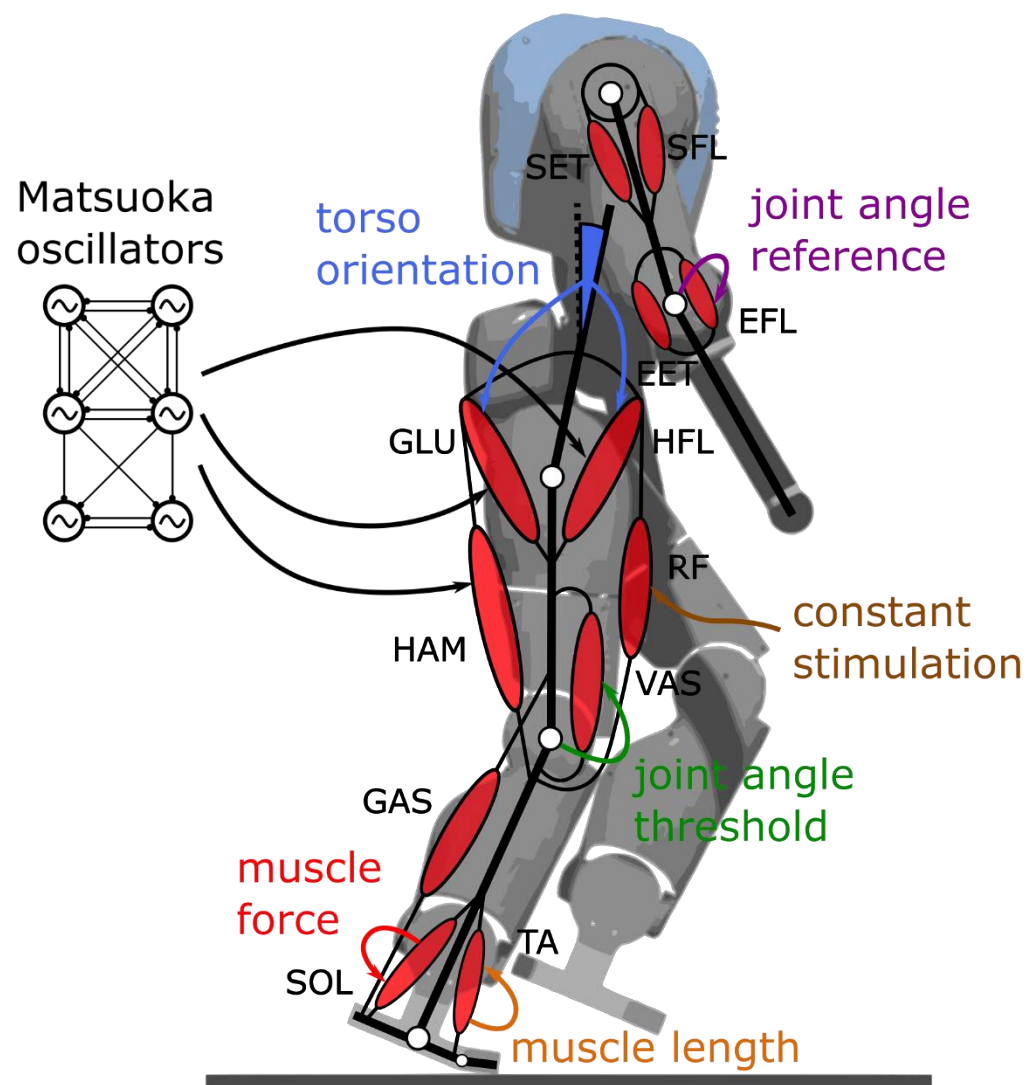
Forward gait modulation in 2D scenarios

- Walking gaits
- Running gaits

Steering control in 3D scenarios

Conclusion

2D running gaits



Extension to running gaits

- **High-level parameters** modulated as functions of the target speed
- All parameters **co-optimized** in one single optimization
- Speeds ranging from **1.3 m/s to 1.7 m/s**

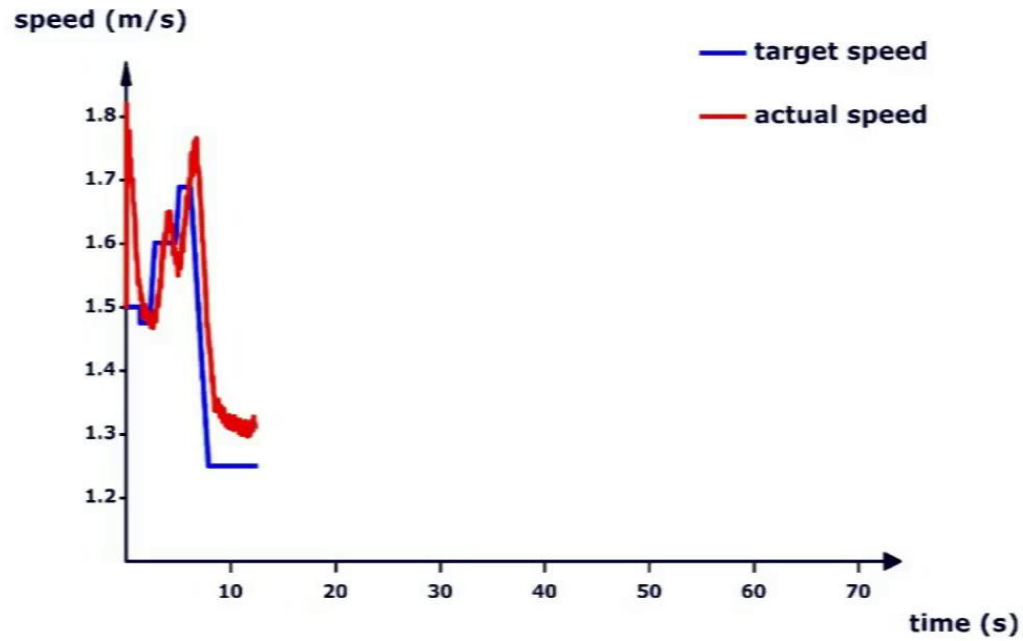


Bruno Somers



Matthew Harding

Forward speed modulation during 2D running



x 1/8



Introduction & Methods

Reflex-based controller

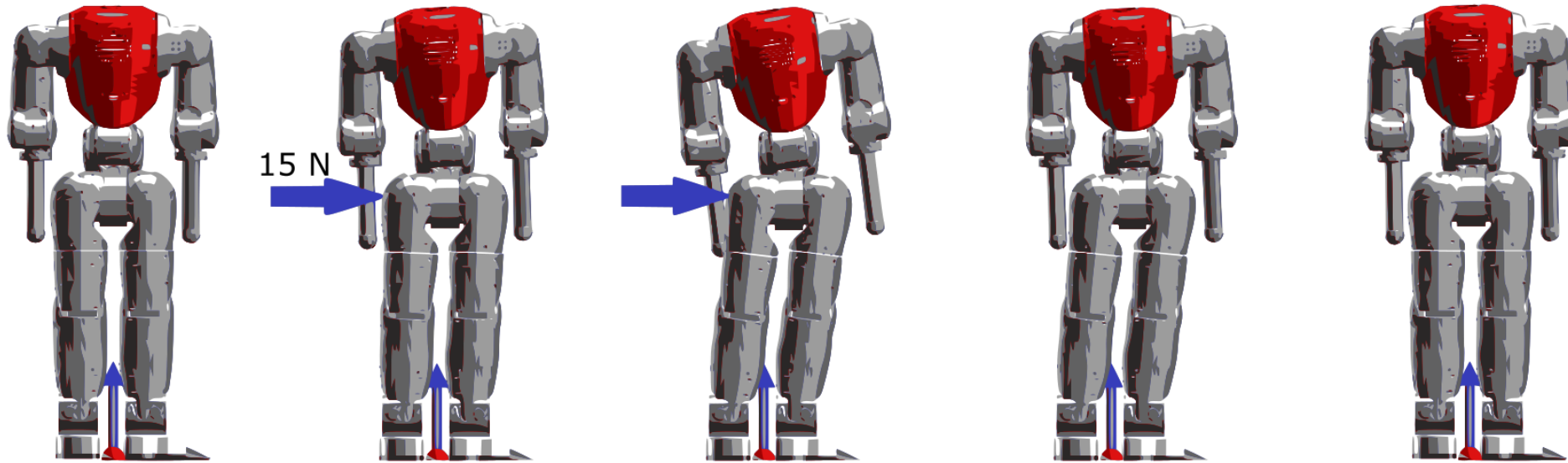
Forward gait modulation in 2D scenarios

Steering control in 3D scenarios

- Bio-inspired balance controller
- Straight walking
- Heading control

Conclusion

Bio-inspired balance controller



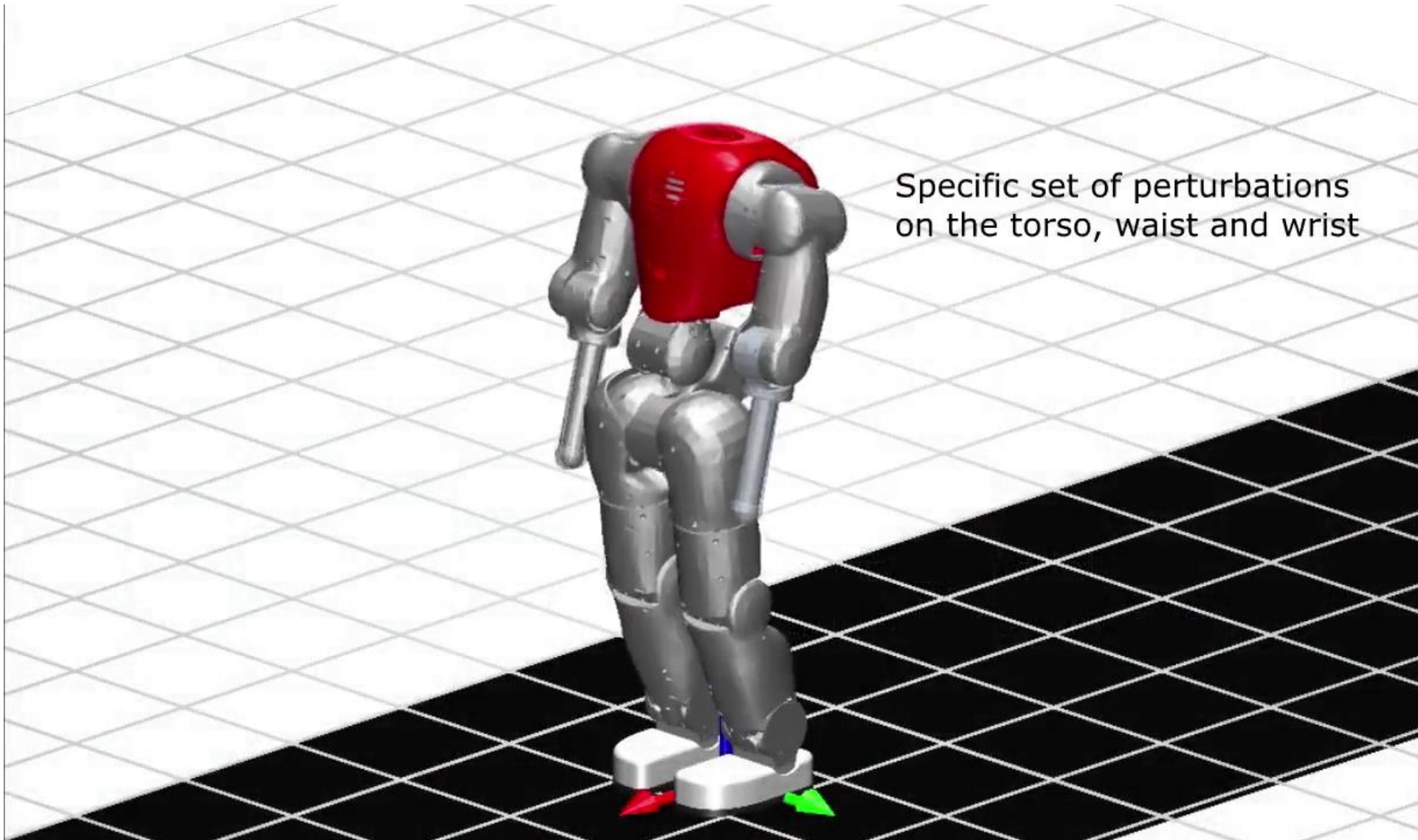
Balance controller

- Resist to external **perturbations**
- Automatically **learn** stimulation patterns
- Control the center of mass (**COM**) position



François Heremans

Resisting to external perturbations



Introduction & Methods

Reflex-based controller

Forward gait modulation in 2D scenarios

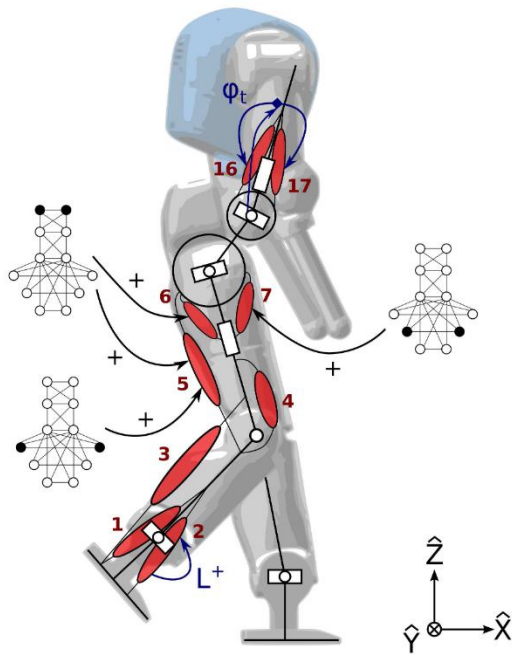
Steering control in 3D scenarios

- Bio-inspired balance controller
- **Straight walking**
- Heading control

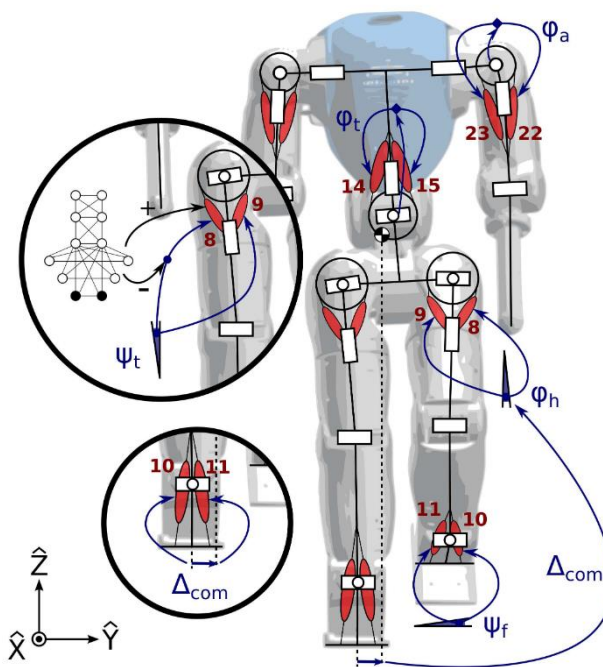
Conclusion

Extension to 3D control

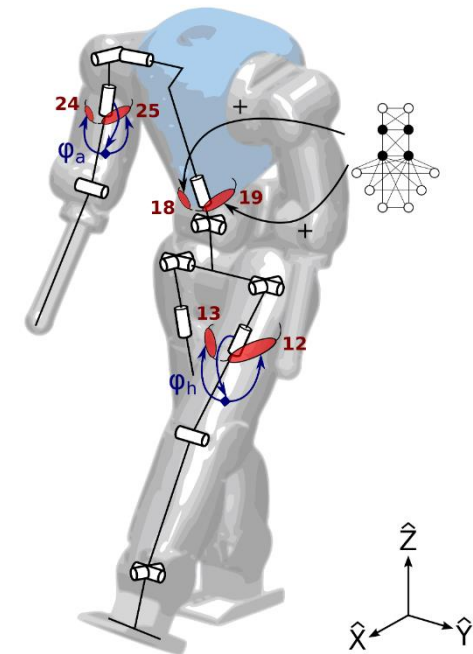
- New virtual **muscles** (in all the planes)
- New **reflex** signals
- **CPG** structure incremented



Sagittal plane

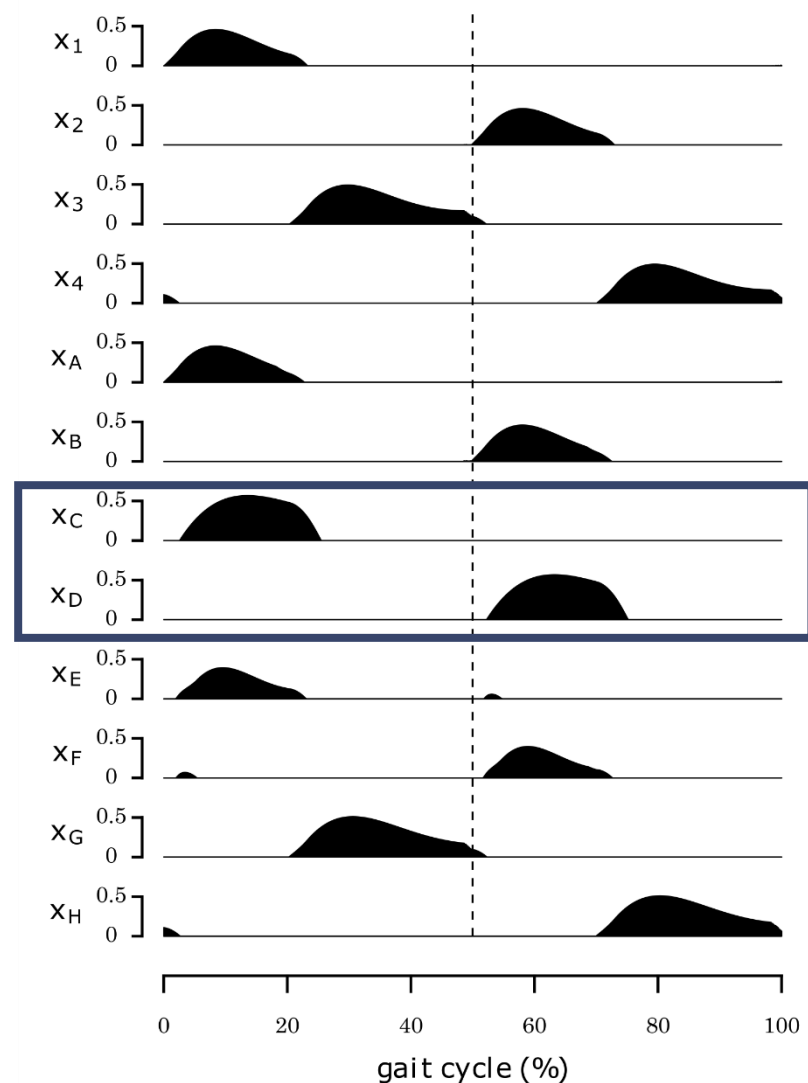
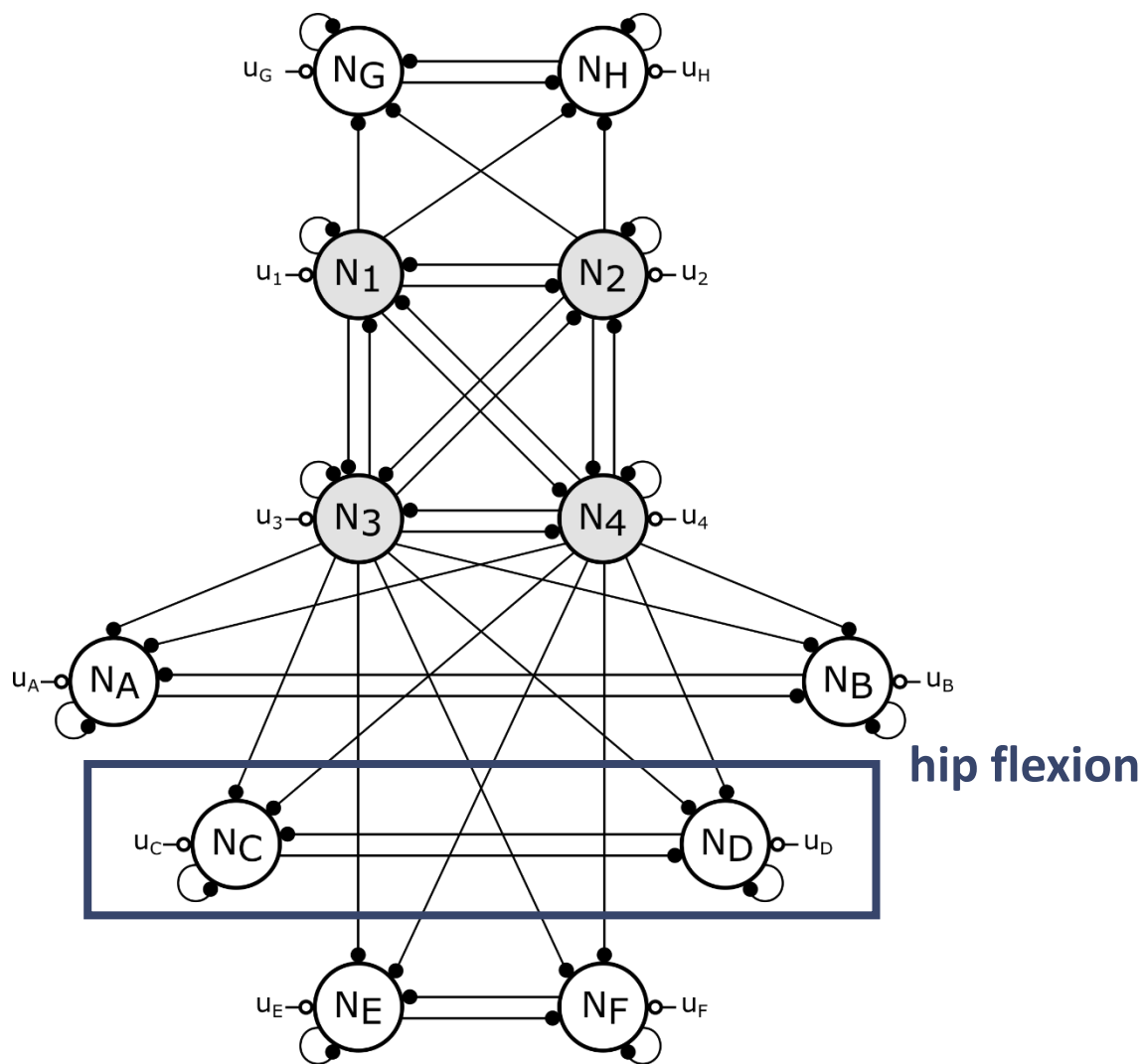


Lateral plane

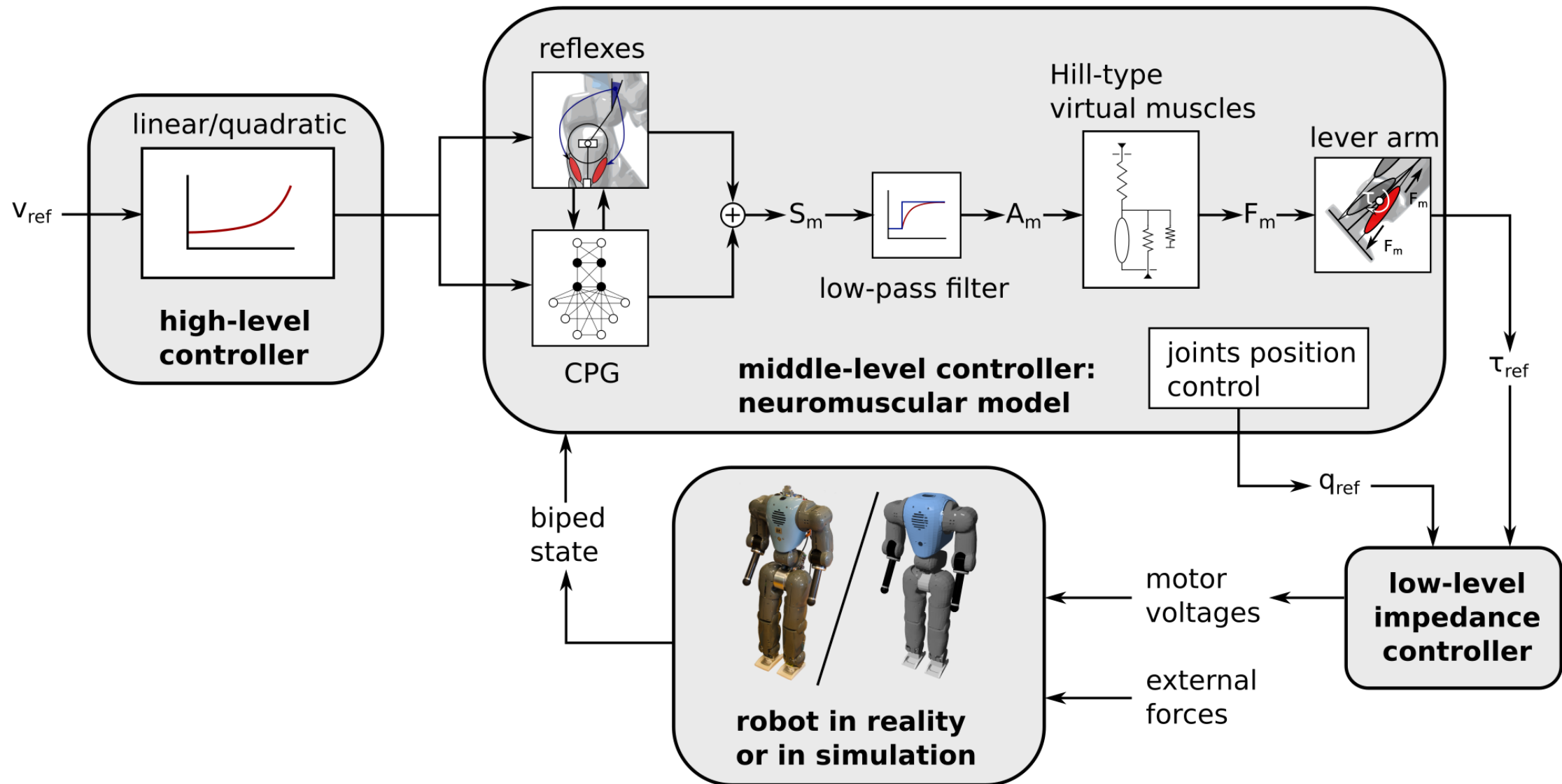


Transverse plane

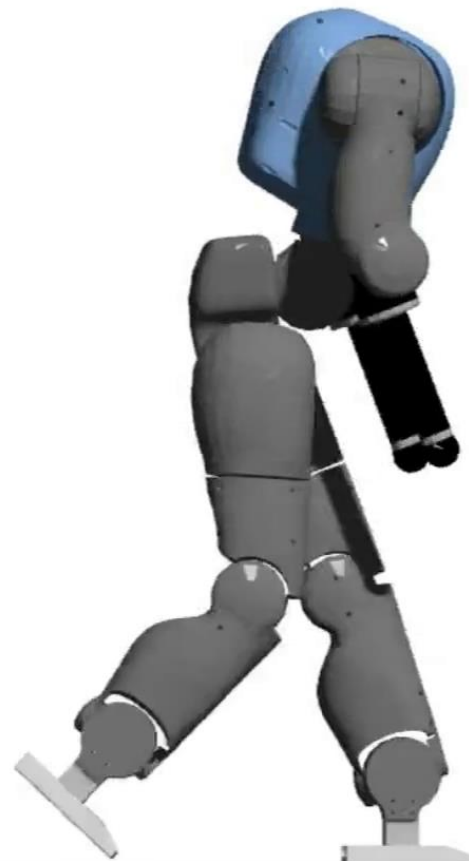
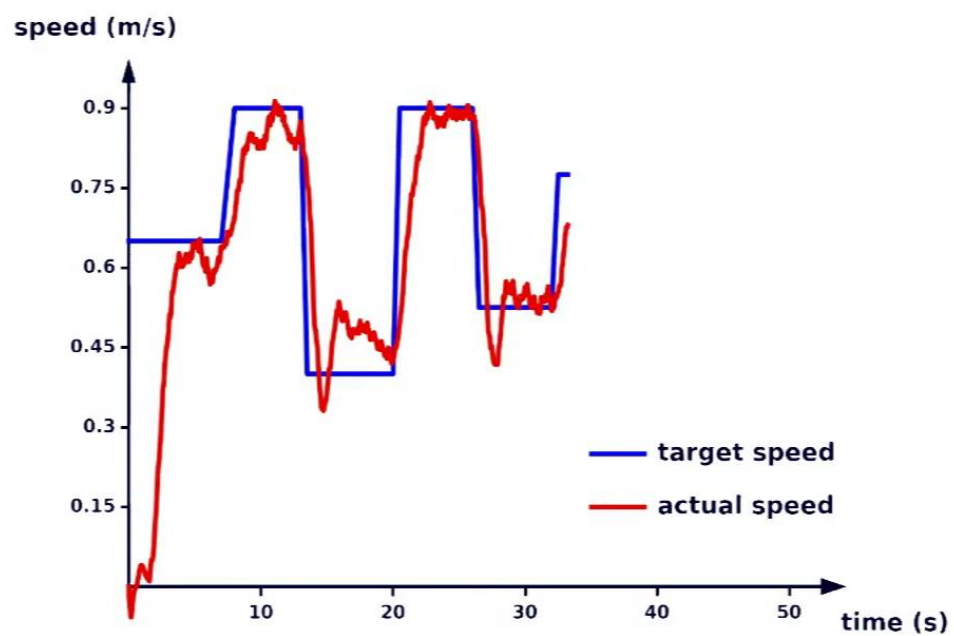
CPG structure for straight walking



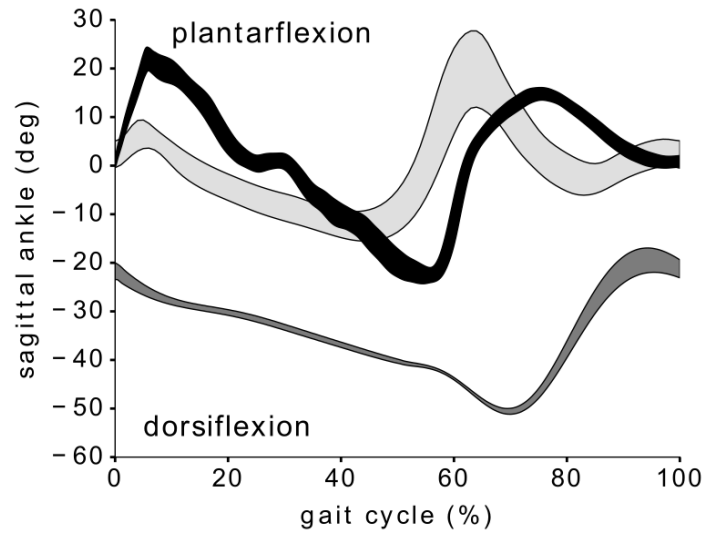
General control framework



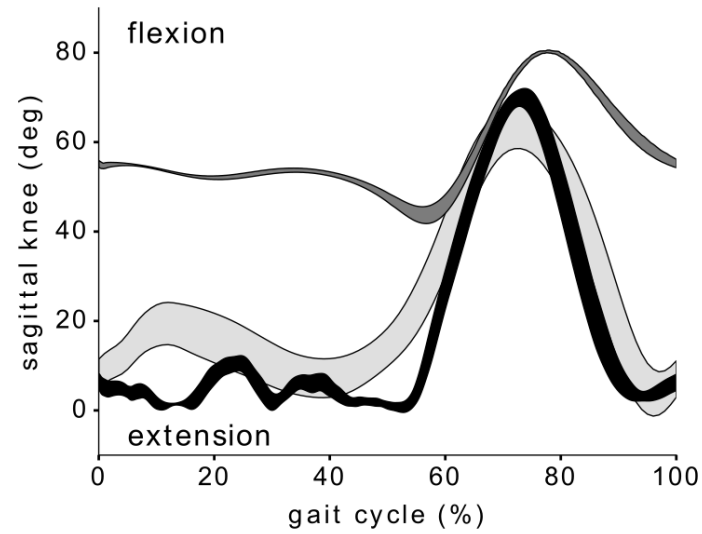
Forward speed tracking



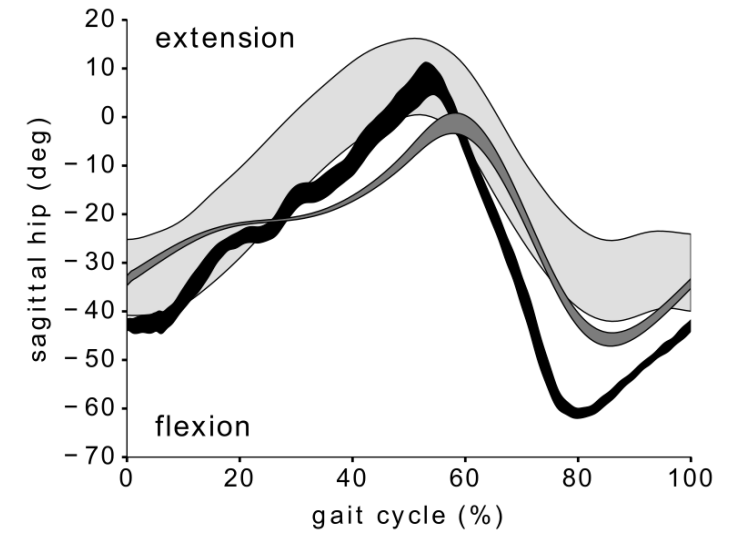
Comparisons to human and traditional data



sagittal ankle angle



sagittal knee angle



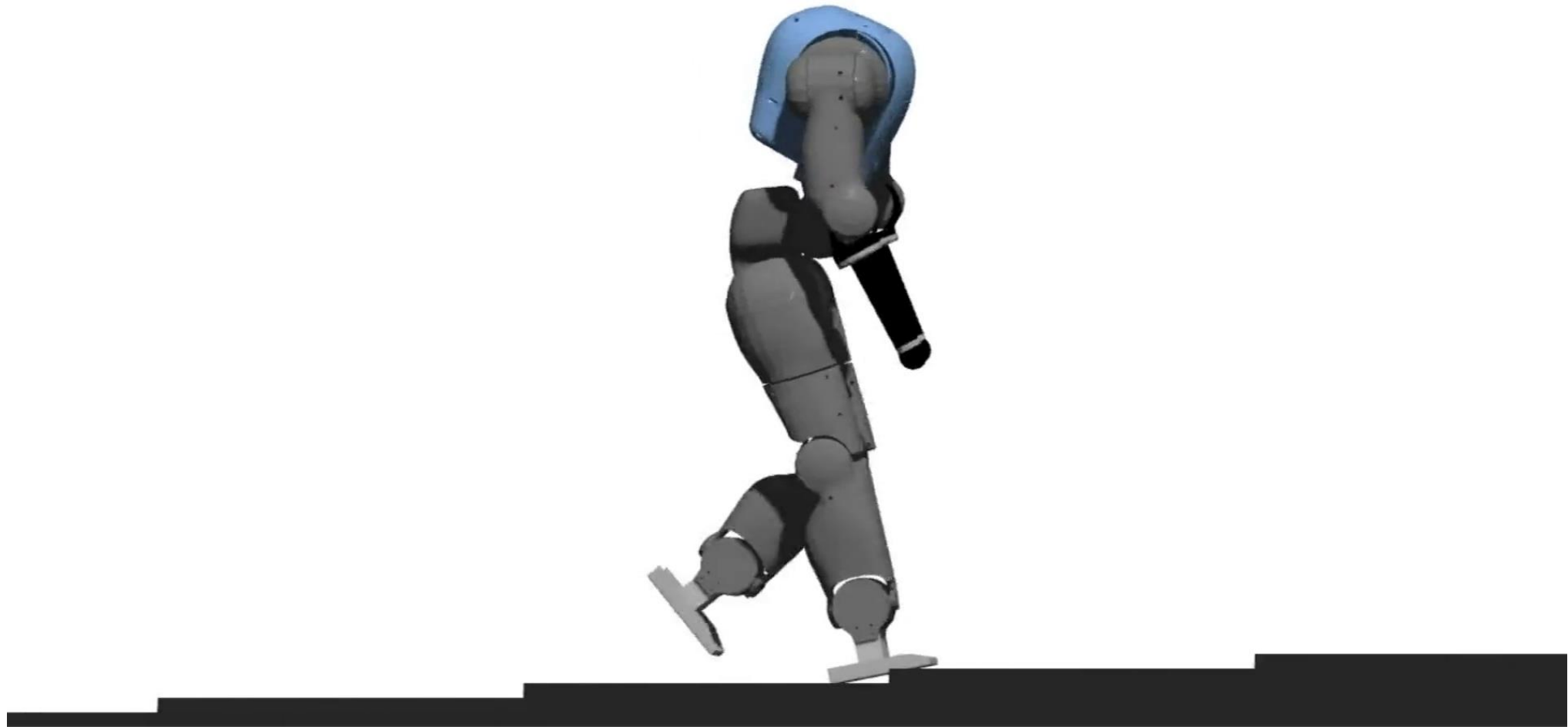
sagittal hip angle

- neuromuscular
- human-data
- traditional control

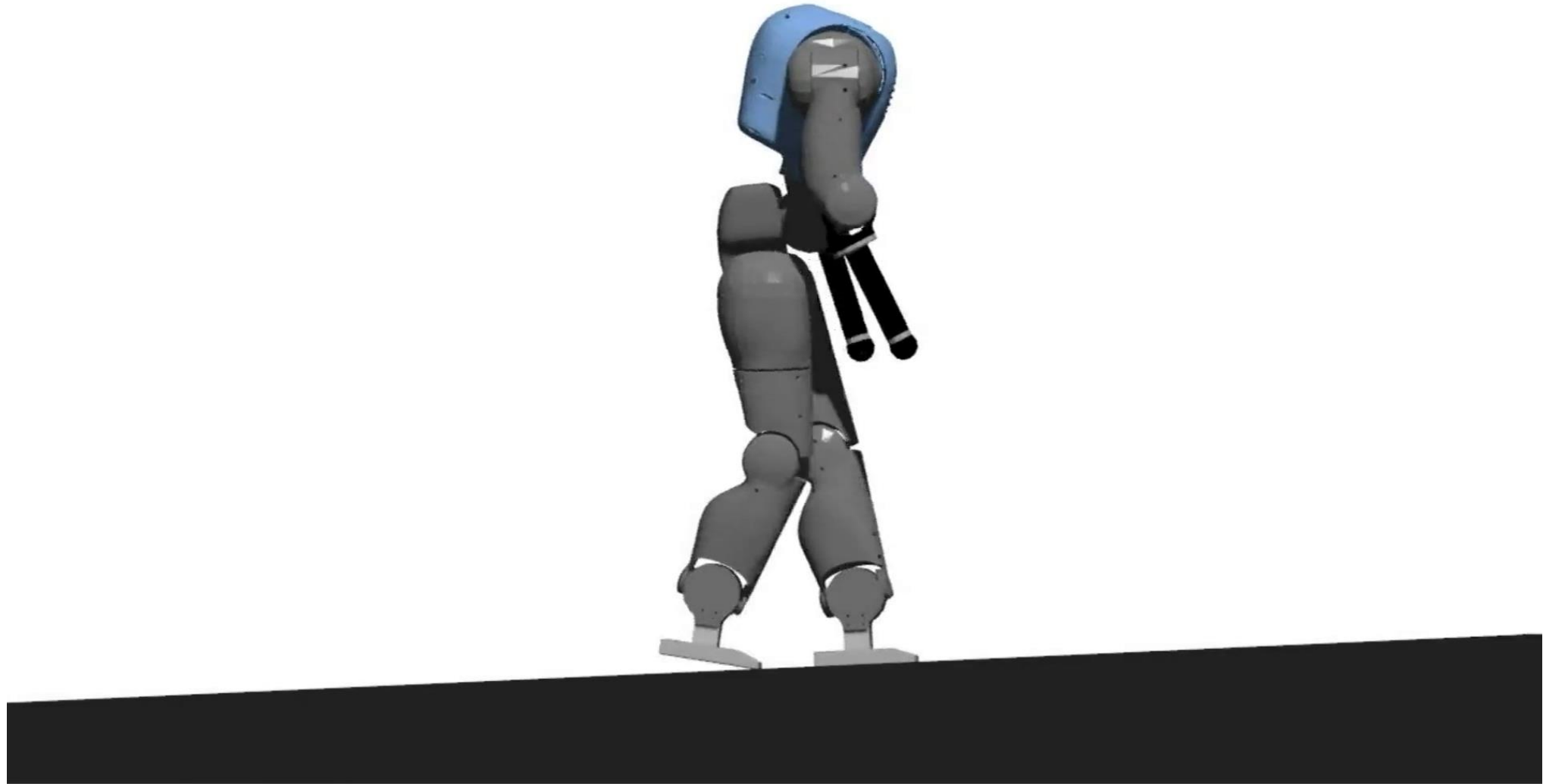
➔ Neuromuscular controller

- more human-like
- more energetically efficient
- faster speeds

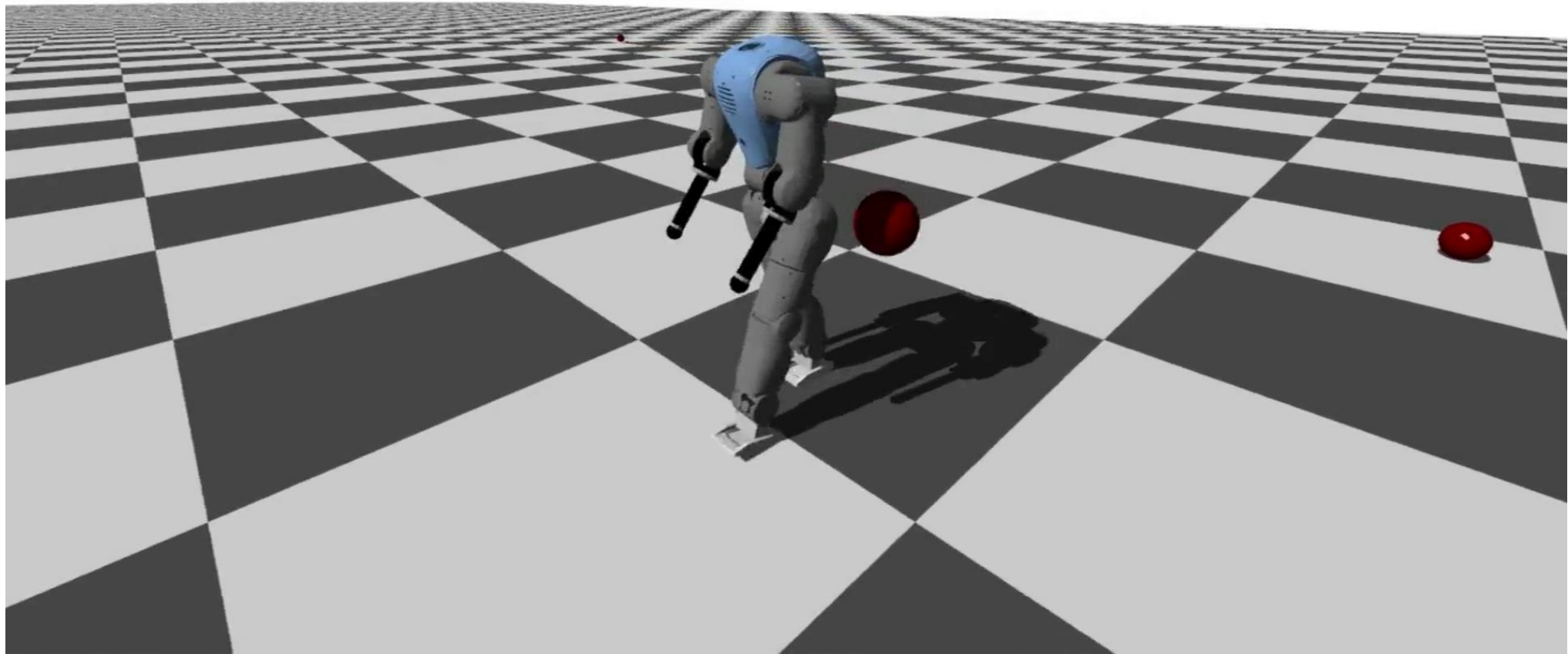
Blind walking: stairs



Blind walking: slope



Blind walking impacted by flying balls



Introduction & Methods

Reflex-based controller

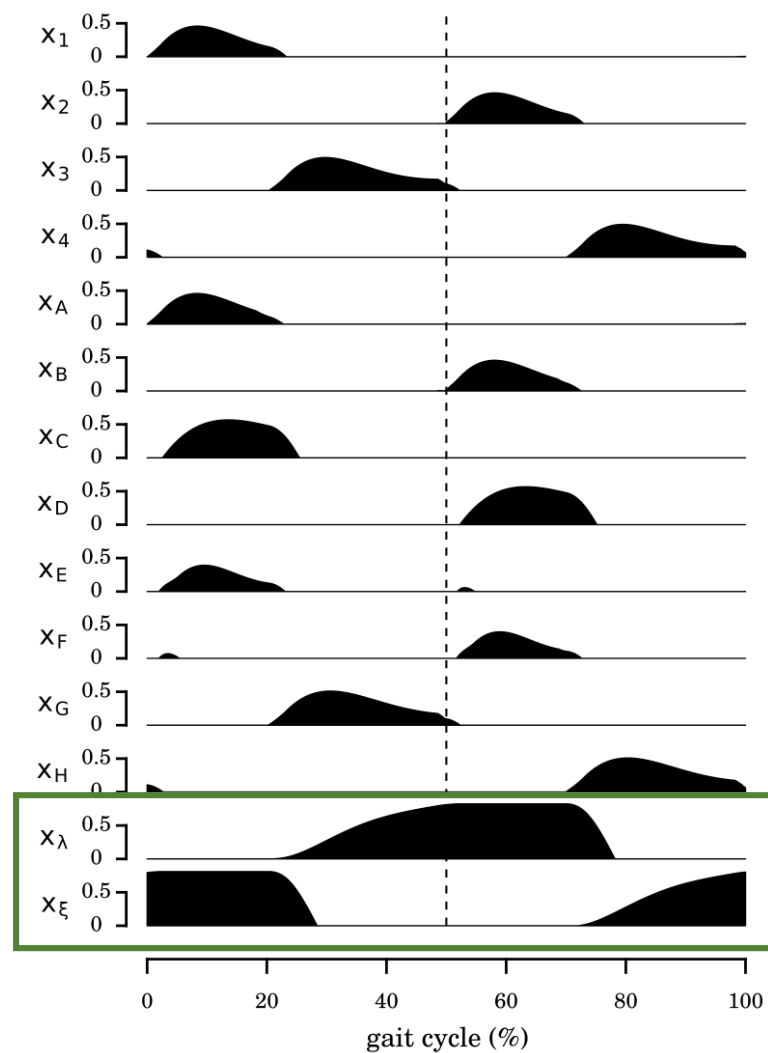
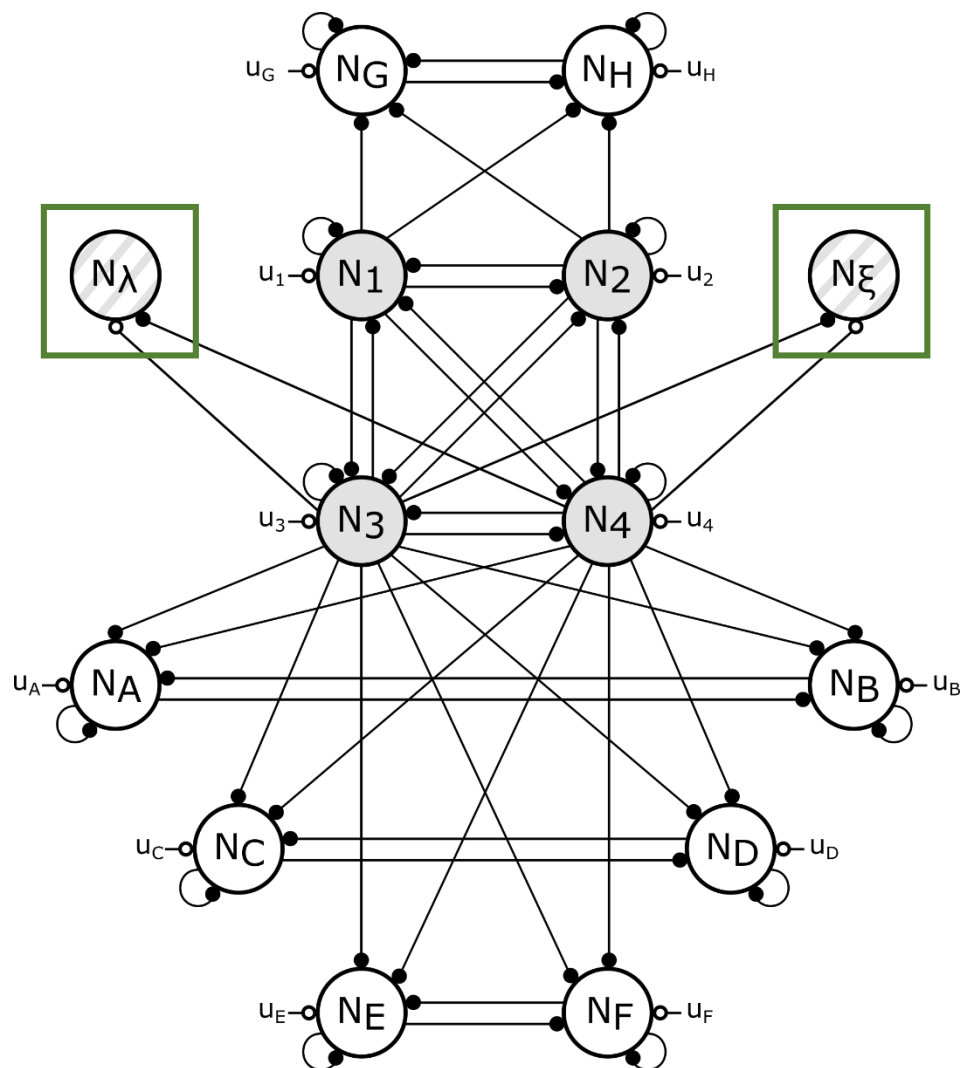
Forward gait modulation in 2D scenarios

Steering control in 3D scenarios

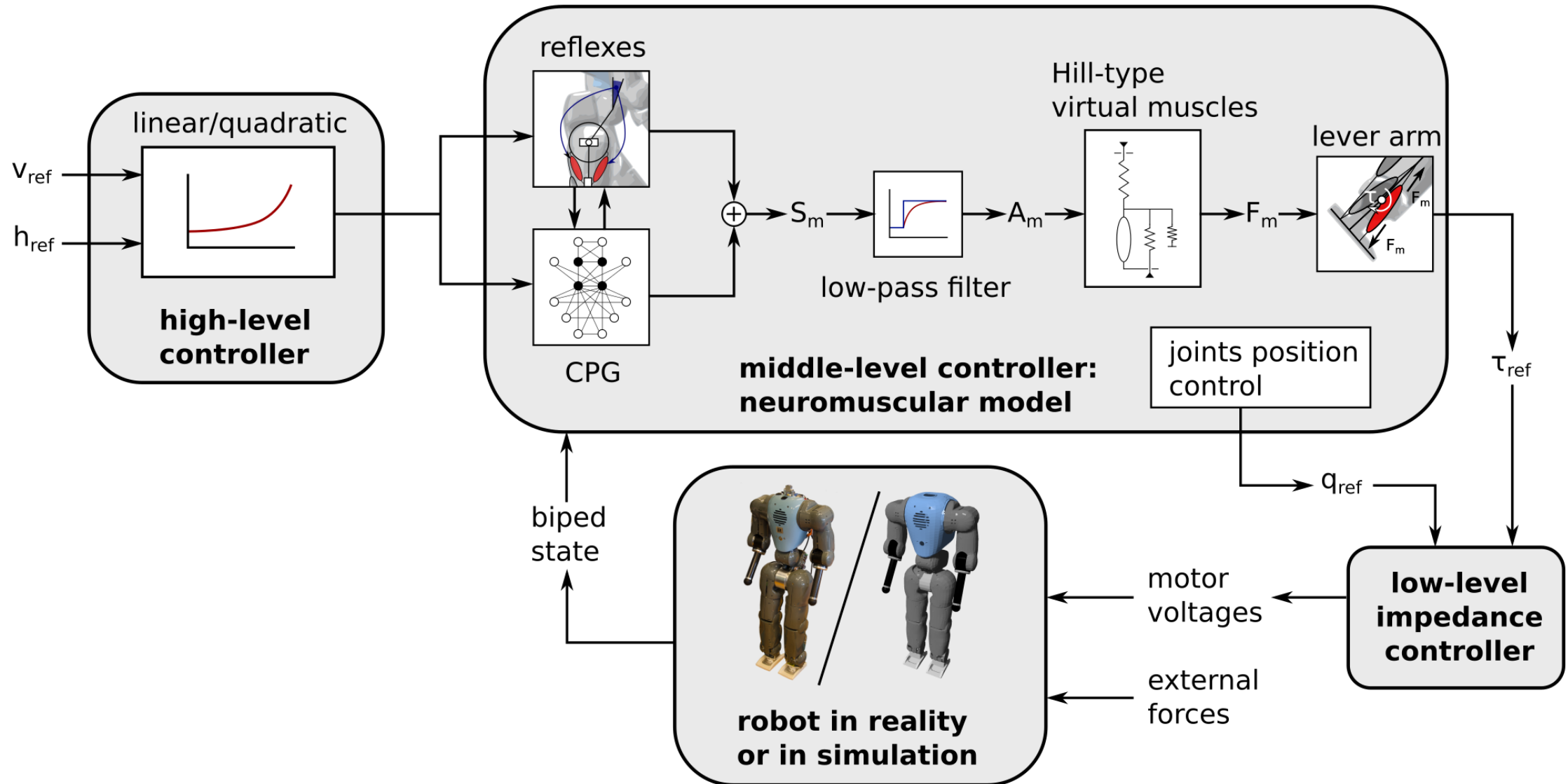
- Bio-inspired balance controller
- Straight walking
- Heading control

Conclusion

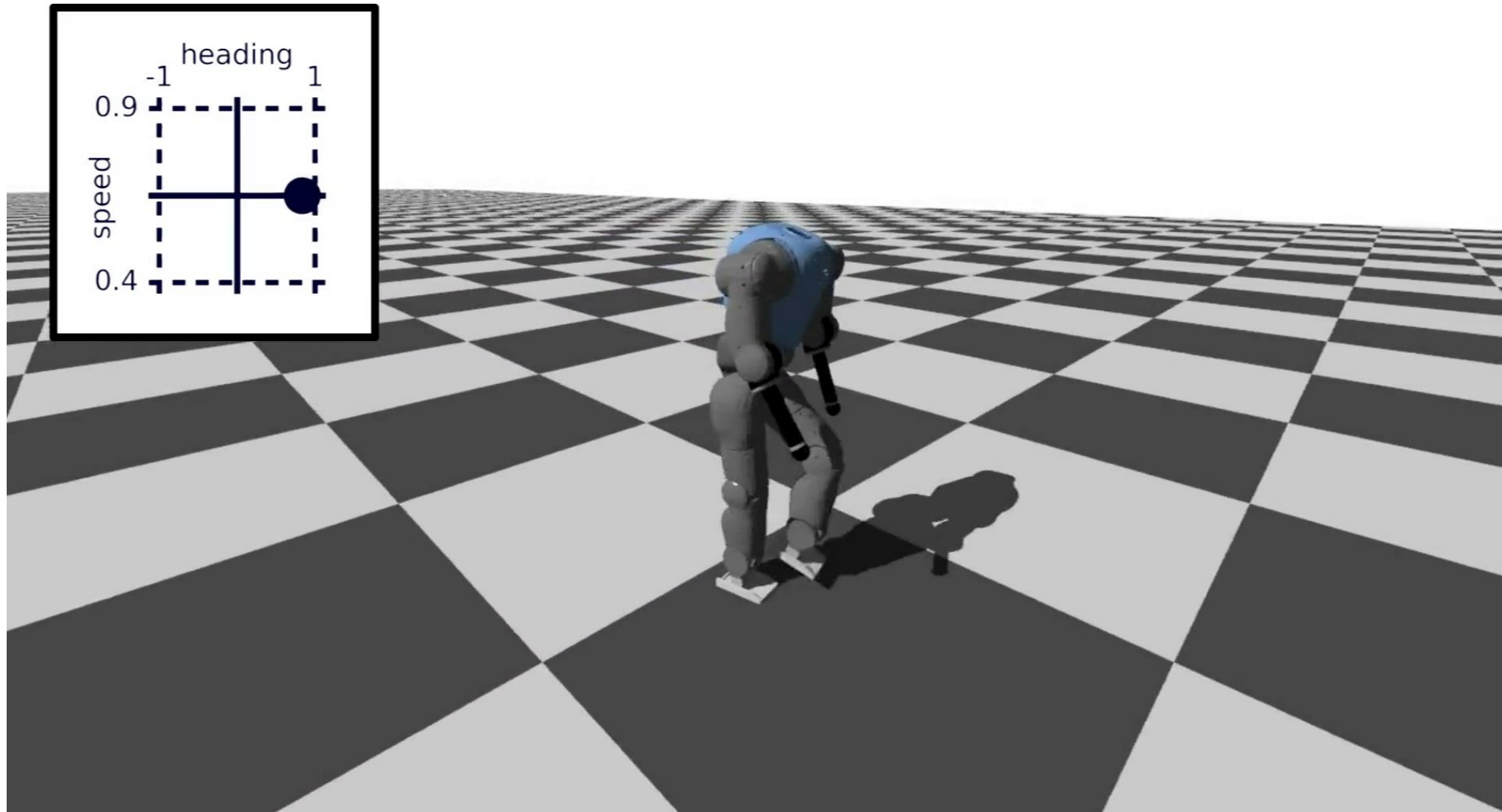
CPG structure for heading control



General control framework

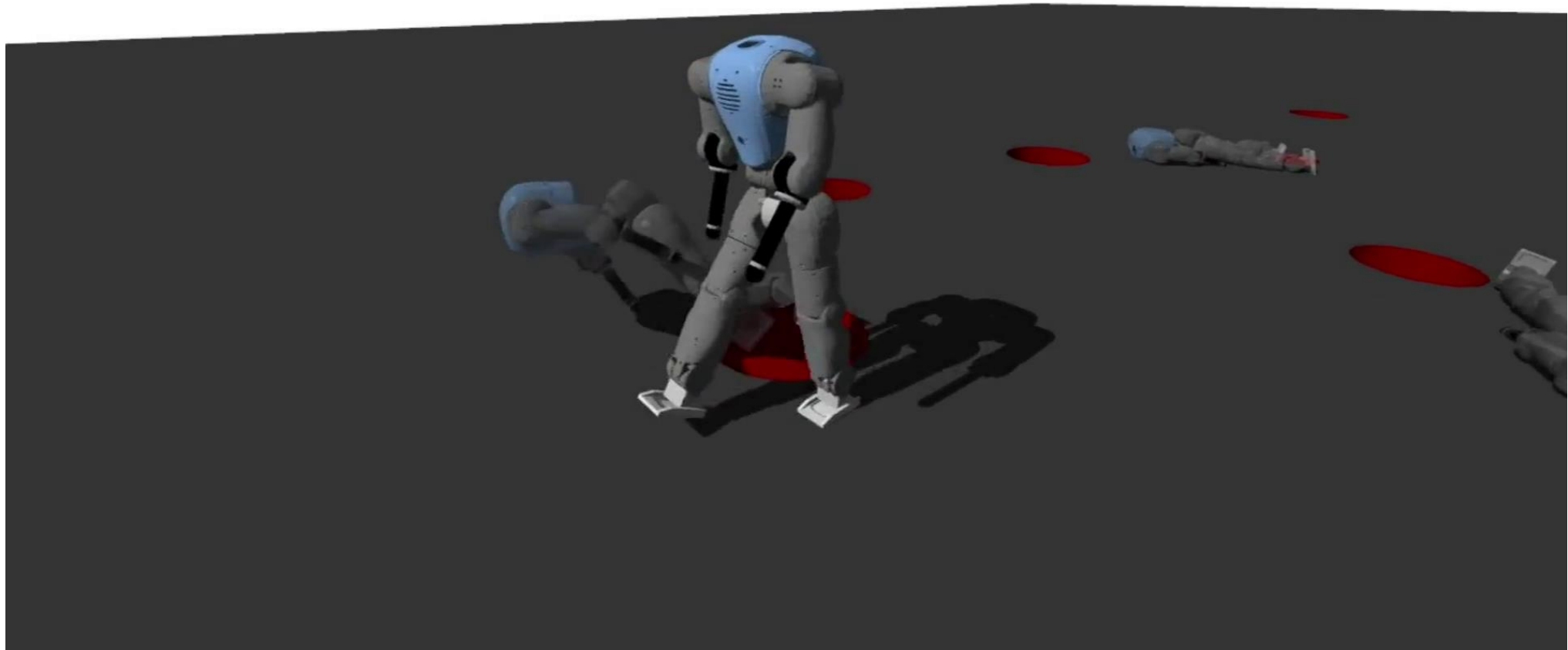


Forward speed and steering control



3D walking: avoiding holes

Depending on the commands received, the walker either falls in a hole or escapes it.



Introduction & Methods

Reflex-based controller

Forward gait modulation in 2D scenarios

Steering control in 3D scenarios

Conclusion

Original contributions

Reflex-based controller

- **Experimental** validation of a neuromuscular controller
- Porting the controllers to **different robots**
- Hill **muscle model** numerical integration
- Feet with human-like **compliance**

Gait modulation in 2D scenarios

- Gait modulation during **walking** gaits
- Speed modulation during **running** gaits

Steering control in 3D scenarios

- Bio-inspired **balance** controller
- Forward speed modulation during **straight** walking
- **Heading** modulation (steering control)

Future directions

- Extend the **panel of motions**
 - stairs climbing
 - side stepping
 - ...
- Study **gait finalization**
- Obtain **slow walking** gaits
 - speeds below 0.3 m/s
- Investigate **real human** locomotion
- Test the 3D walking controller on a **real robot**
- ...

Acknowledgements

Advisors



Prof. Renaud Ronsse



Prof. Auke Ijspeert

Master theses & semester project students



François Heremans



Adrien De Coninck



Bruno Somers



Philippe Greiner



Matthew Harding

Acknowledgements



CEREM



BioRob



Acknowledgements



List of publications

Journal papers

- **Van der Noot N**, Ijspeert AJ and Ronsse R (conditionally accepted) **Bio-inspired controller achieving forward speed modulation with a 3D bipedal walker**. *International Journal of Robotics Research*.
- Zbova AA, Habra T, **Van der Noot N**, Dallali H, Tsagarakis NG, Fiset P and Ronsse R (2017) **Multi-physics modelling of a compliant humanoid robot**. *Multibody System Dynamics* 39 (1-2), pp. 95-114.

Conference papers

- Heremans F, **Van der Noot N**, Ijspeert AJ and Ronsse R (2016) **Bio-inspired balance controller for a humanoid robot**. In: *2016 6th IEEE International Conference on Biomedical Robotics and Biomechatronics (BioRob)*, Singapore, 26-29 June 2016, pp. 441-448.
- Colasanto L, **Van der Noot N** and Ijspeert AJ (2015) **Bio-inspired walking for humanoid robots using feet with human-like compliance and neuromuscular control**. In: *2015 IEEE-RAS 15th International Conference on Humanoid Robots (Humanoids)*, Seoul, 3-5 Nov. 2015, pp. 26-32.

List of publications

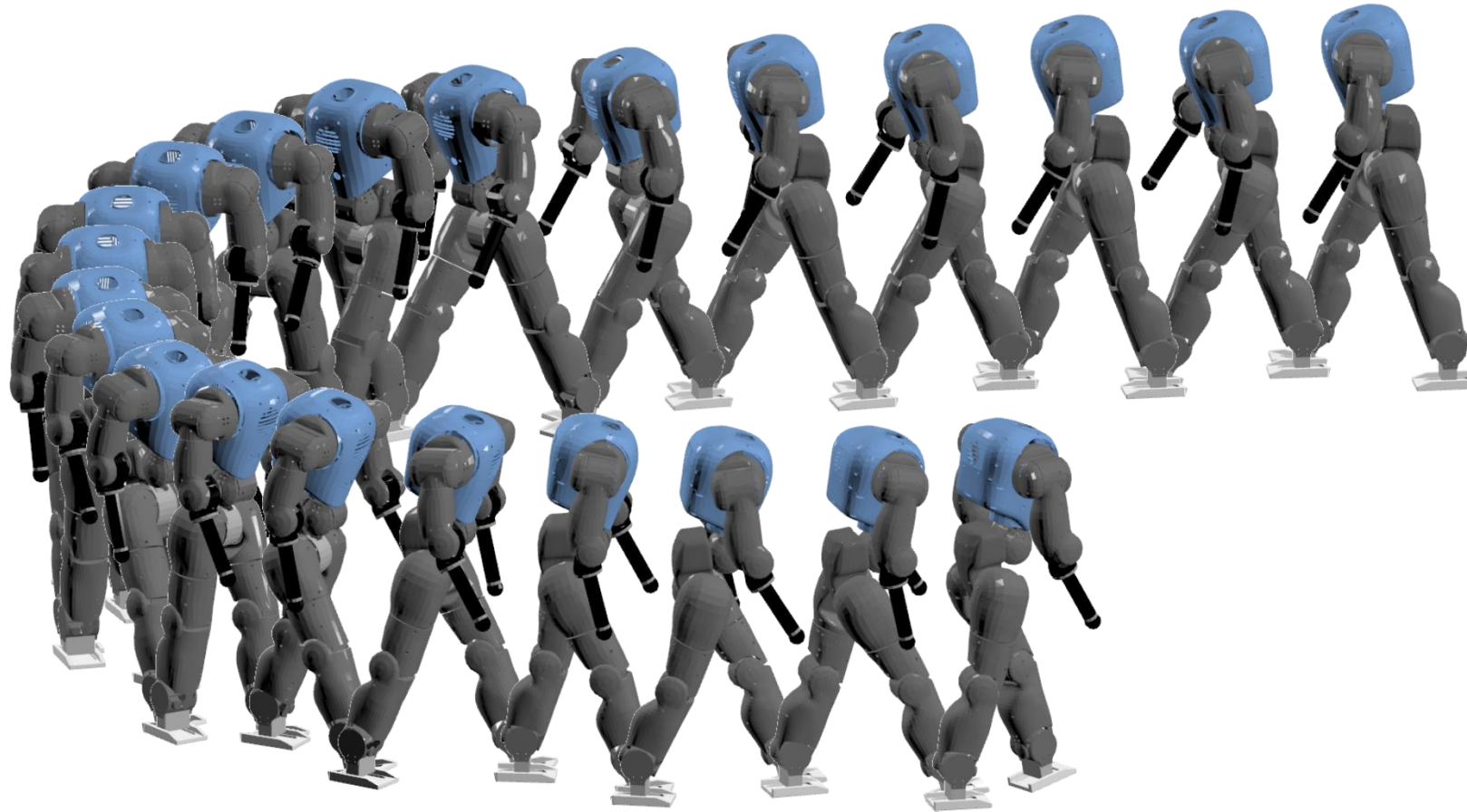
- **Van der Noot N**, Colasanto L, Barrea A, van den Kieboom J, Ronsse R and Ijspeert AJ (2015) **Experimental validation of a bio-inspired controller for dynamic walking with a humanoid robot**. In: *2015 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*, Hamburg, Sept. 28 2015-Oct. 2 2015, pp. 393-400.
- Zobova AA, Habra T, **Van der Noot N**, Dallali H, Tsagarakis NG, Fiset P and Ronsse R (2015) **Multi-physics modelling of a compliant humanoid robot**. In: *ECCOMAS Thematic Conference Multibody Dynamics 2015*, Barcelona, 29 June-02 July 2015.
- **Van der Noot N**, Ijspeert AJ and Ronsse R (2015) **Biped gait controller for large speed variations, combining reflexes and a central pattern generator in a neuromuscular model**. In: *2015 IEEE International Conference on Robotics and Automation (ICRA)*, Seattle, WA, 26-30 May 2015, pp. 6267-6274.
- **Van der Noot N** and Barrea A (2014) **Zero-Moment Point on a bipedal robot under bio-inspired walking control**. In: *MELECON 2014 - 17th IEEE Mediterranean Electrotechnical Conference*, Beirut, 13-16 April 2014, pp. 85-90. DOI: 10.1109/MELCON.2014.6820512.

List of publications

Poster presentations

- **Van der Noot N**, Ijspeert AJ and Ronsse R (2016) **Neuro-Muscular Controller Based on Reflexes and a Central Pattern Generator to Achieve Gait Modulation**. In: *Koroibot Final Workshop*, Heidelberg, 13-14 September 2016.
- **Van der Noot N**, Ijspeert AJ and Ronsse R (2016) **Humanoid Robot Control Recruiting Muscles, Reflexes and a Central Pattern Generator**. In: *IEEE-EMB Benelux Chapter and the 14th National Day on Biomedical Engineering*, Brussels, 4 March 2016.
- **Van der Noot N**, Colasanto L, Ronsse R and Ijspeert AJ (2015) **Porting Reflex-Based Muscles Control to Real Humanoid Robots**. In: *2015 IEEE International Conference on Robotics and Automation (ICRA) - Workshop on Dynamic Locomotion and Balancing*, Seattle, WA, 26 May 2015.
- **Van der Noot N**, Dzeladini F, Ijspeert AJ and Ronsse R (2014) **Simplification of the Hill Muscle Model Computation for Real-Time Walking Controllers with Large Time Steps**. In: *Dynamic Walking*, Zurich, 10-13 June 2014.

Respite finem



Introduction & Methods

Reflex-based controller

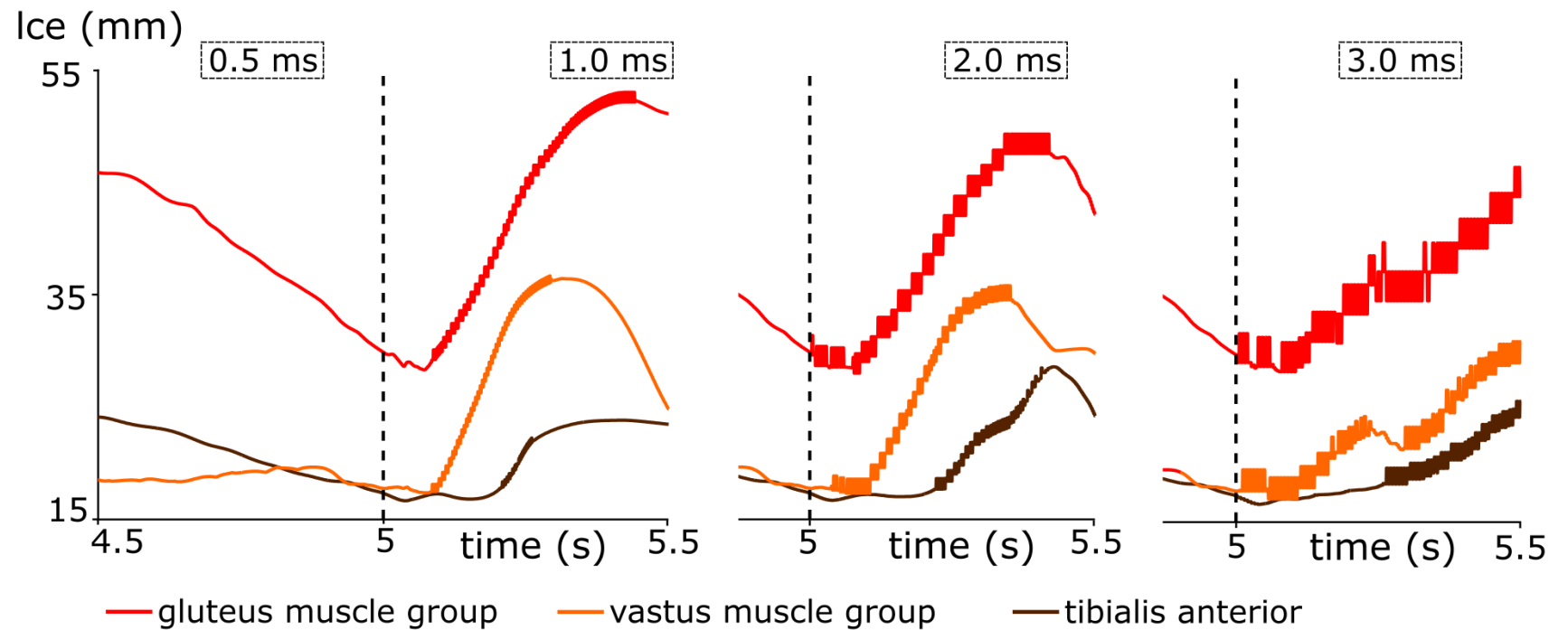
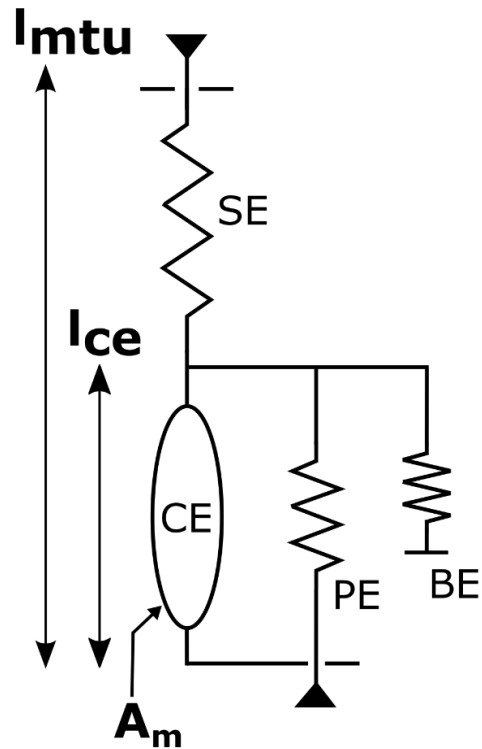
Forward speed modulation in 2D scenarios

Steering control in 3D scenarios

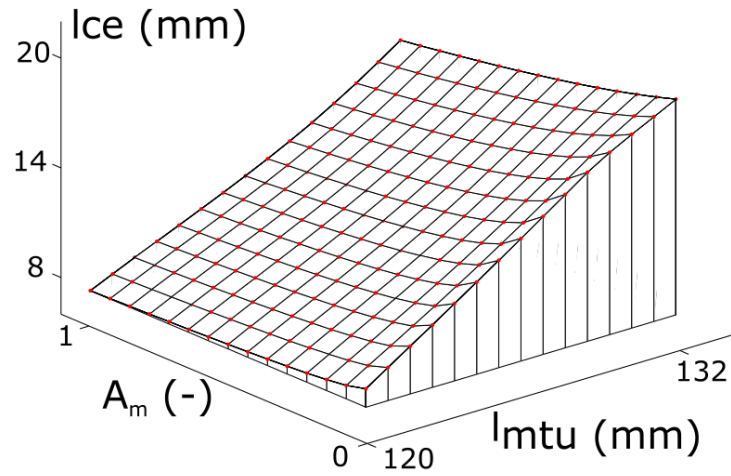
Conclusion

Supplementary material

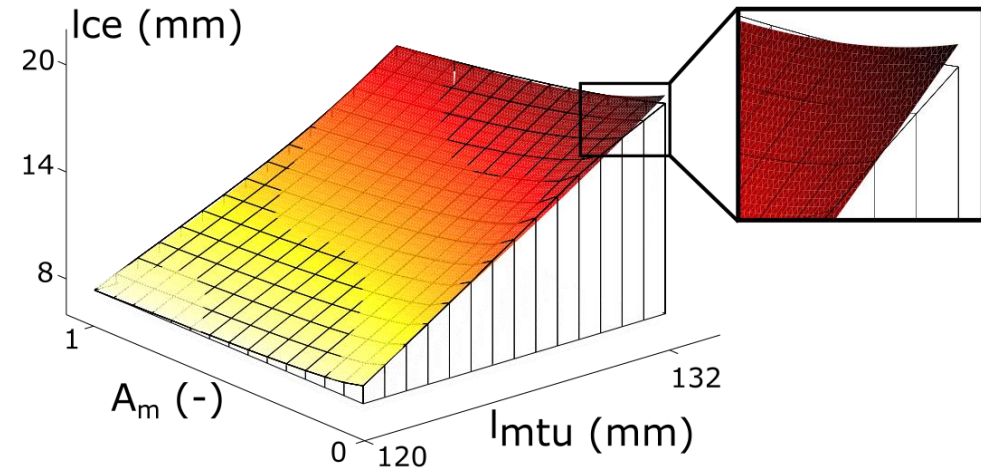
Hill muscle model integration problem



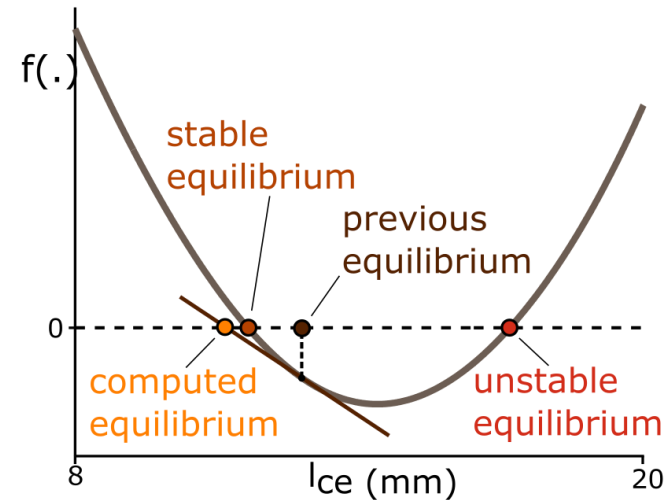
Hill muscles: computing the steady-state values



Look Up Table (LUT)

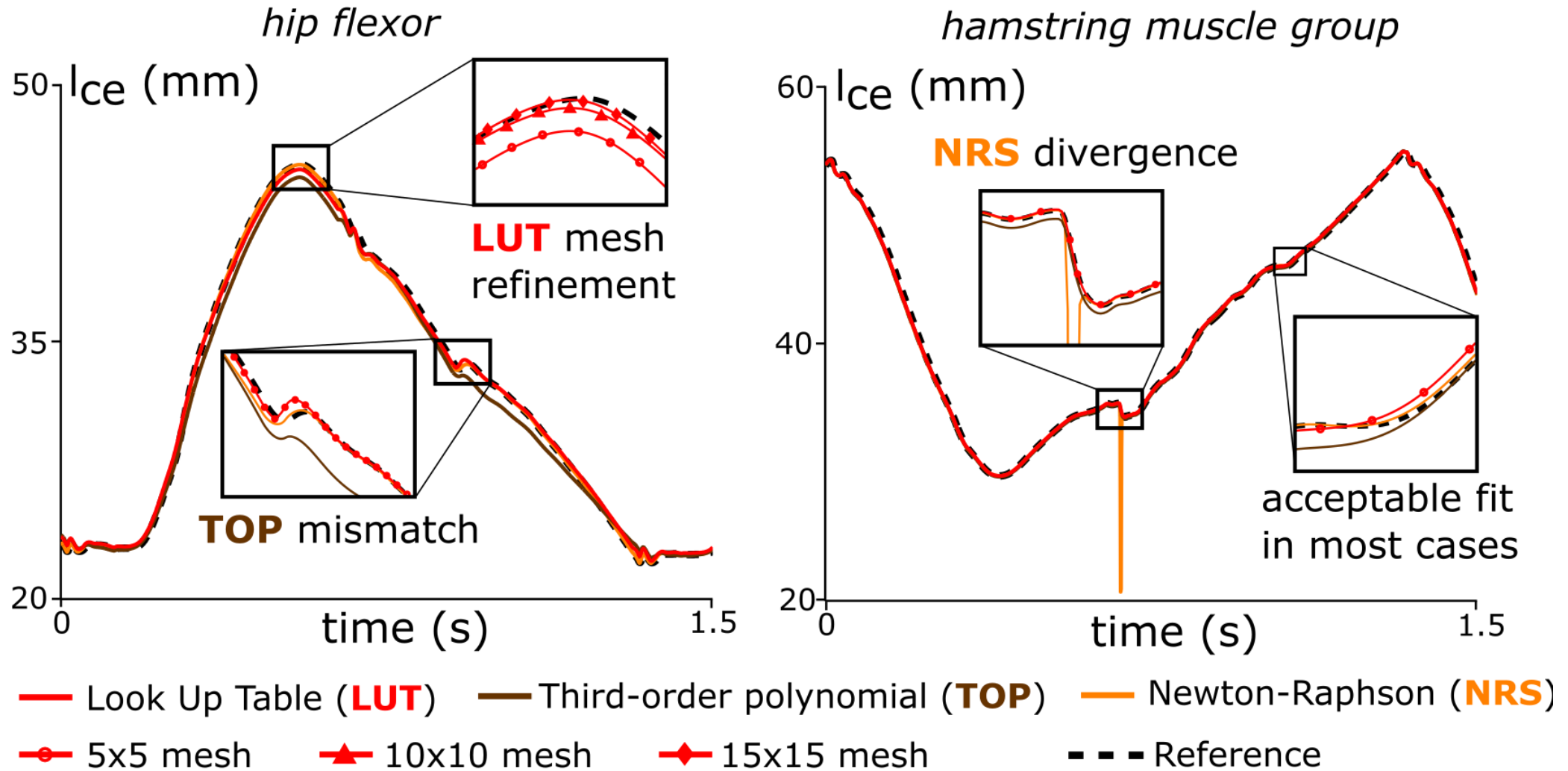


Third-order polynomial (TOP)

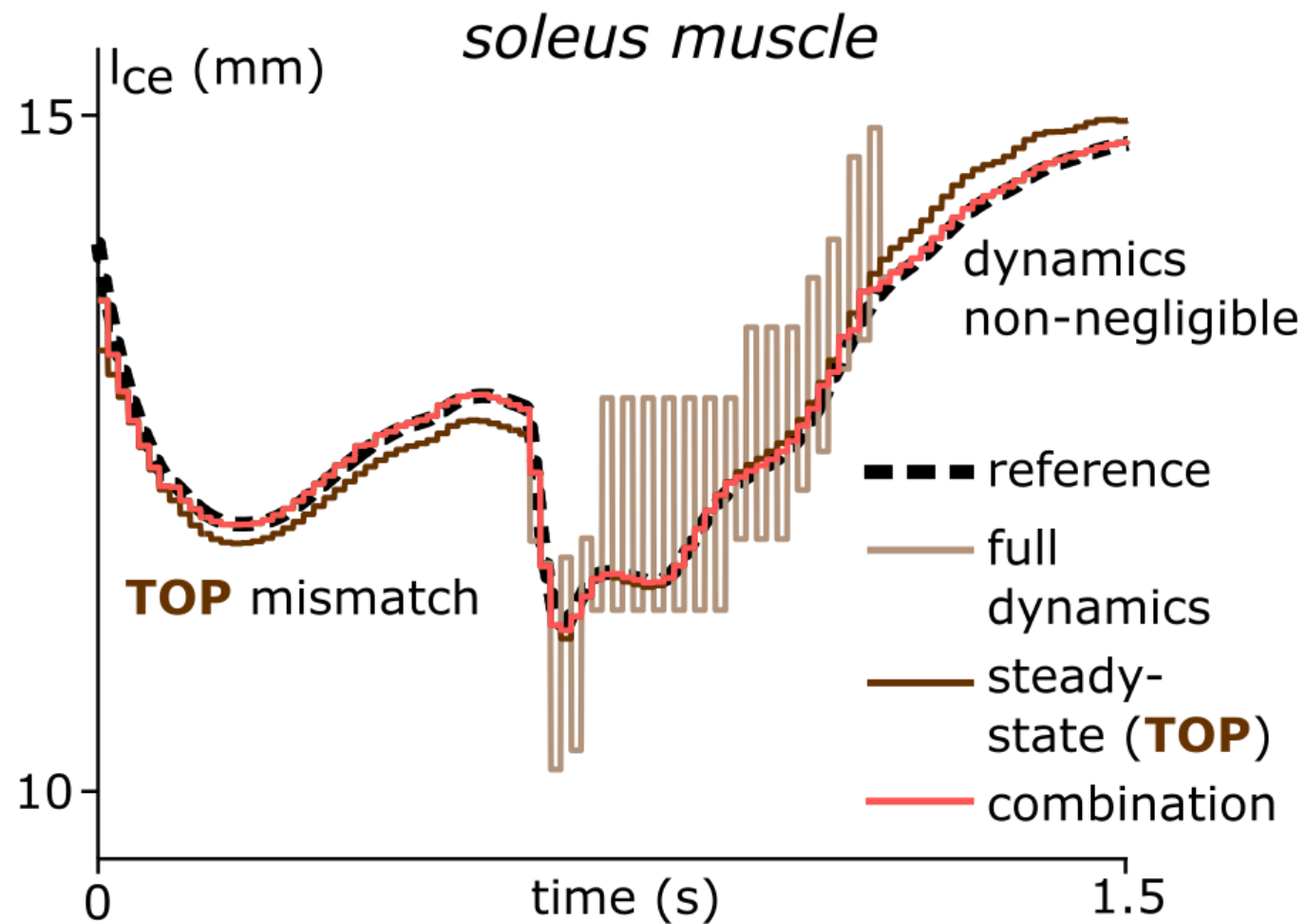


Newton-Raphson scheme (NRS)

Hill muscles: steady-state approximation results

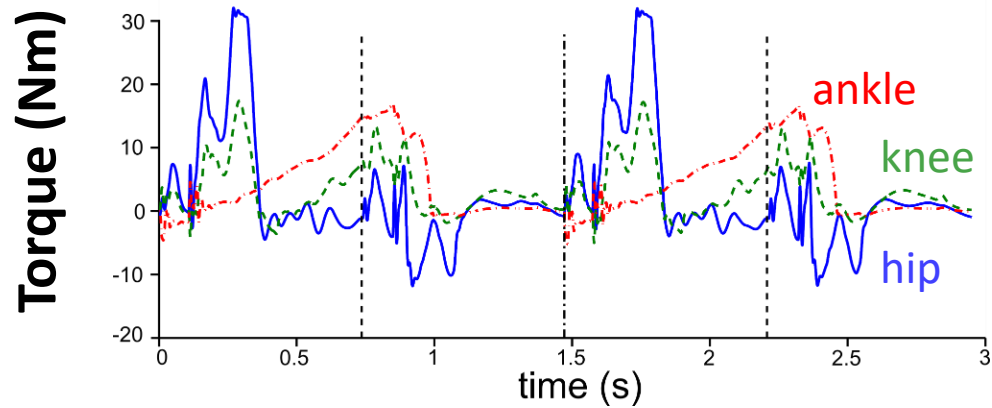
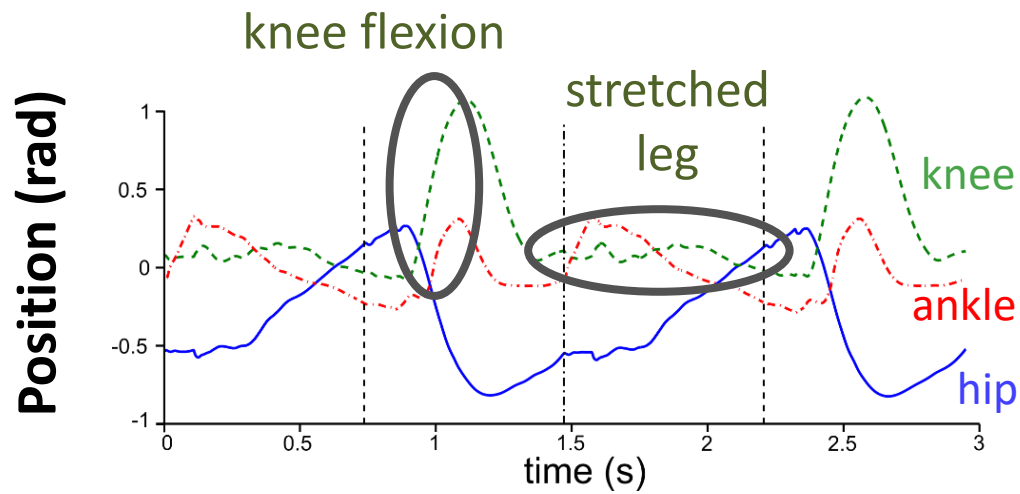


Combining approximations and full dynamics

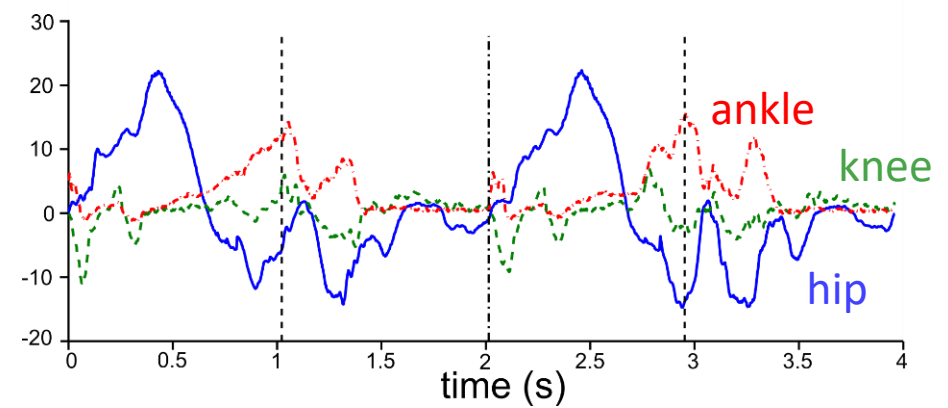
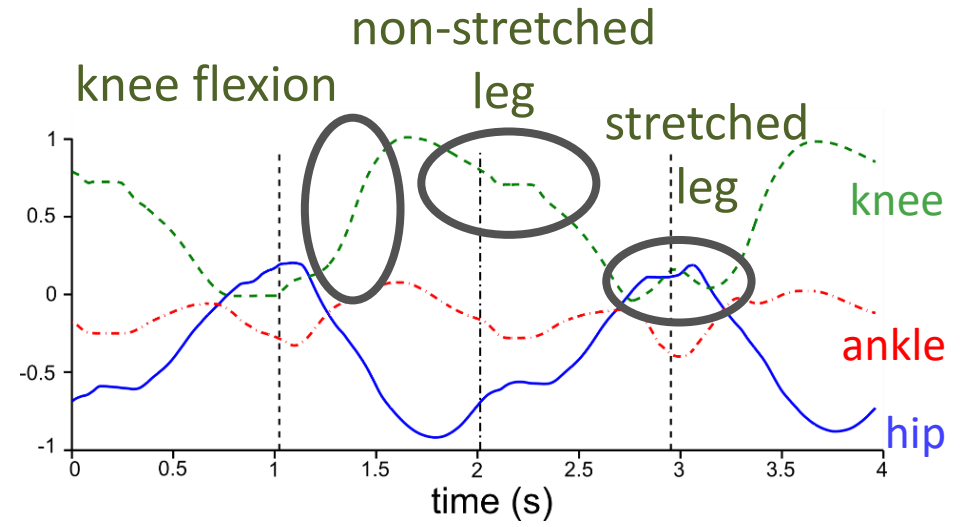


Real experiment: simulation and experimental gaits

Simulation

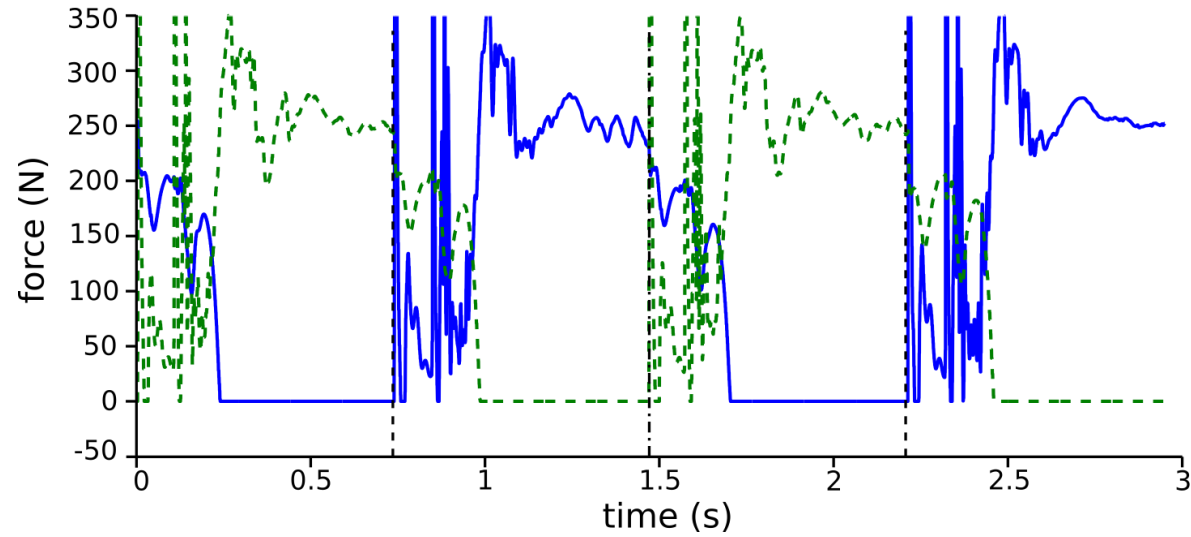


Real robot

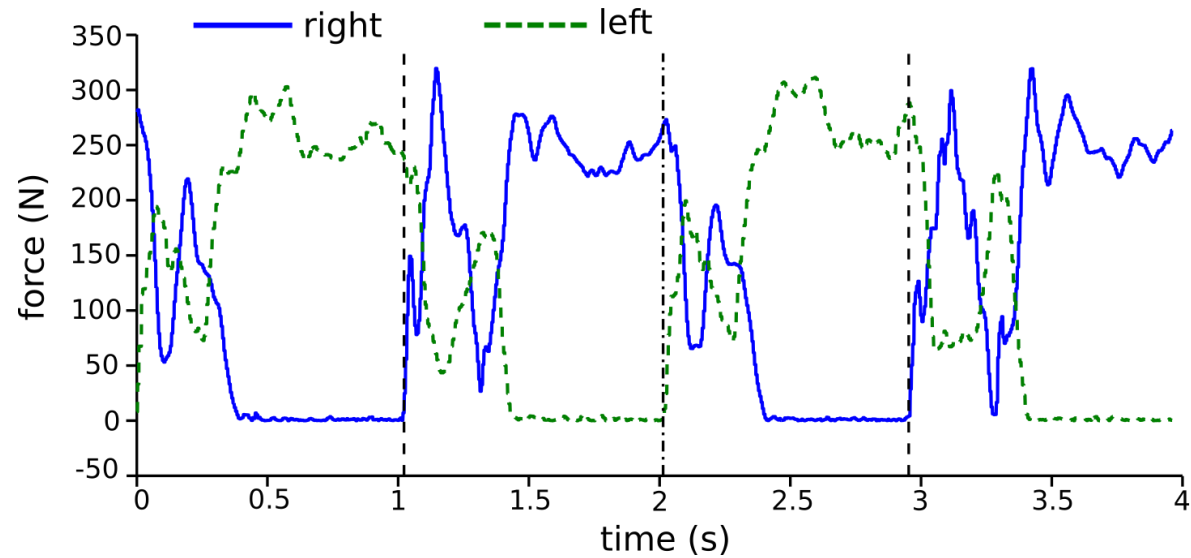


Real experiment: vertical foot forces

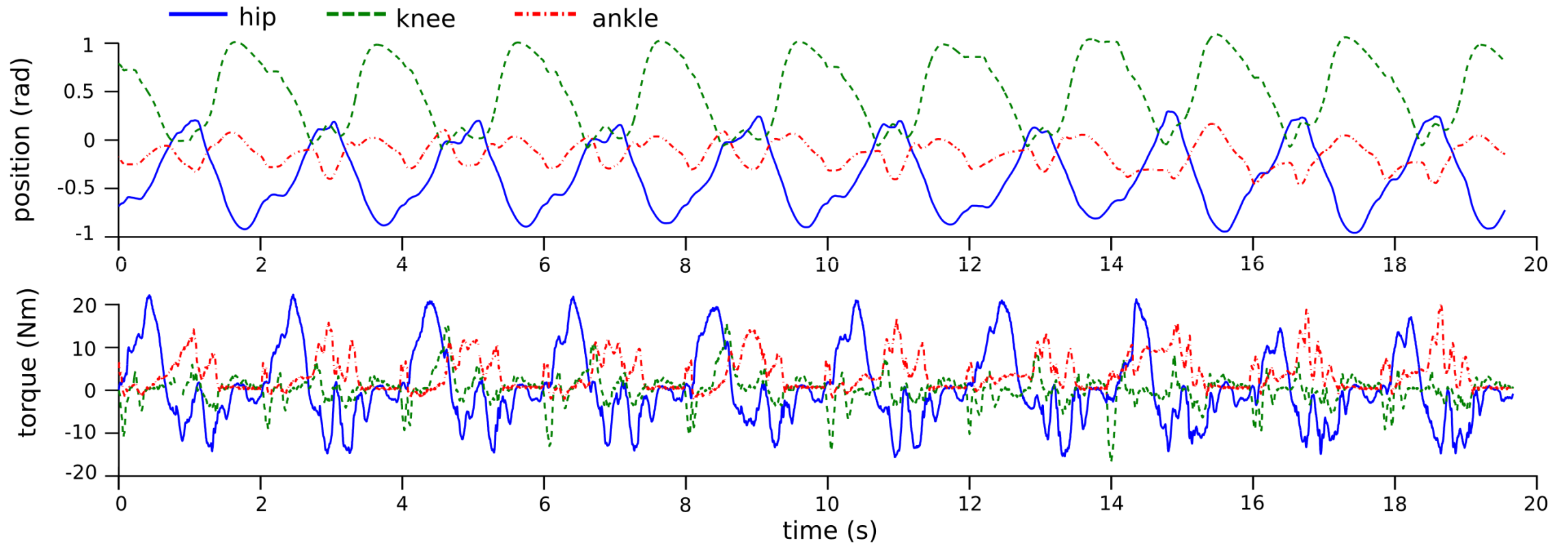
Simulation forces



Real experiment forces



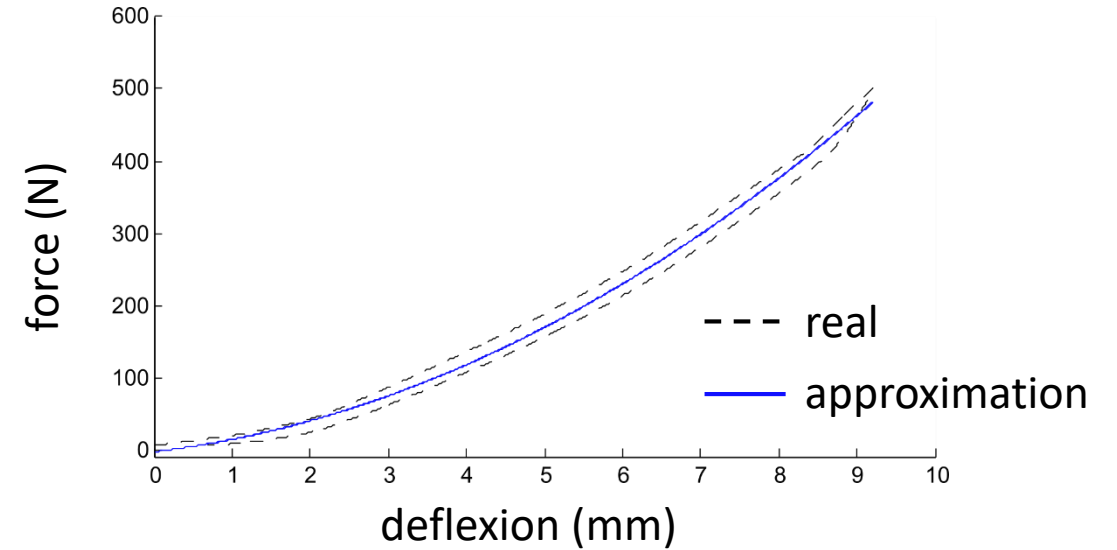
Real experiment: long walk



Feet with human-like compliance



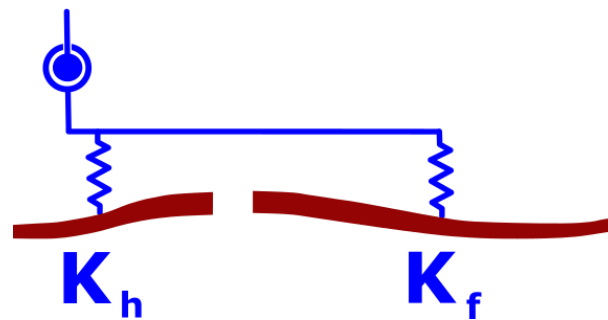
Flex-Foot Junior prosthesis



Force-displacement characteristic



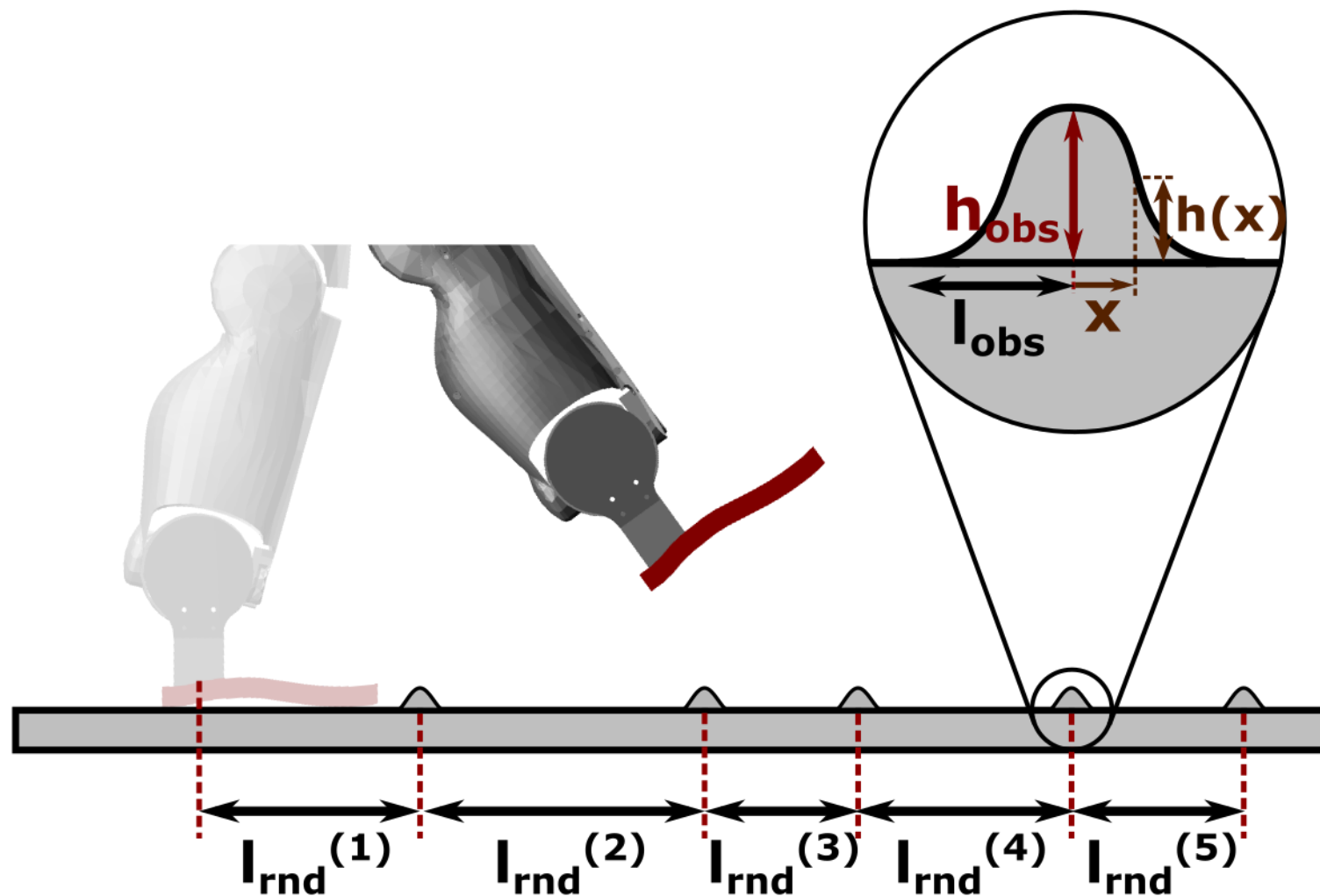
Luca Colasanto



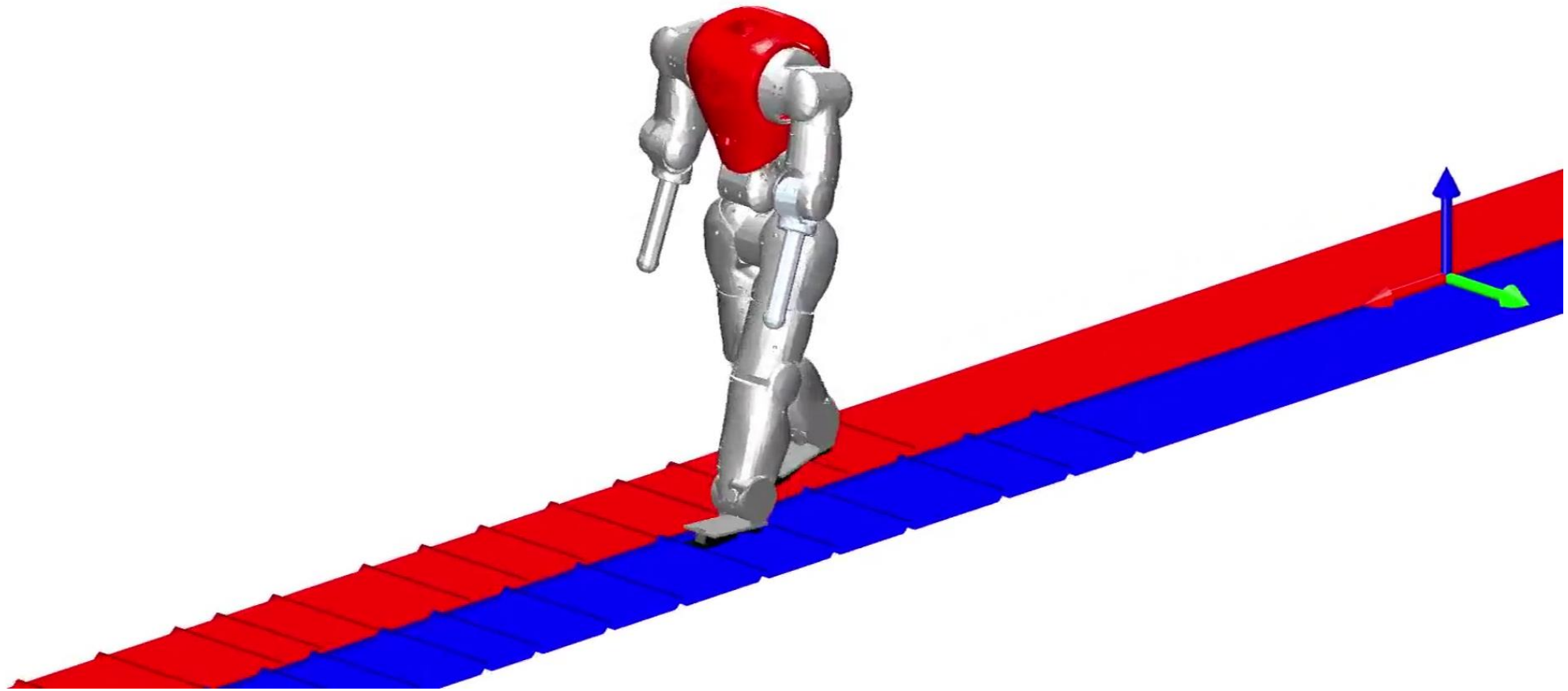
Compliant foot design



Feet comparisons: ground bumps description

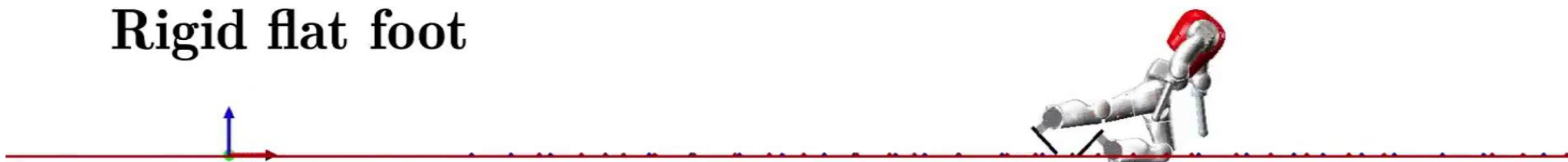


Compliant feet on uneven terrains



Feet comparisons on uneven terrains

Rigid flat foot



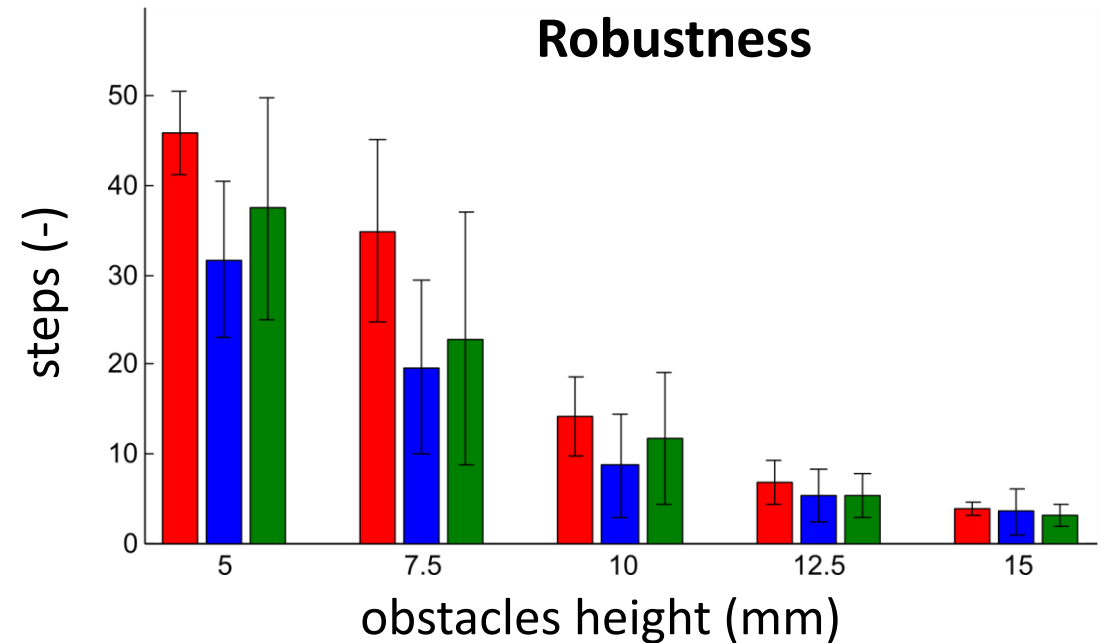
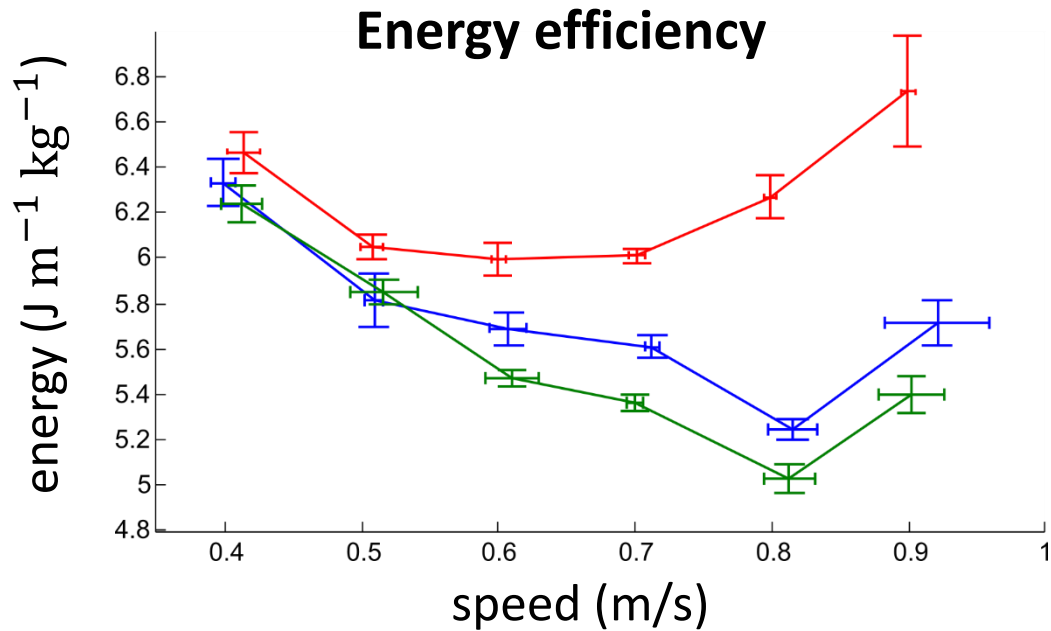
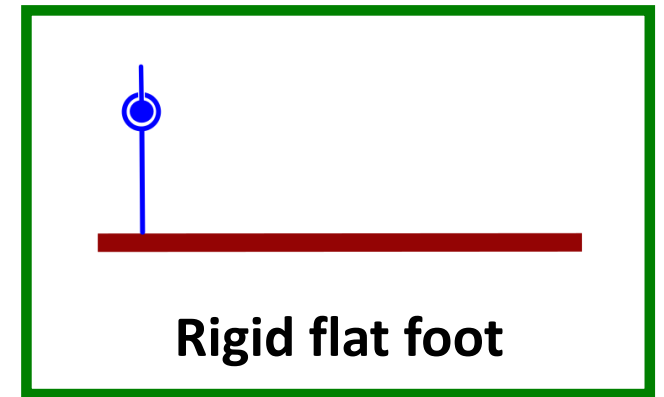
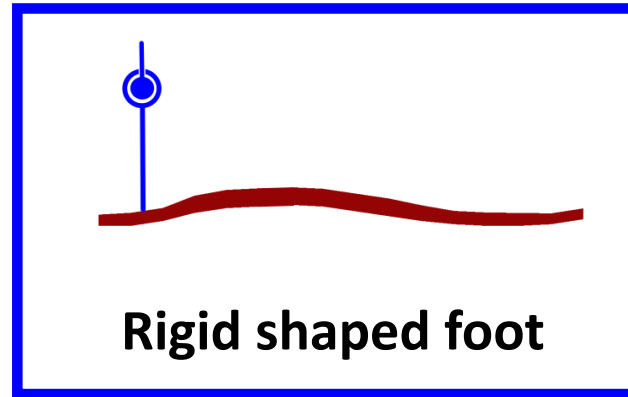
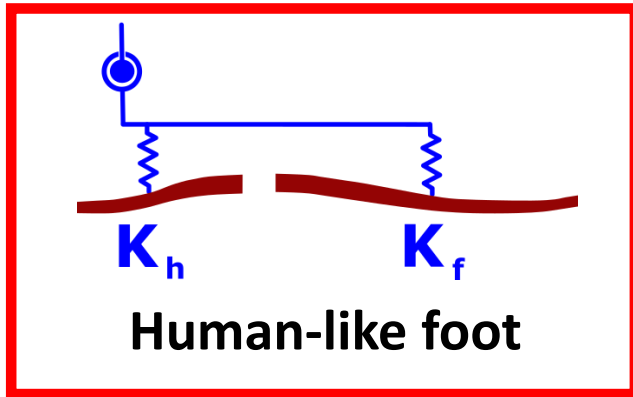
Rigid shaped foot



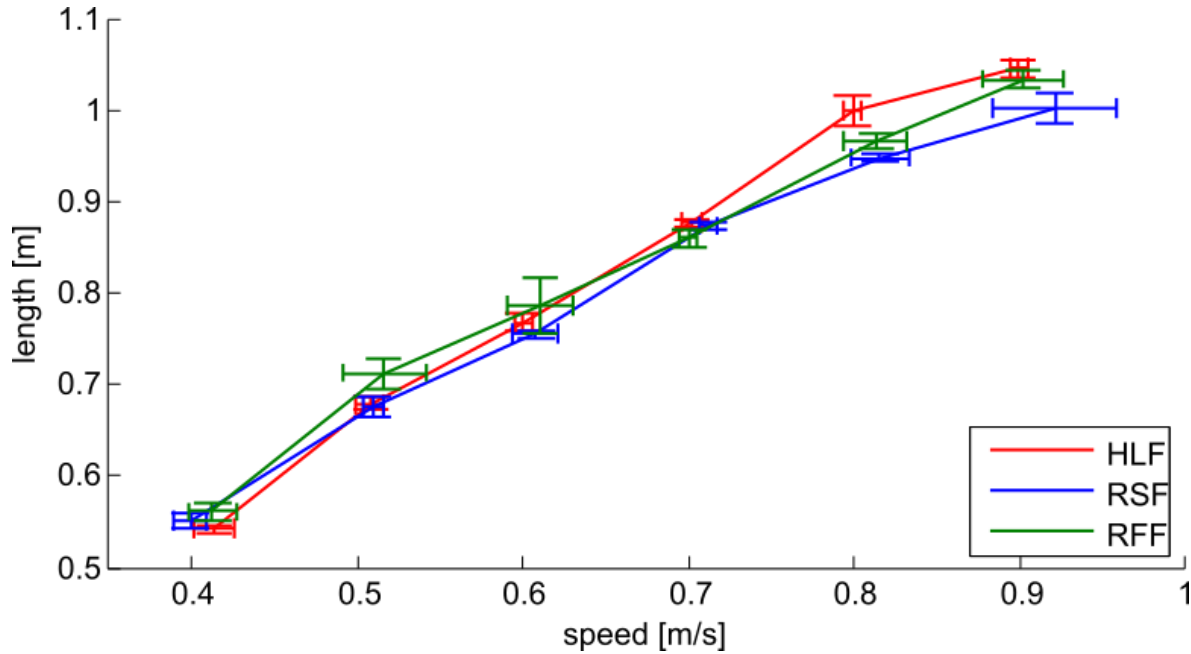
Human-like foot



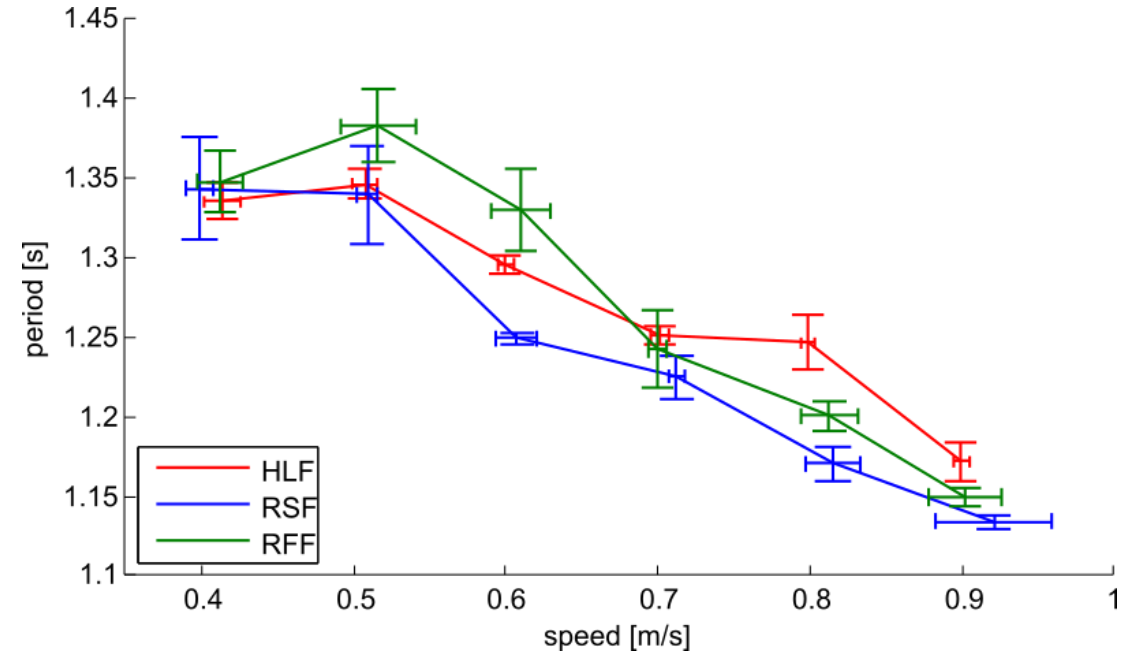
Feet comparisons: energy and robustness



Feet comparisons: stride length and period

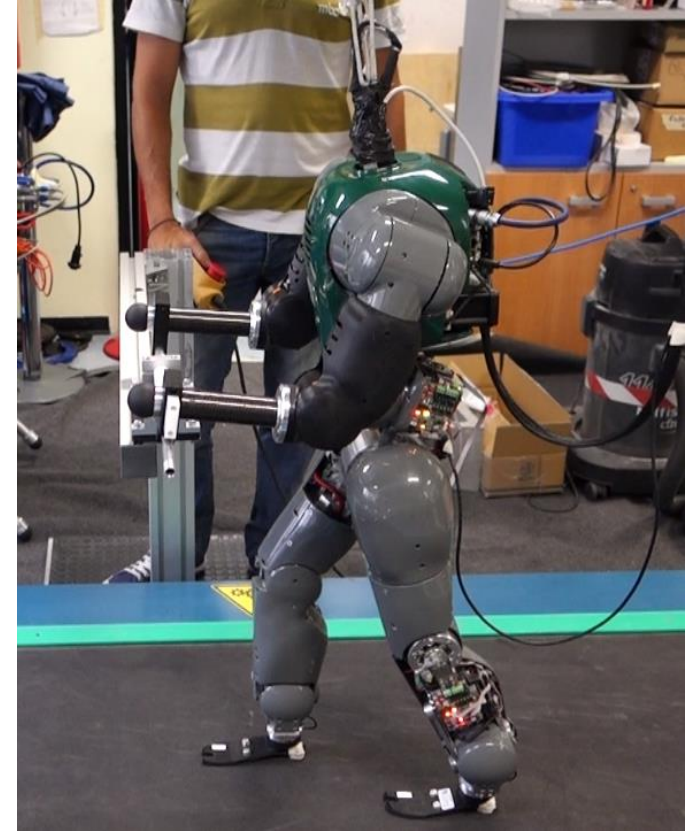
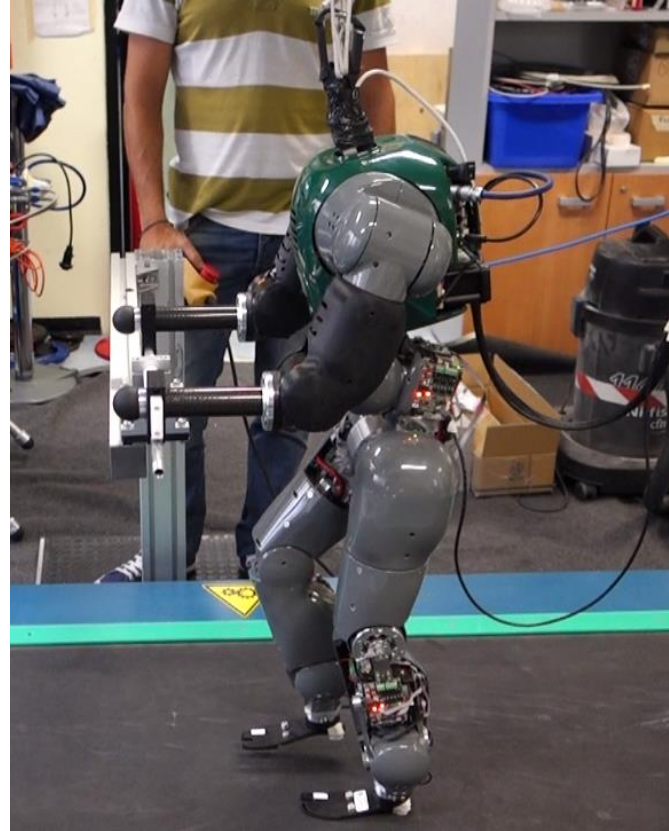
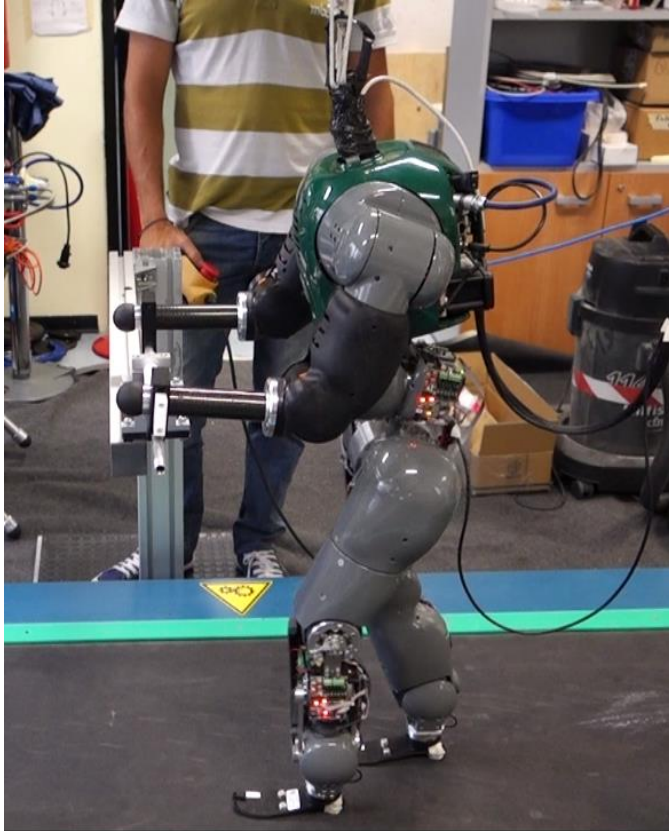


Stride length

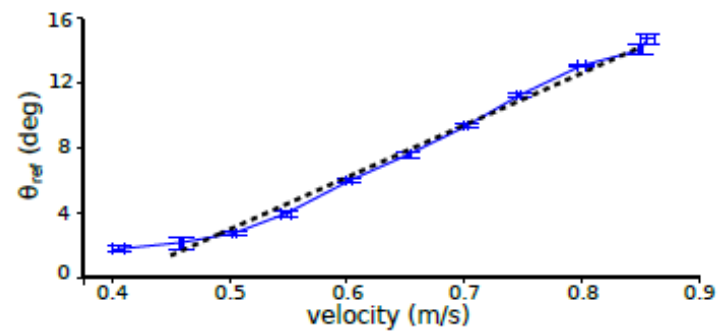


Stride period

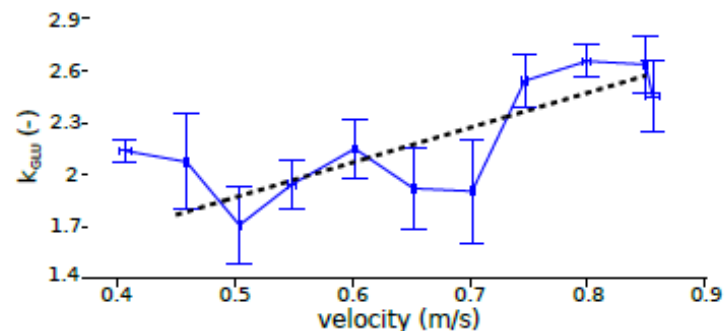
Real experiment: flexible feet



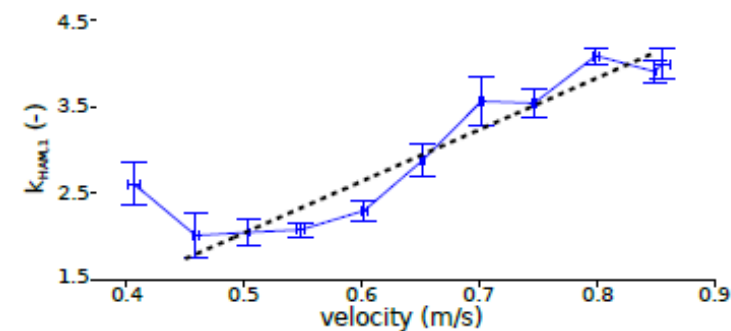
2D walking: speed parameters



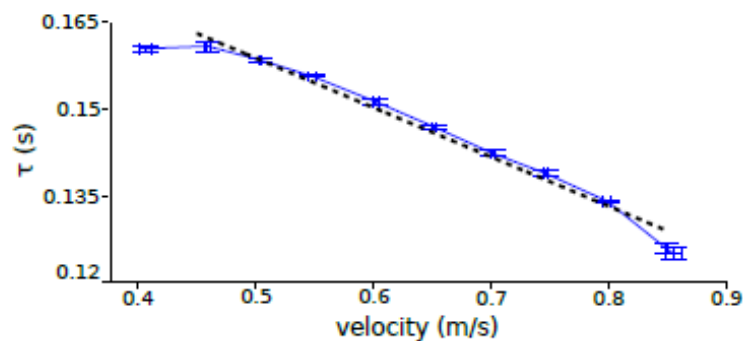
(a) Trunk reference angle θ_{ref}



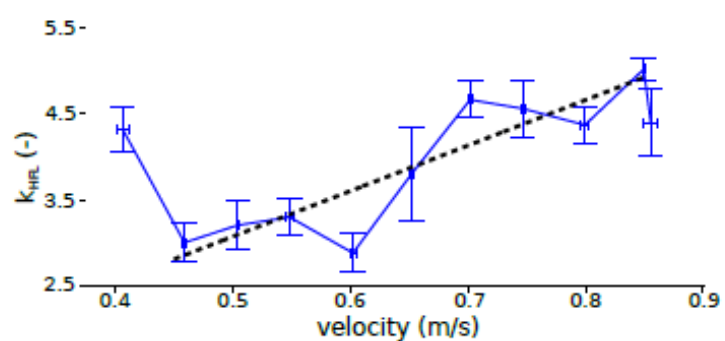
(b) Stimulation gain k_{GLU}



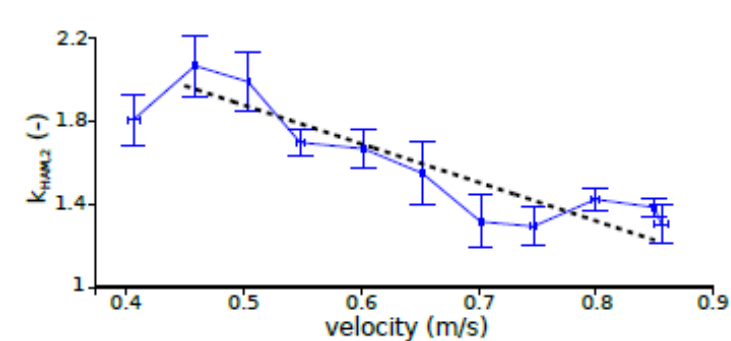
(c) Stimulation gain $k_{HAM,1}$



(d) Oscillator time constant τ



(e) Stimulation gain k_{HFL}

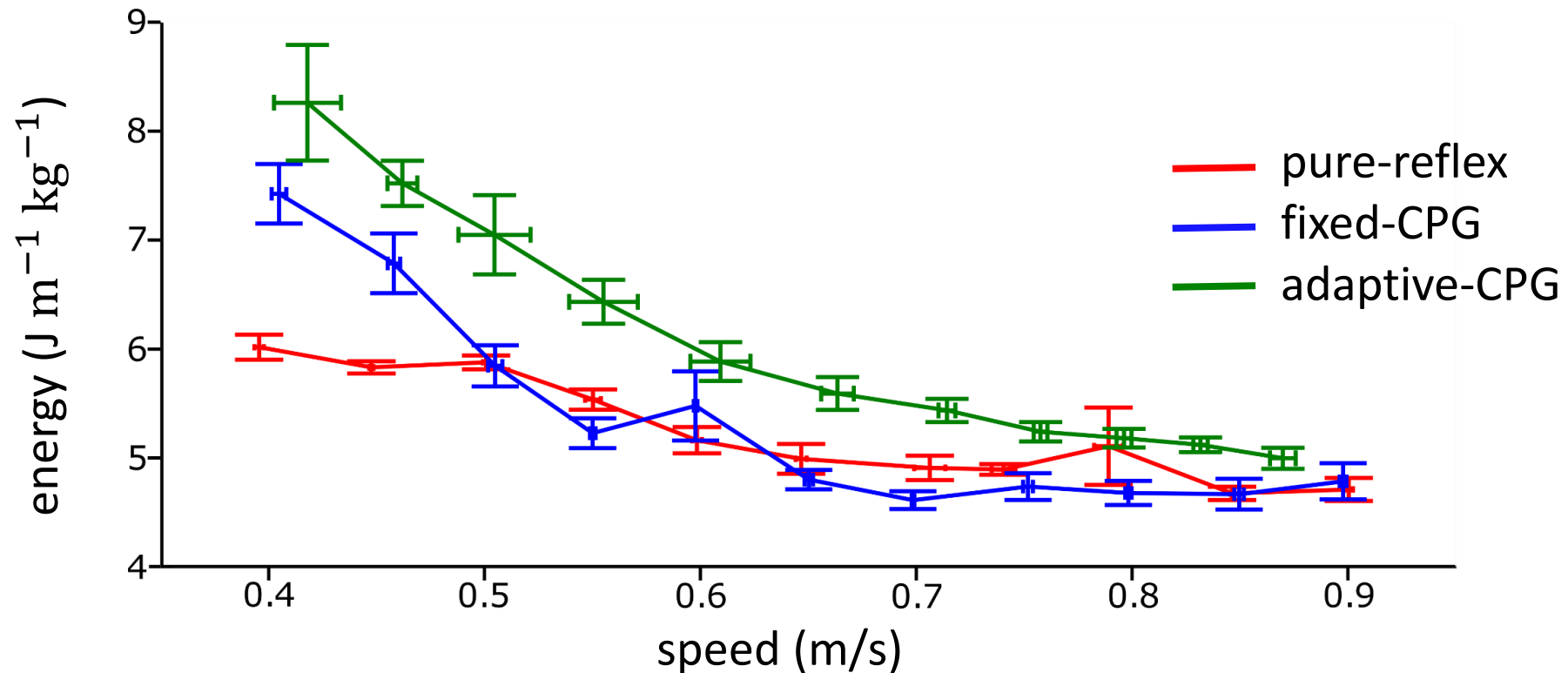


(f) Stimulation gain $k_{HAM,2}$

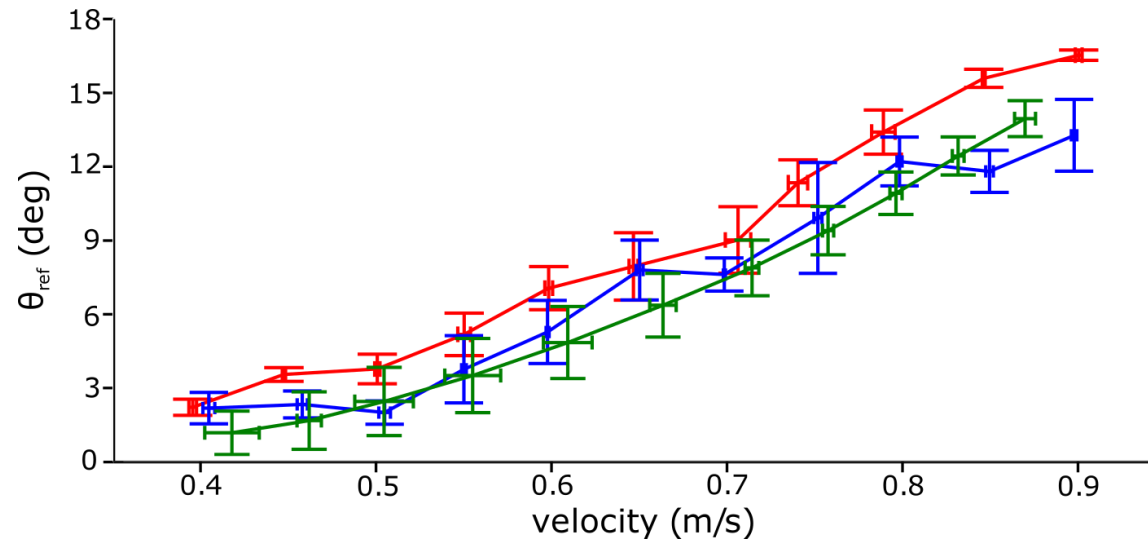
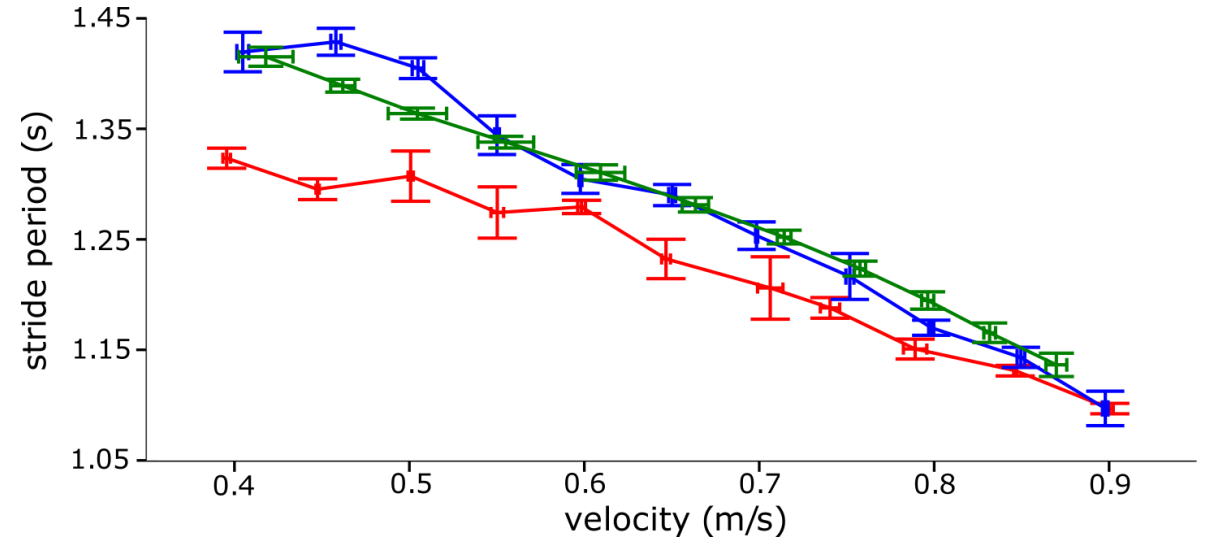
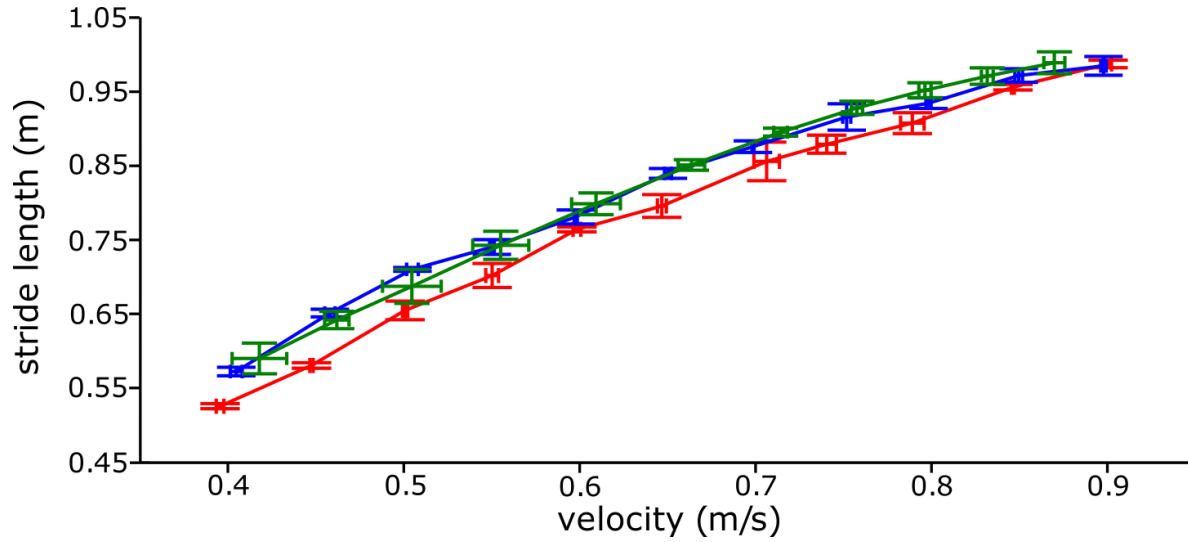
2D walking: metabolic energy consumption

Small increase in **energy consumption** for the adaptive-CPG controller.

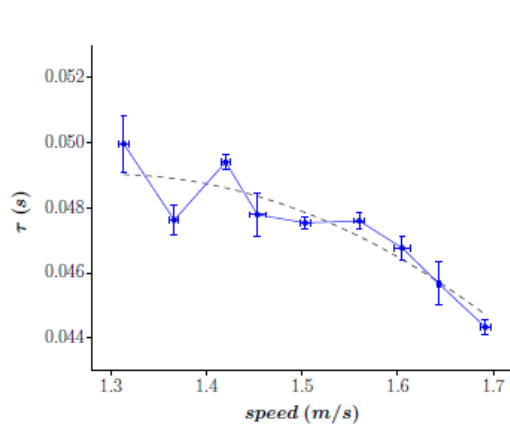
Reasonable price to pay for the resulting **versatility**.



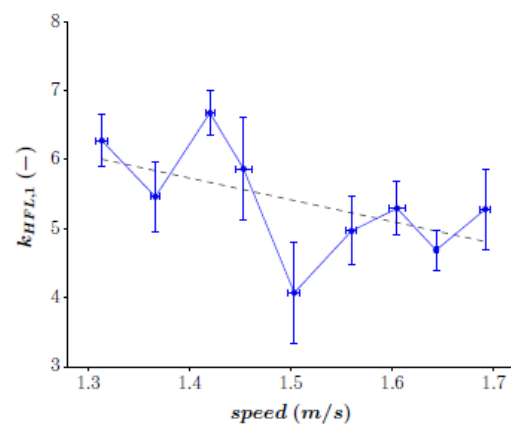
2D walking: characteristics



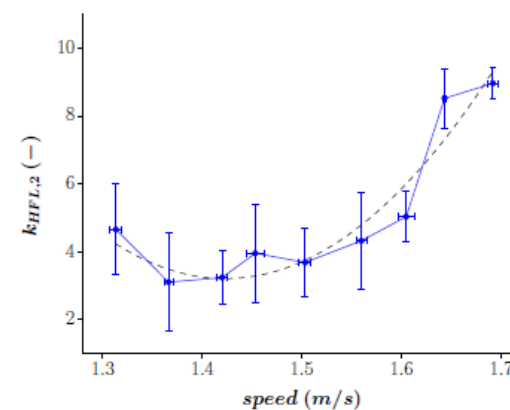
2D running: speed parameters (I)



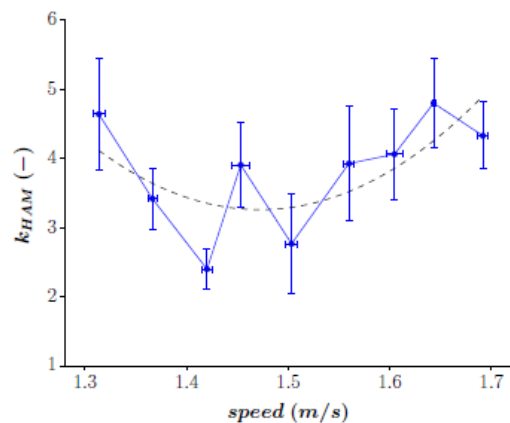
(a) CPG time constant τ



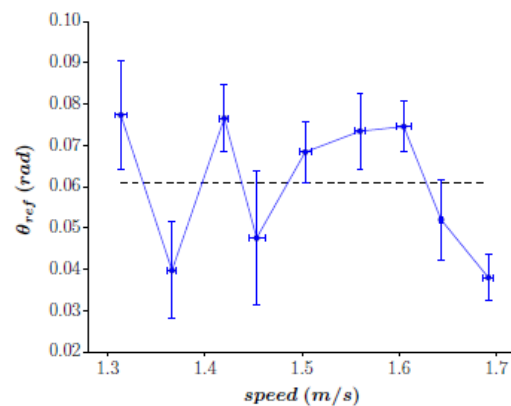
(b) CPG gain $k_{HFL,1}$



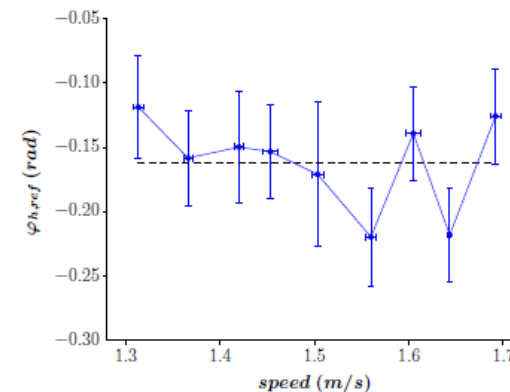
(c) CPG gain $k_{HFL,2}$



(d) CPG gain k_{HAM}

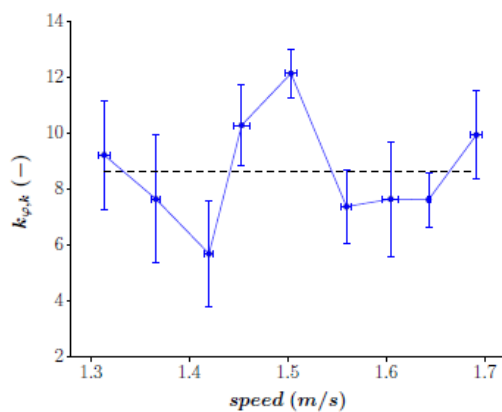


(e) Torso orientation reference θ_{ref}

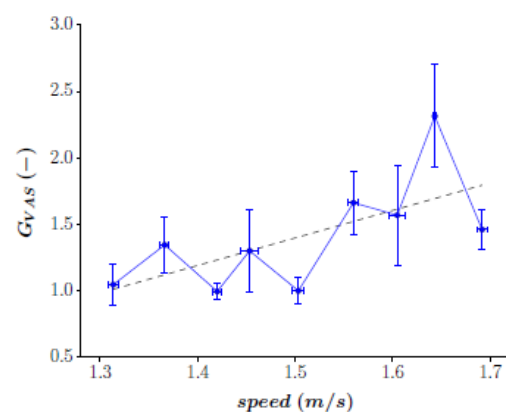


(f) Hip angle reference $\varphi_{h,ref}$

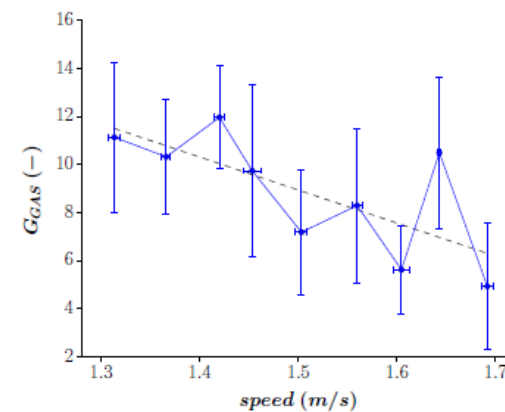
2D running: speed parameters (II)



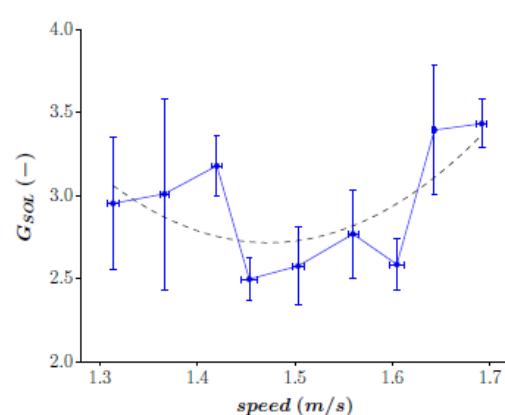
(g) Knee angle gain $k_{\varphi,k}$



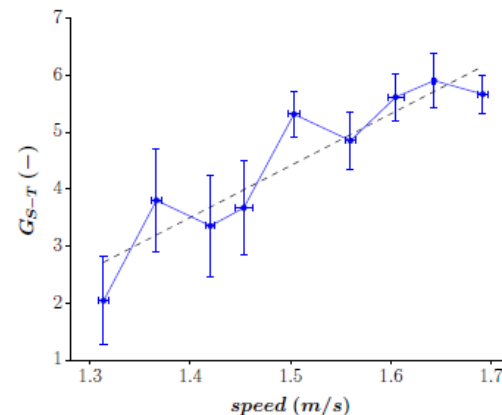
(h) reflex gain G_{VAS}



(i) reflex gain G_{GAS}

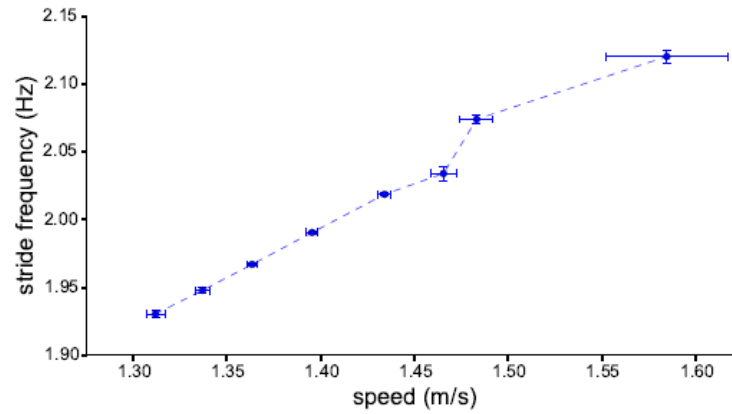


(j) reflex gain G_{SOL}

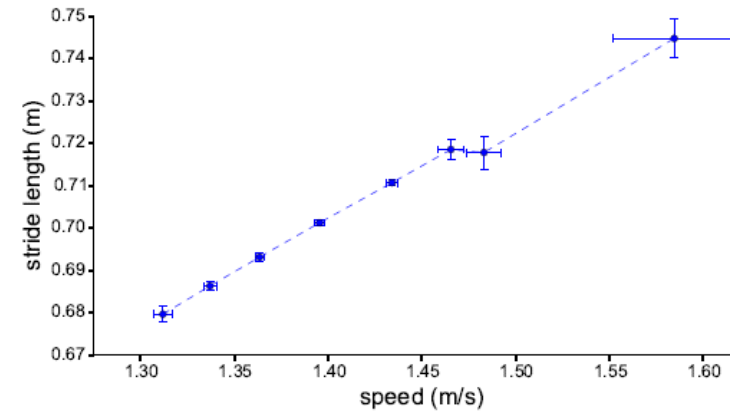


(k) reflex gain G_{S-T}

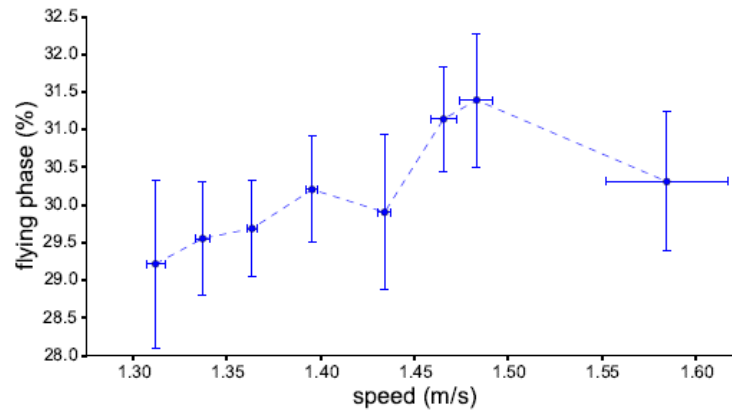
2D running: characteristics



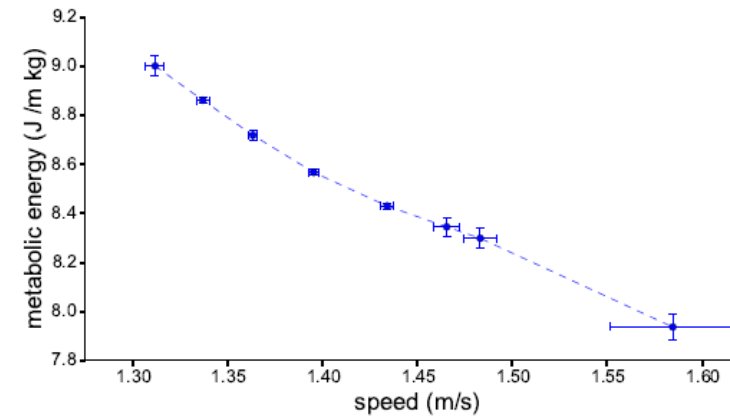
(a) stride frequency



(b) stride length

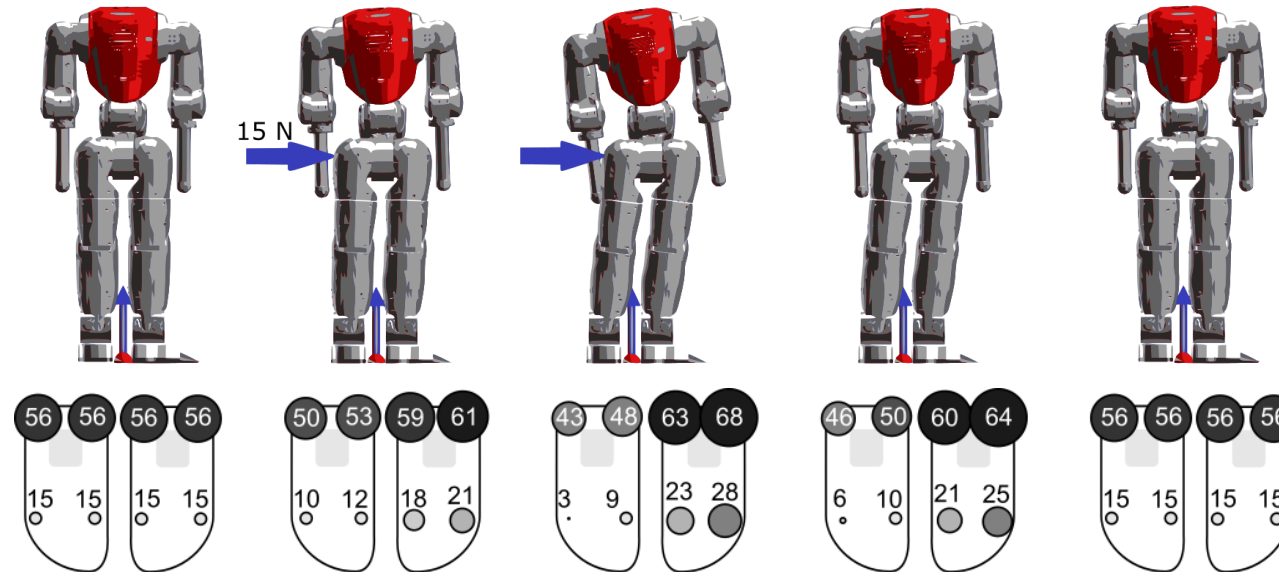
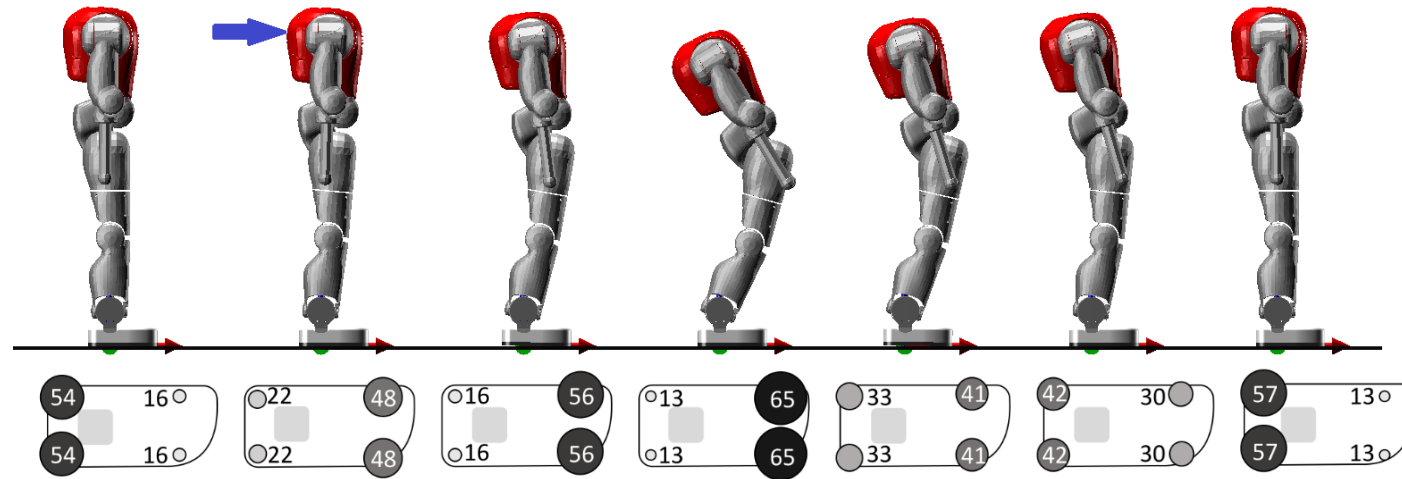


(c) flying phase ratio

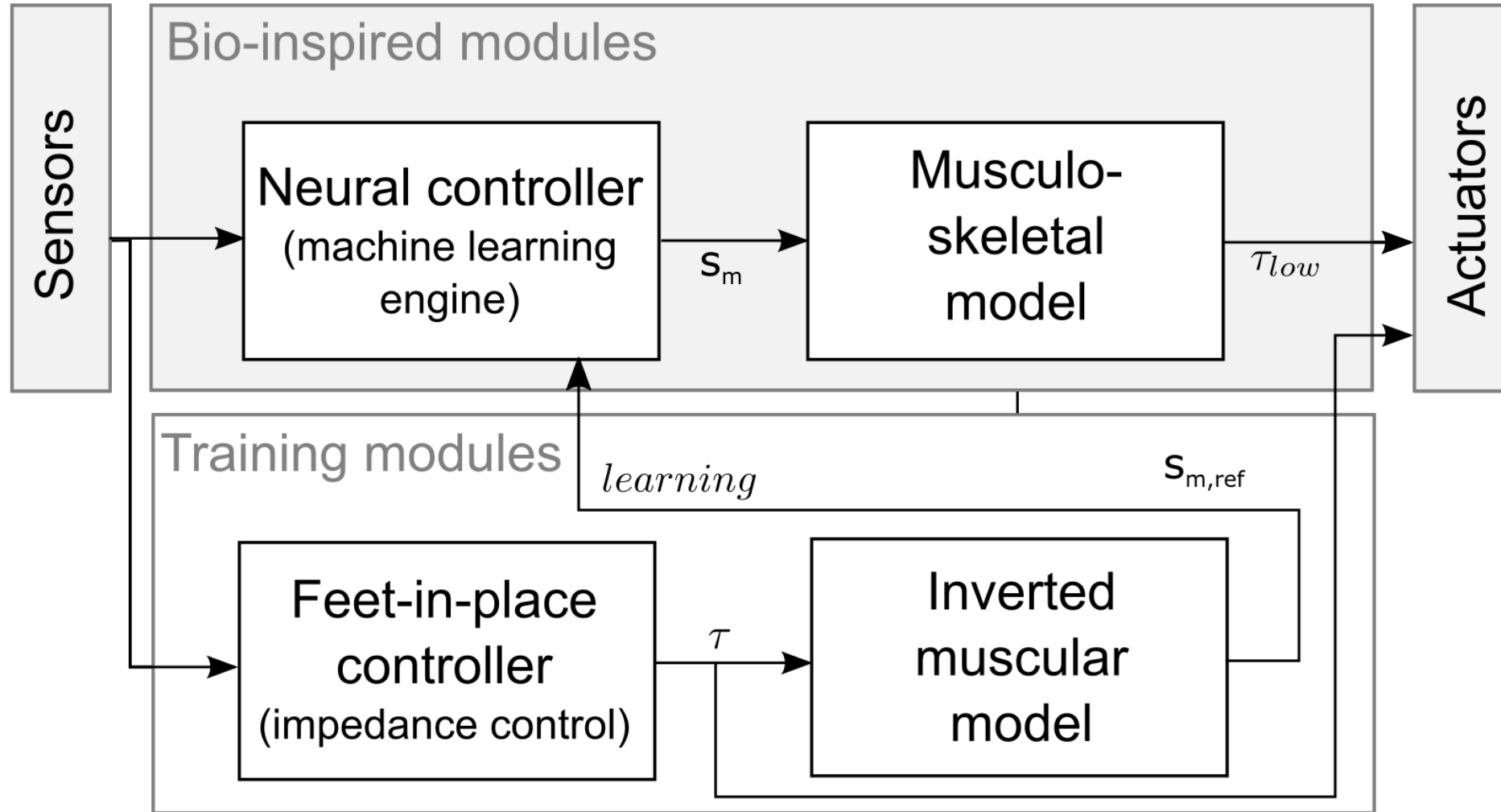


(d) metabolic energy consumption

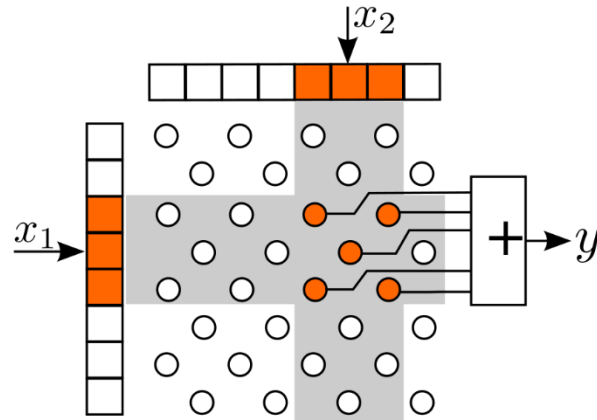
Pushes: foot contact forces



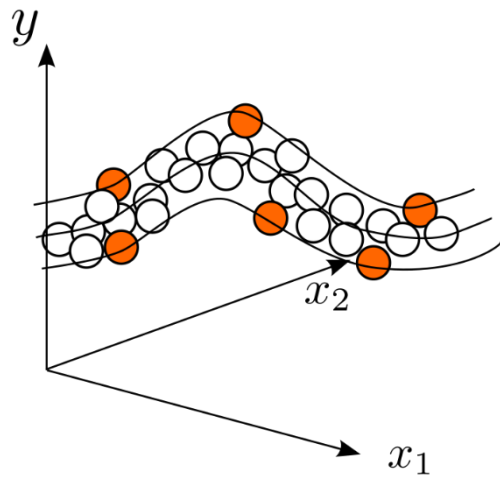
Learning process



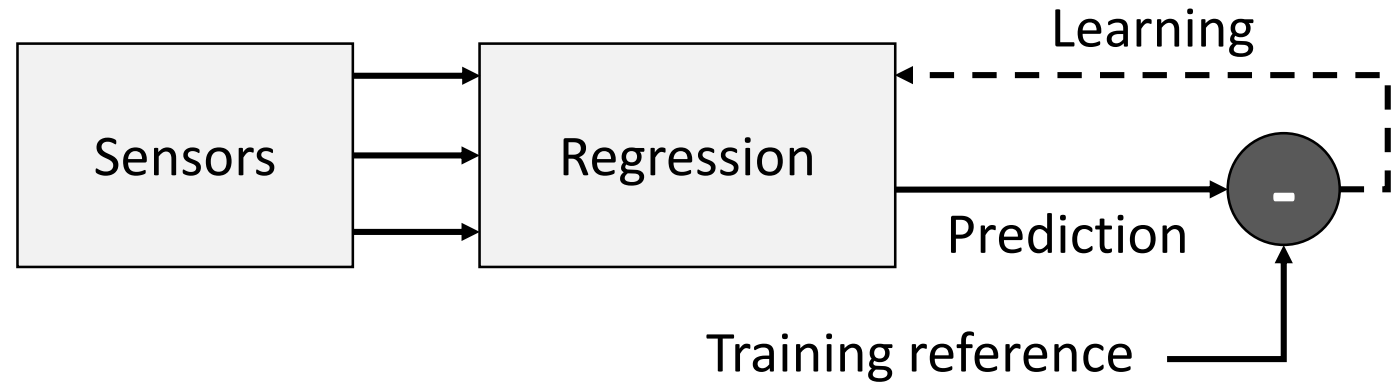
Neural controller: a regression engine



CMAC



SVR



Cerebellum Model for Articulation Control (CMAC)

Based on the cerebellum organization

Neural network

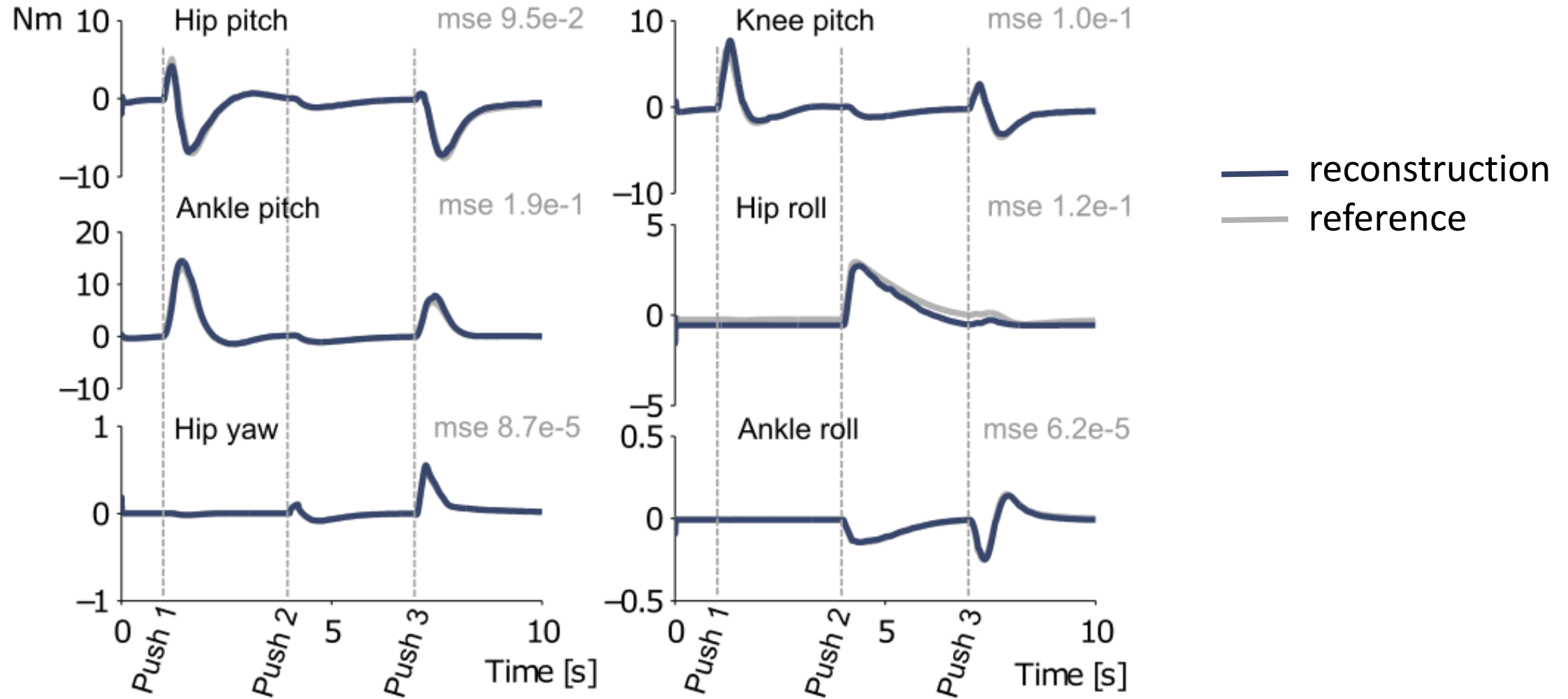
[Smith 1998]

Support Vector Regression (SVR)

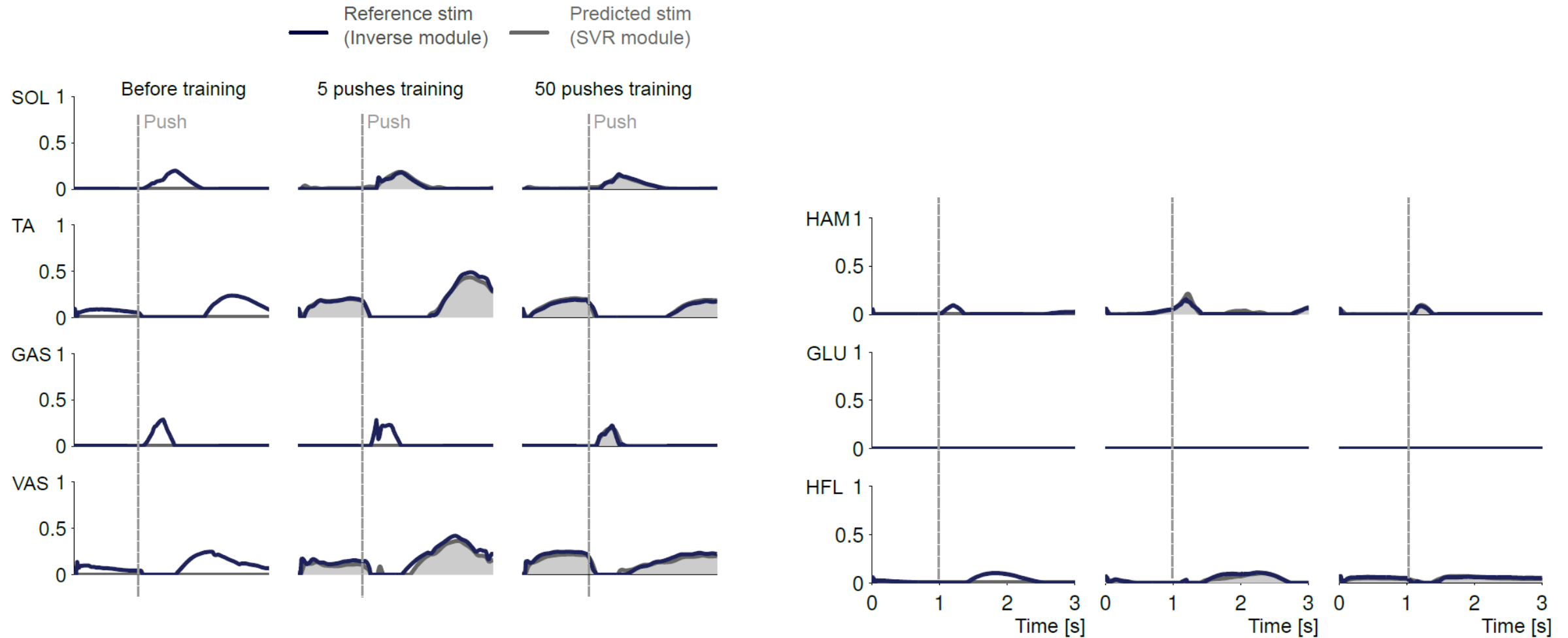
Mathematical model

Data points selected as support vectors

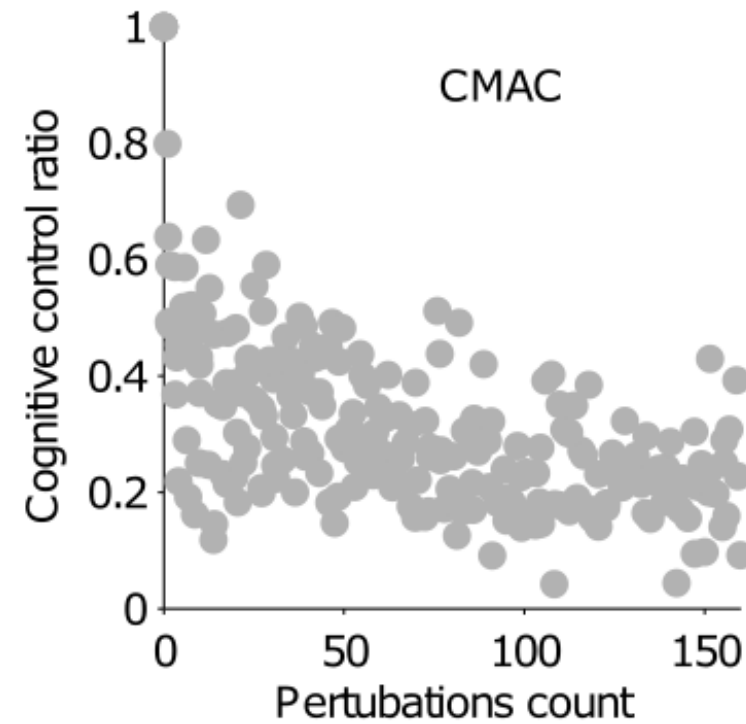
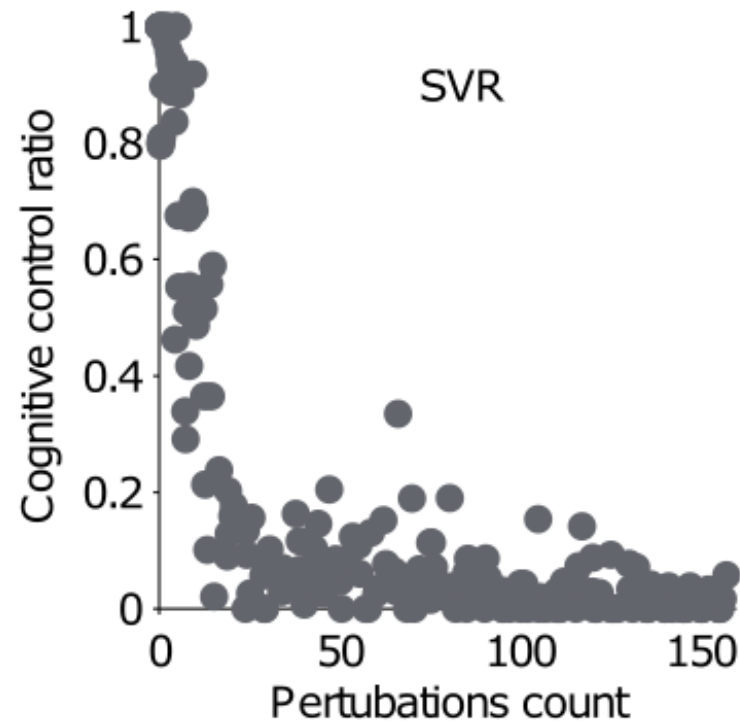
Torques reconstruction



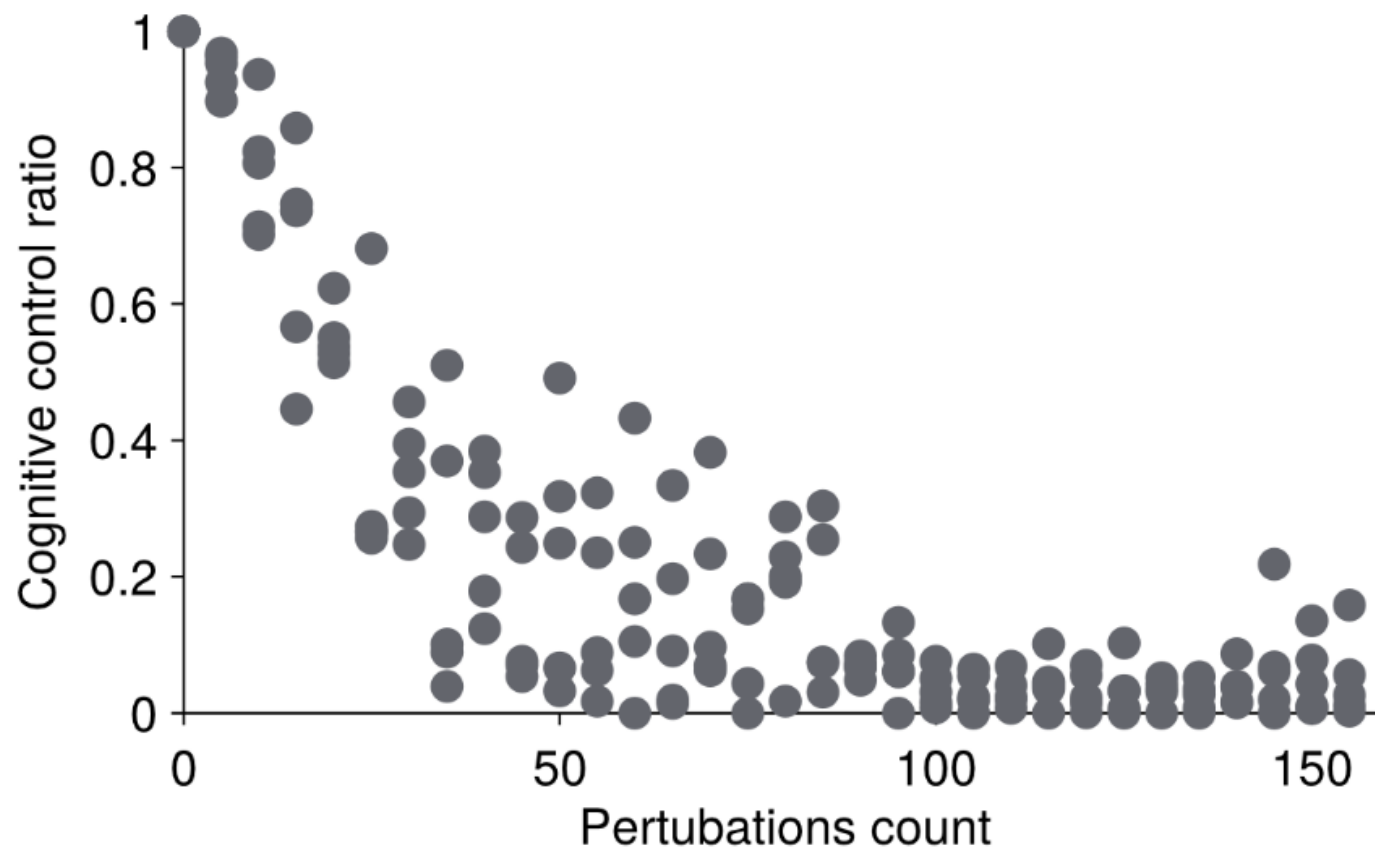
Stimulations reconstruction



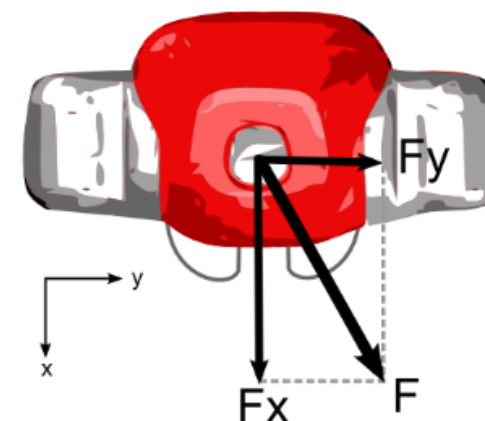
COG ration: sagittal plane



COG ration: transverse plane



Horizontal perturbation



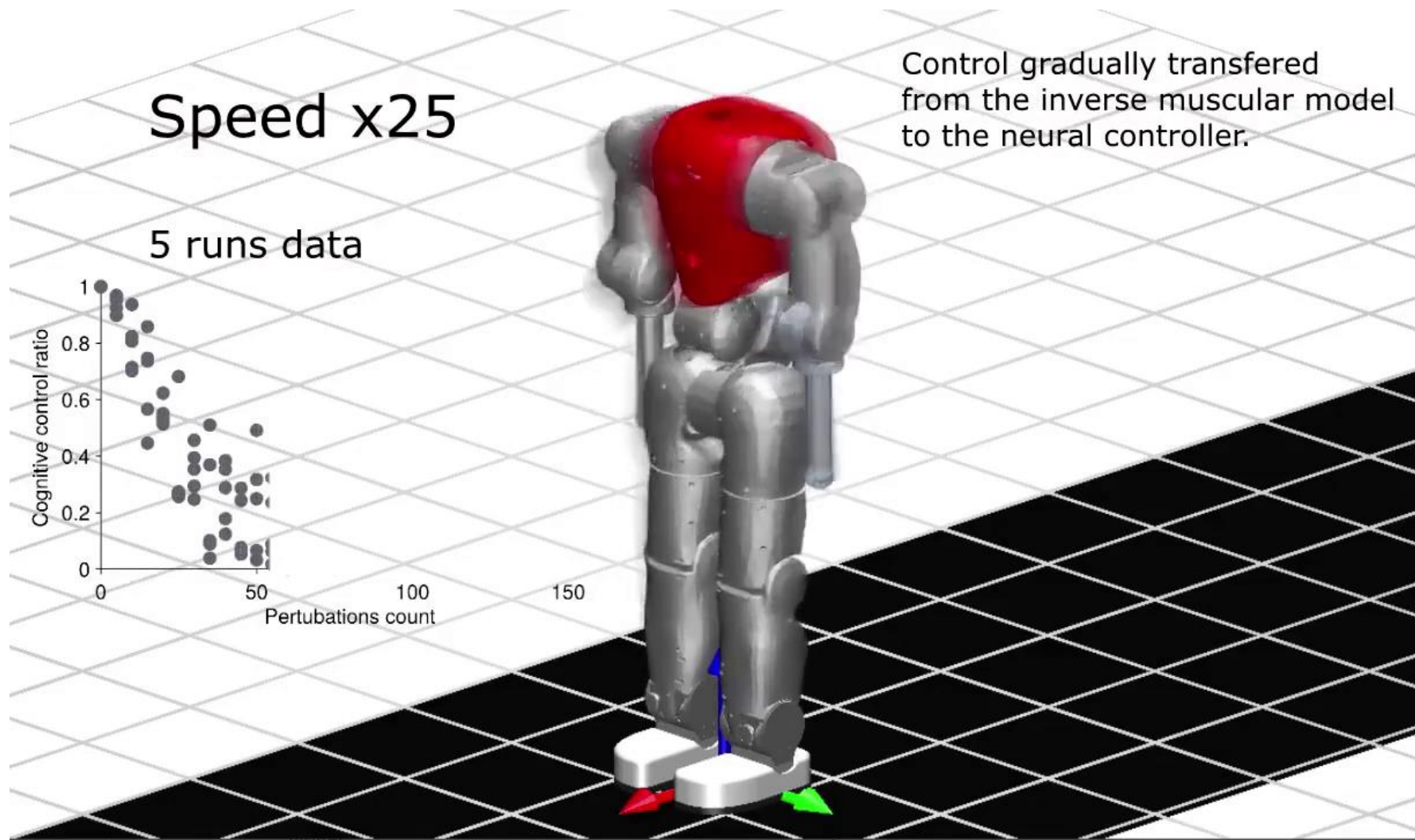
Magnitude

Uniform distribution

F_x in $[-5, 15]$ N

F_y in $[-10, 10]$ N

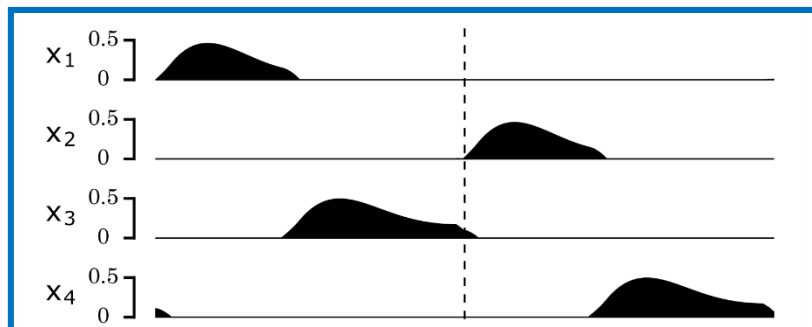
Learning performances



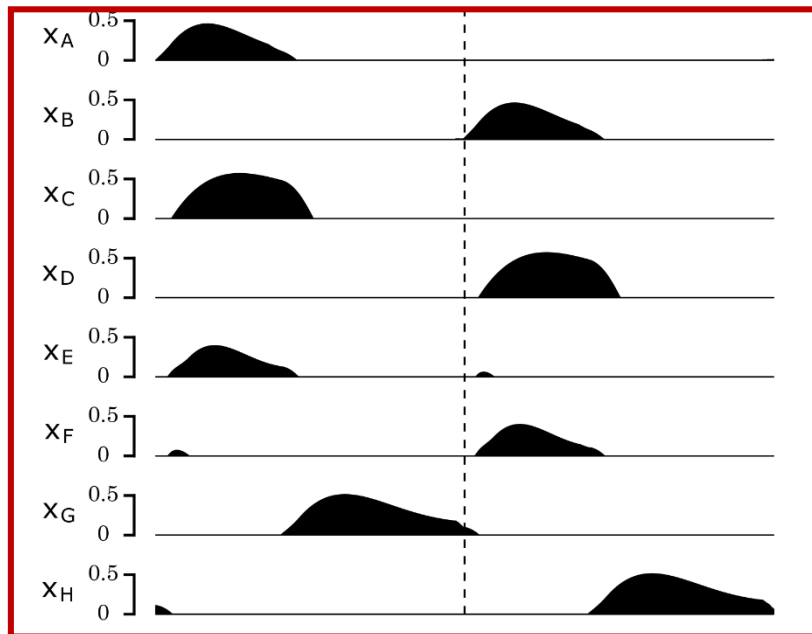
Cognitive control ratio

$$\frac{\text{training time}}{\text{elapsed simulation time}}$$

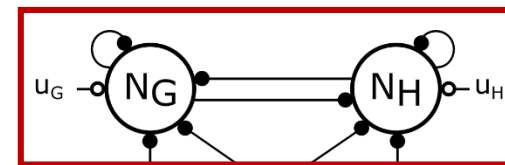
CPG structure for straight walking



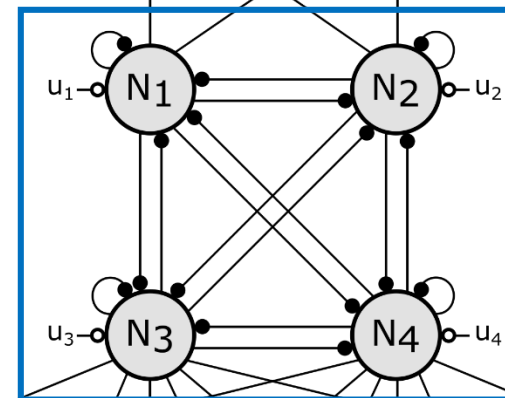
RG



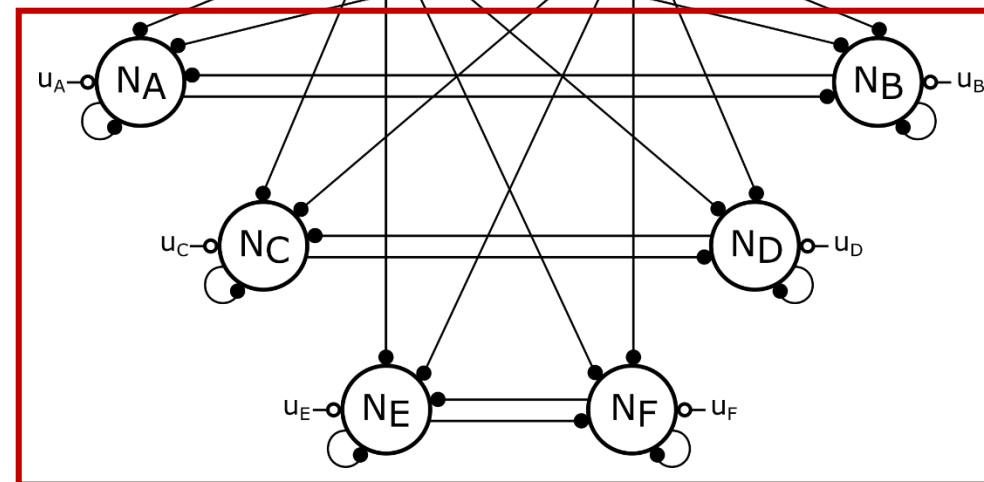
PF



PF

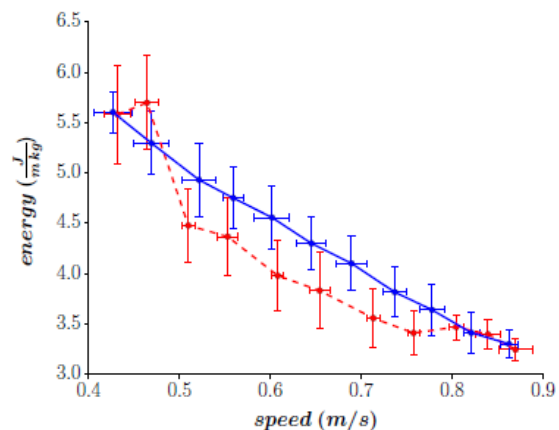


RG

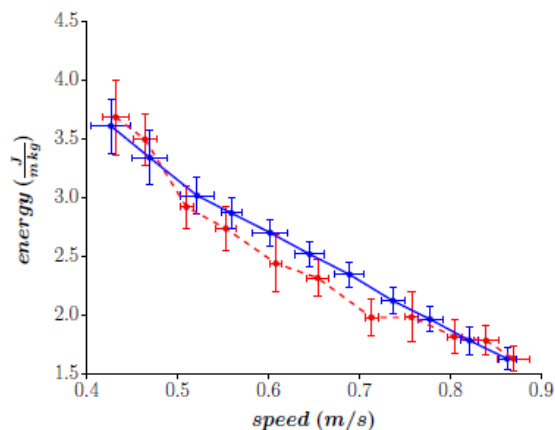


PF

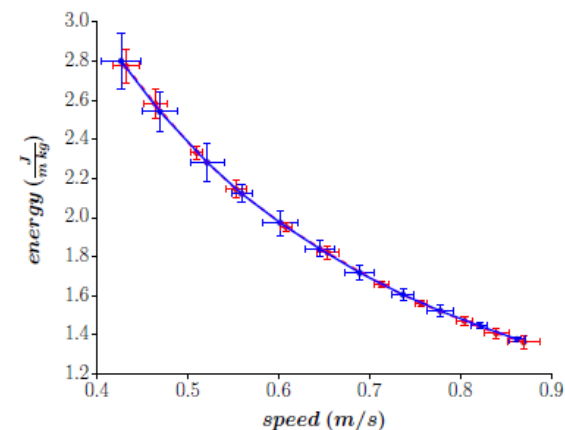
3D straight walking: characteristics



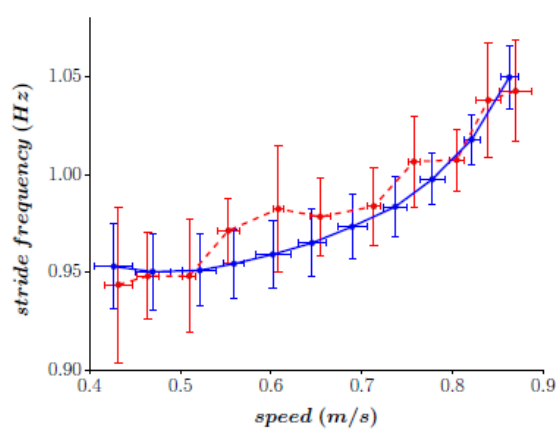
(a) energy sagittal muscles



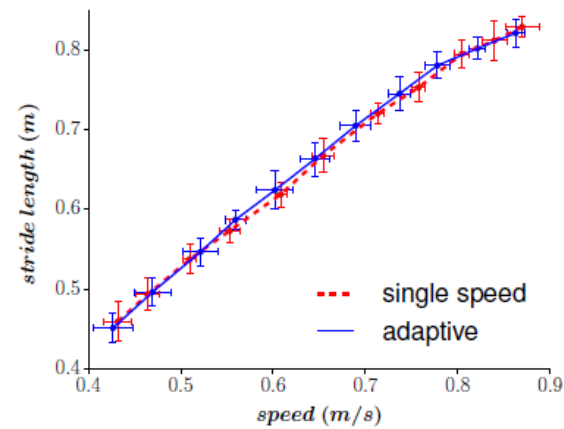
(b) energy lateral muscles



(c) energy transverse muscles

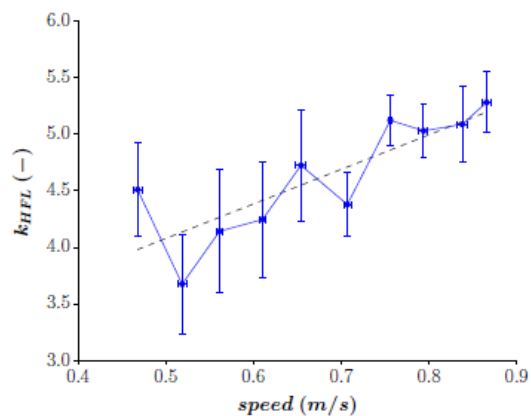


(d) stride frequency

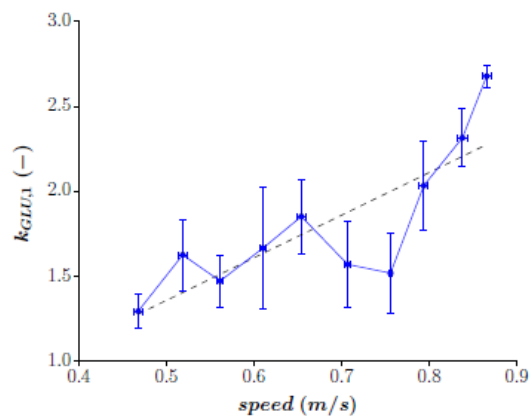


(e) stride length

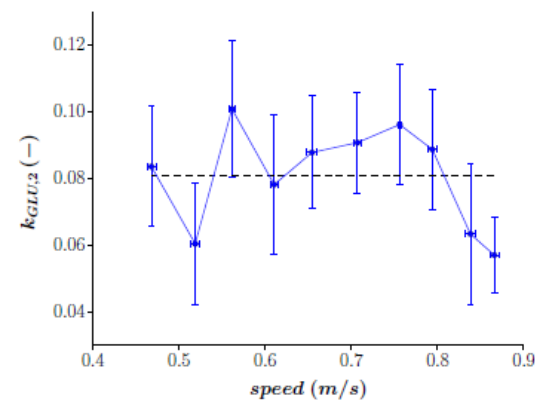
3D walking: speed parameters (I)



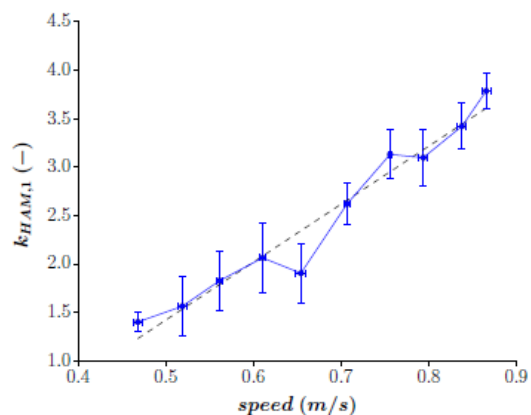
(a) Stimulation gain k_{HFL}



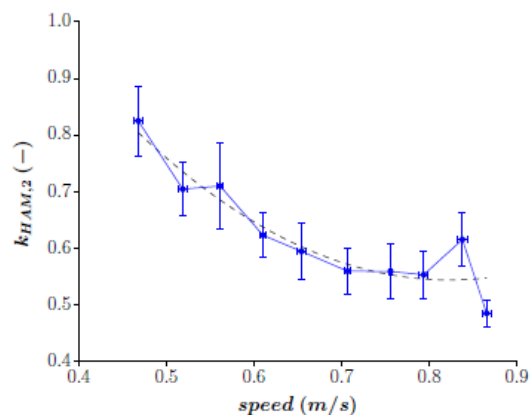
(b) Stimulation gain $k_{GLU,1}$



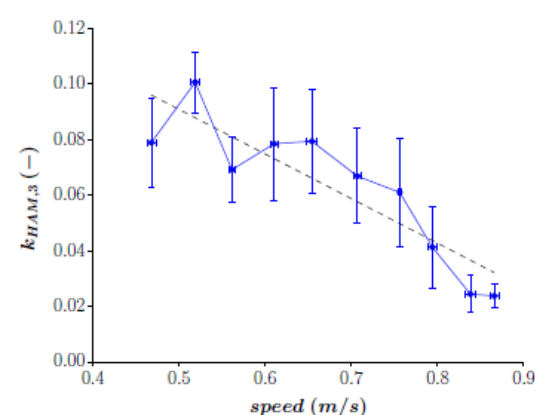
(c) Stimulation gain $k_{GLU,2}$



(d) Stimulation gain $k_{HAM,1}$

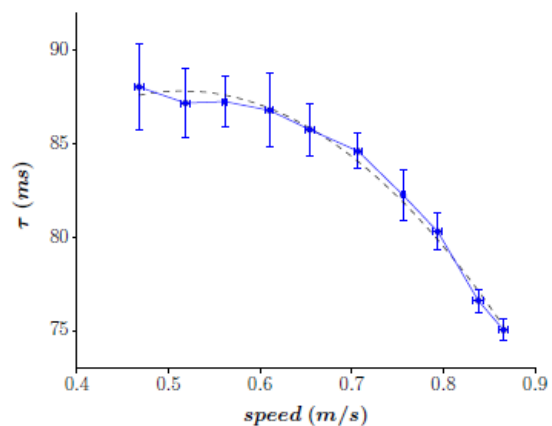


(e) Stimulation gain $k_{HAM,2}$

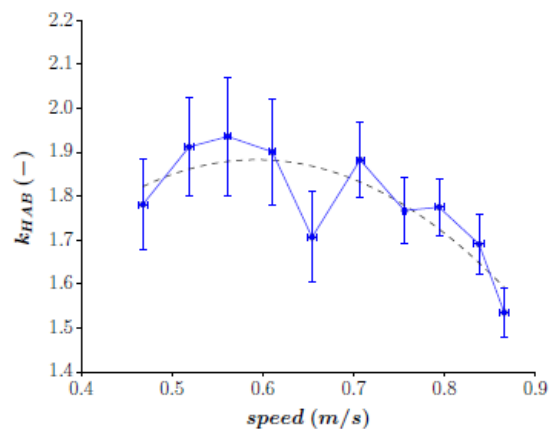


(f) Stimulation gain $k_{HAM,3}$

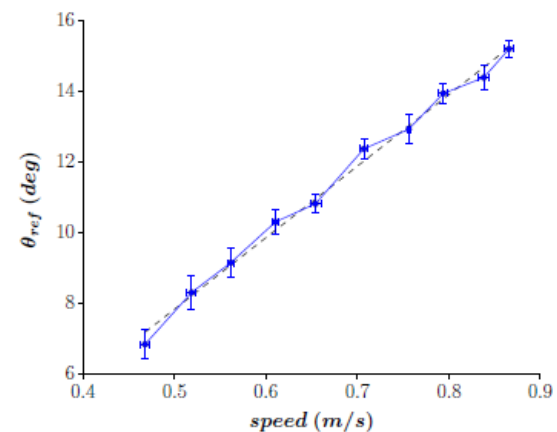
3D walking: speed parameters (II)



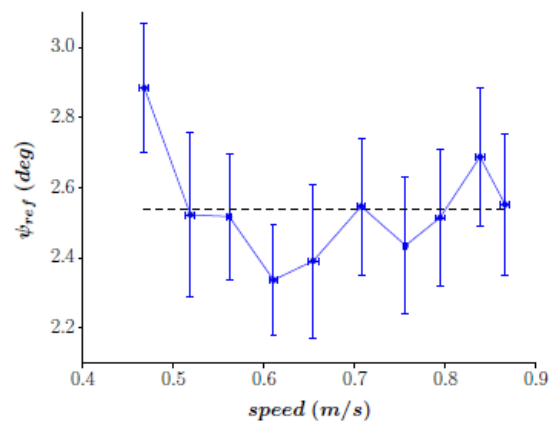
(g) CPG time constant τ



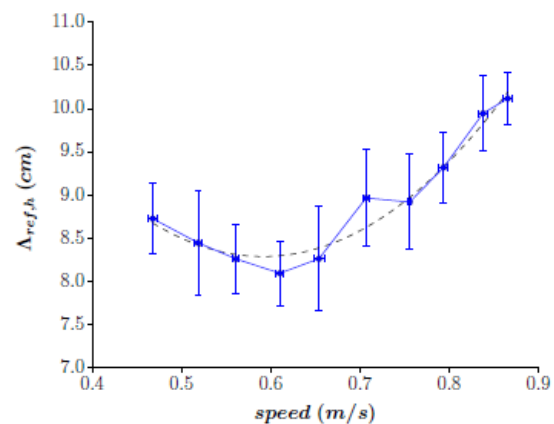
(h) Stimulation gain k_{HAB}



(i) Sagittal torso reference θ_{ref}

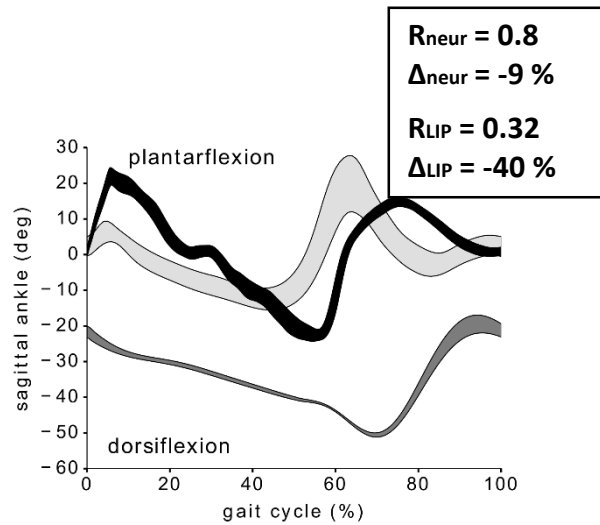


(j) Lateral torso reference Ψ_{ref}

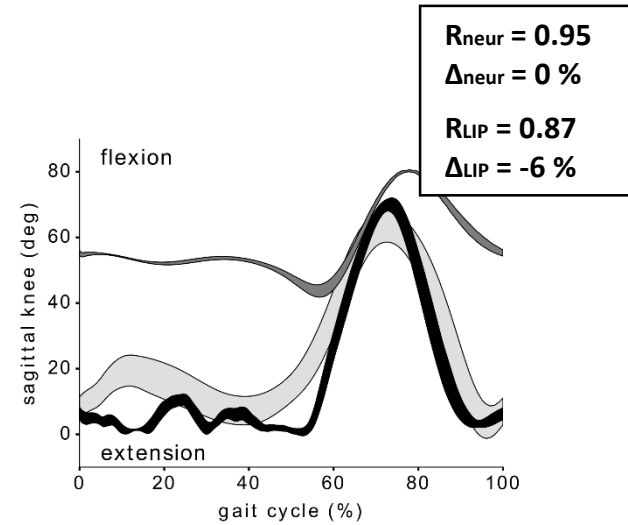


(k) COM reference $\Lambda_{ref,h}$

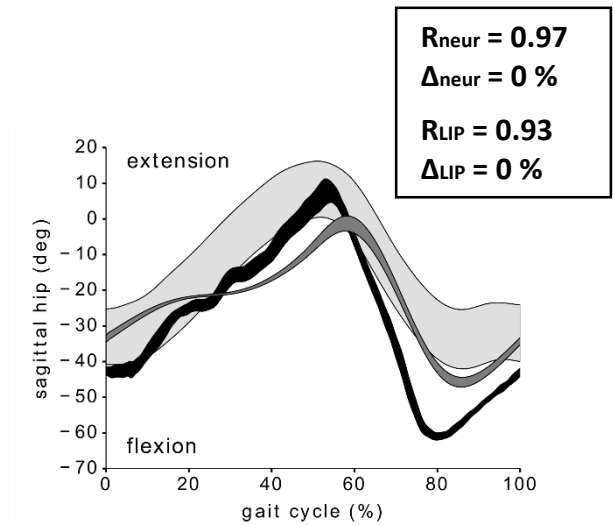
Comparisons to human and LIP-based data



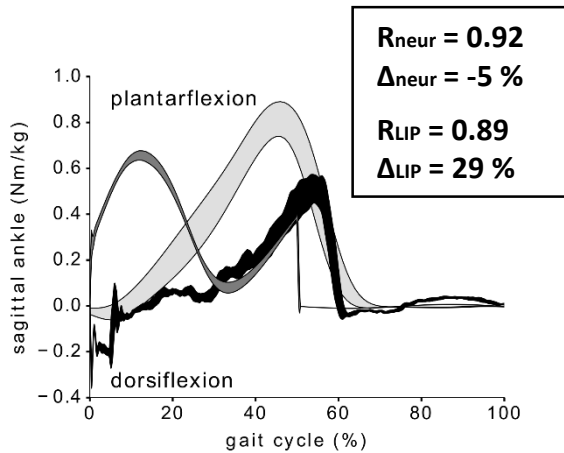
sagittal ankle angle



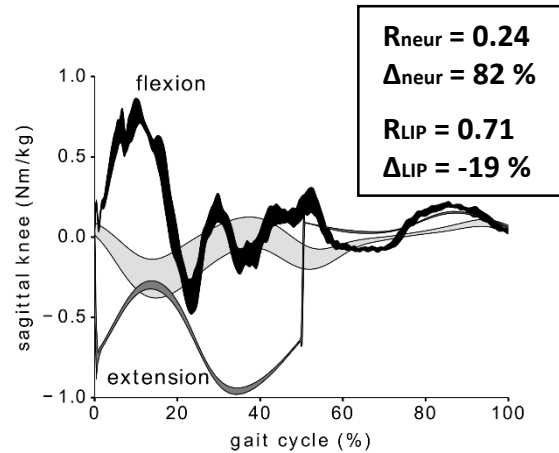
sagittal knee angle



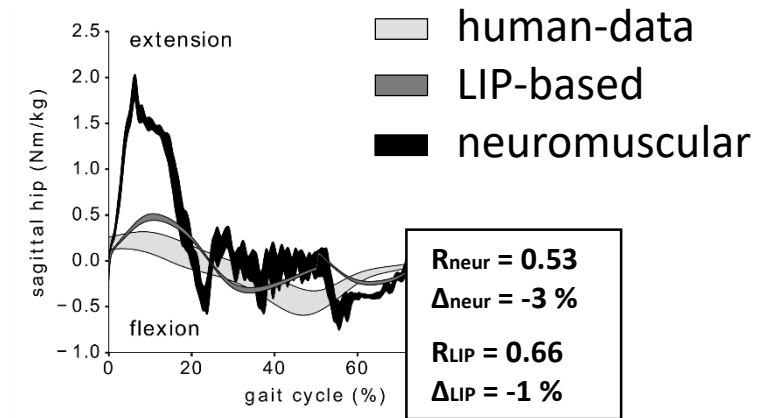
sagittal hip angle



sagittal ankle torque



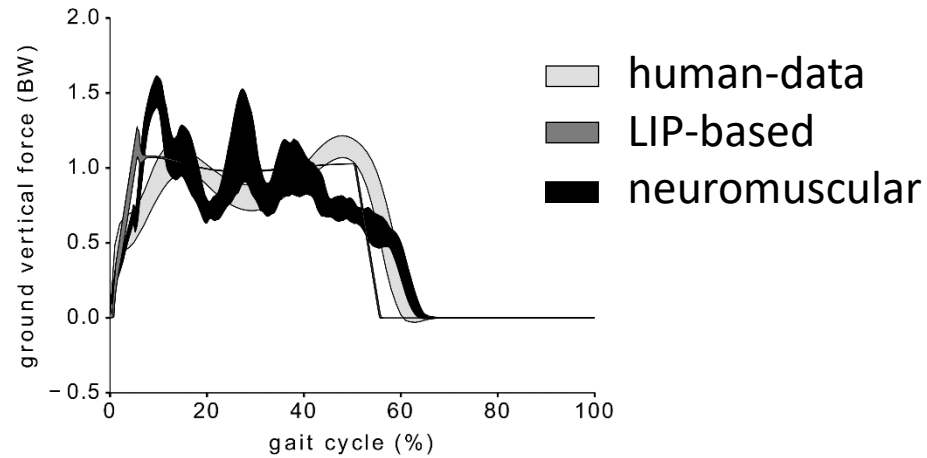
sagittal knee torque



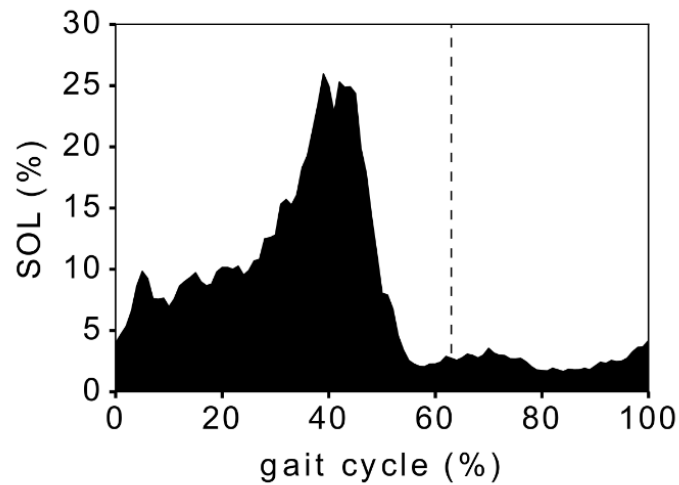
sagittal hip torque

Comparisons to human and LIP-based data

$R_{neur} = 0.96$
 $\Delta_{neur} = 1\%$
 $R_{LIP} = 0.98$
 $\Delta_{LIP} = 3\%$

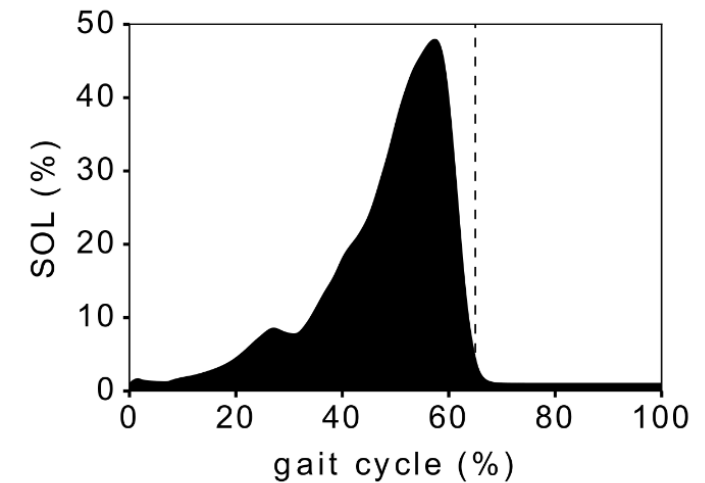


vertical ground reaction forces



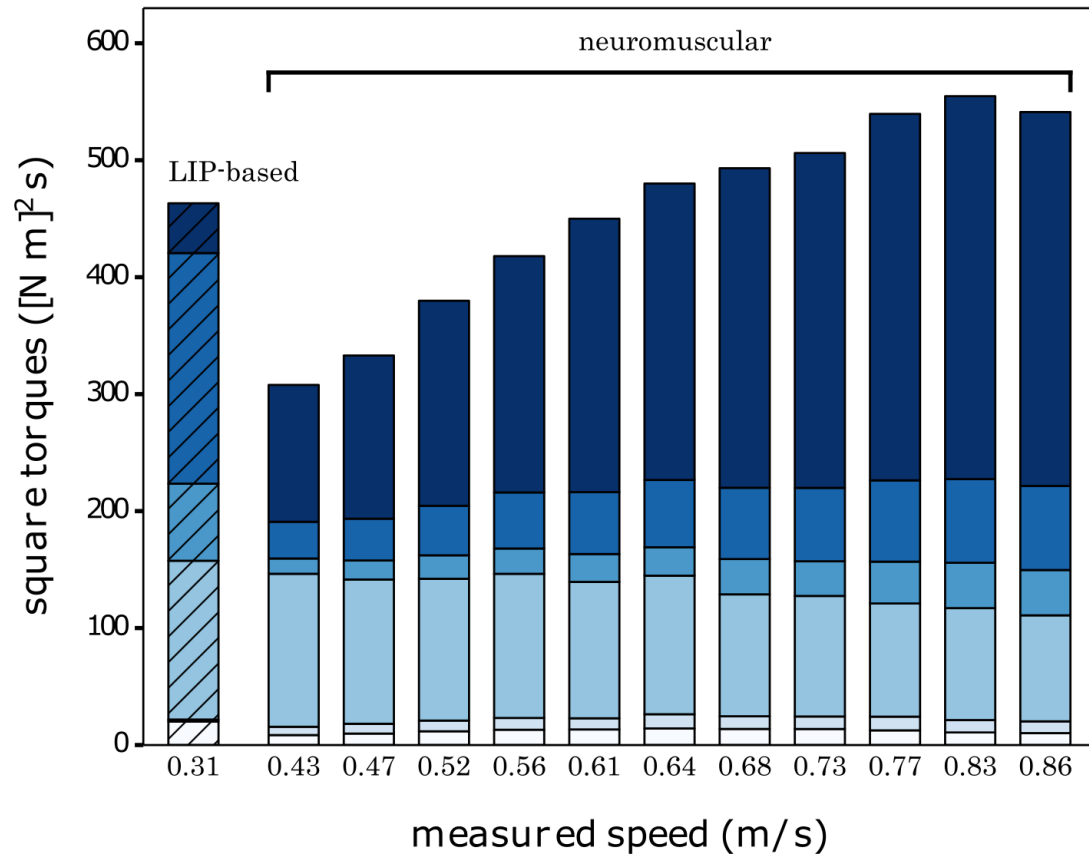
human soleus EMG

$R_{neur} = 0.96$
 $\Delta_{neur} = -14\%$

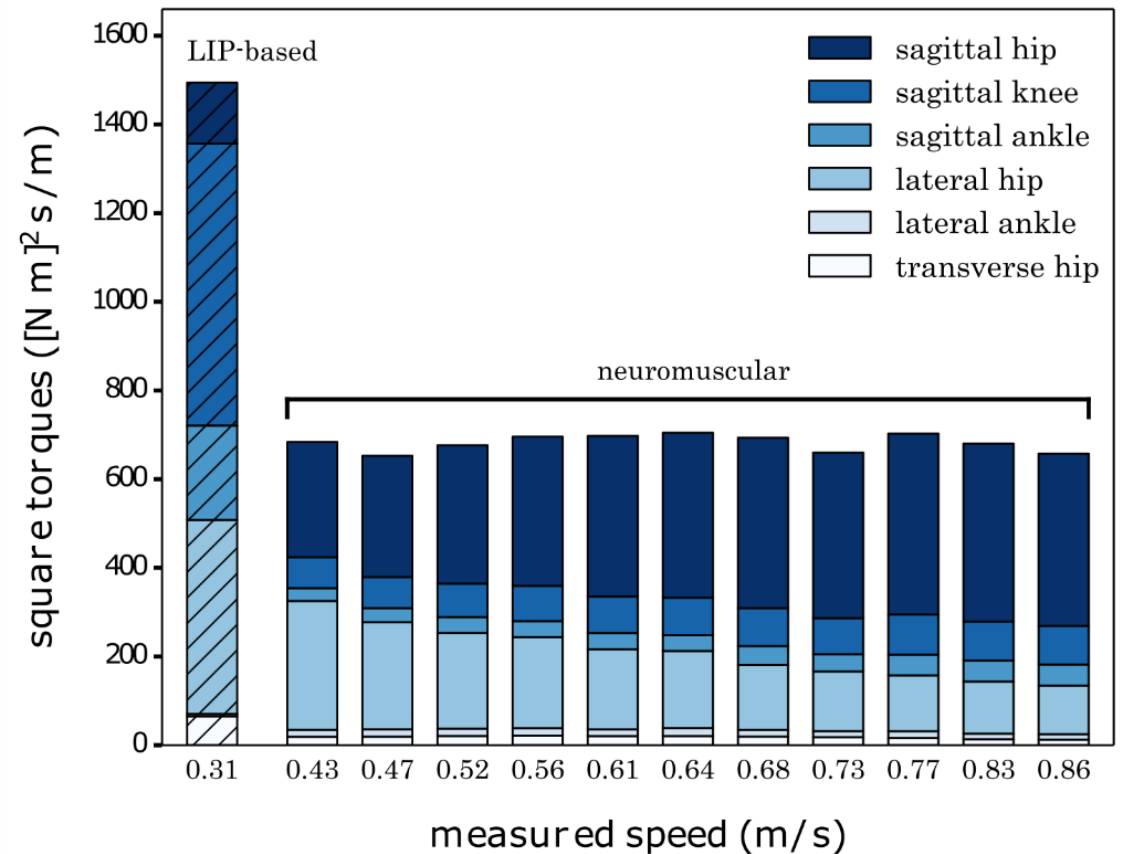


COMAN soleus activation

Energetic consumption: square torques integration



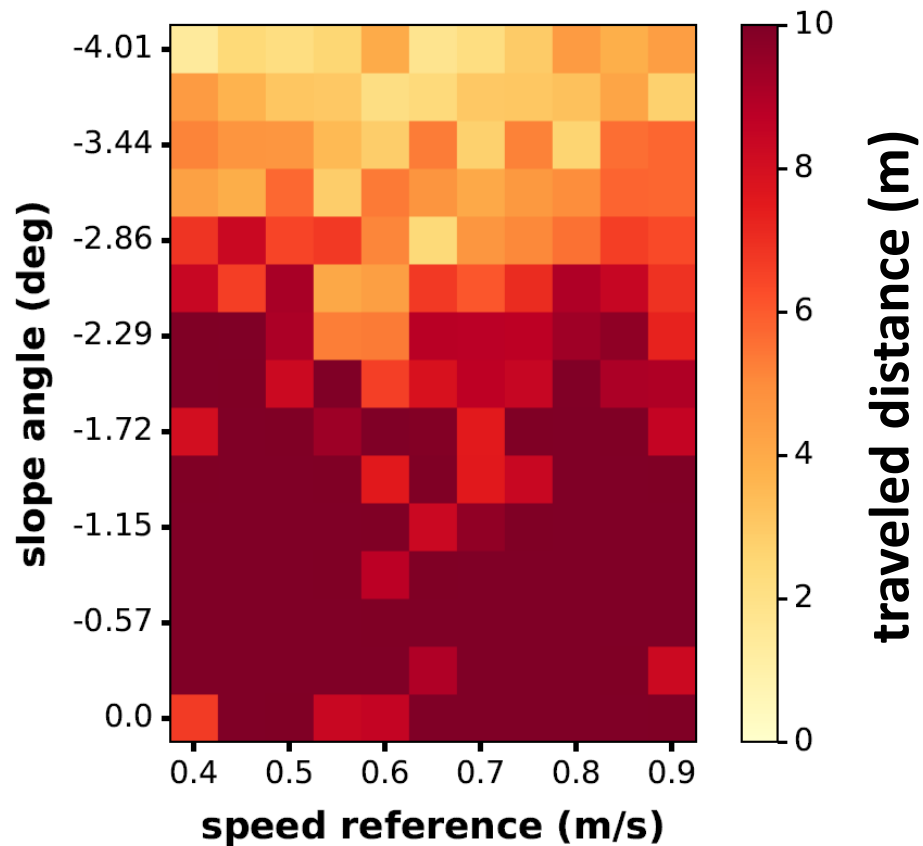
square torques per gait cycle



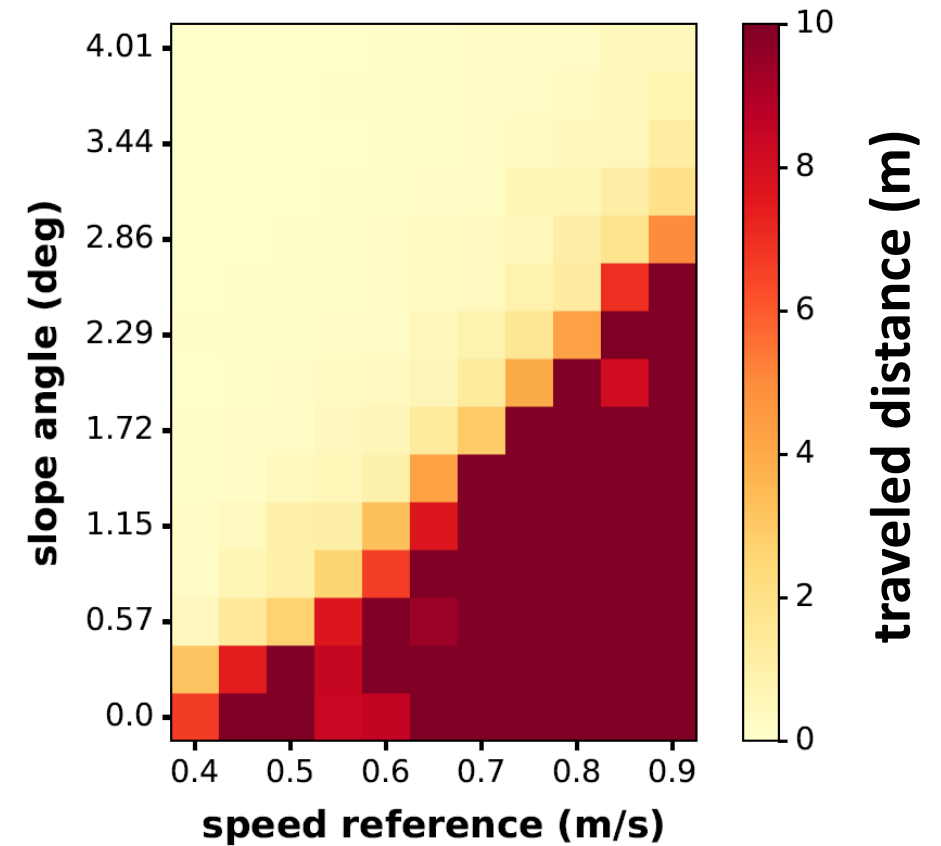
square torques per gait cycle,
divided by traveled distance

Robustness: facing unknown slopes

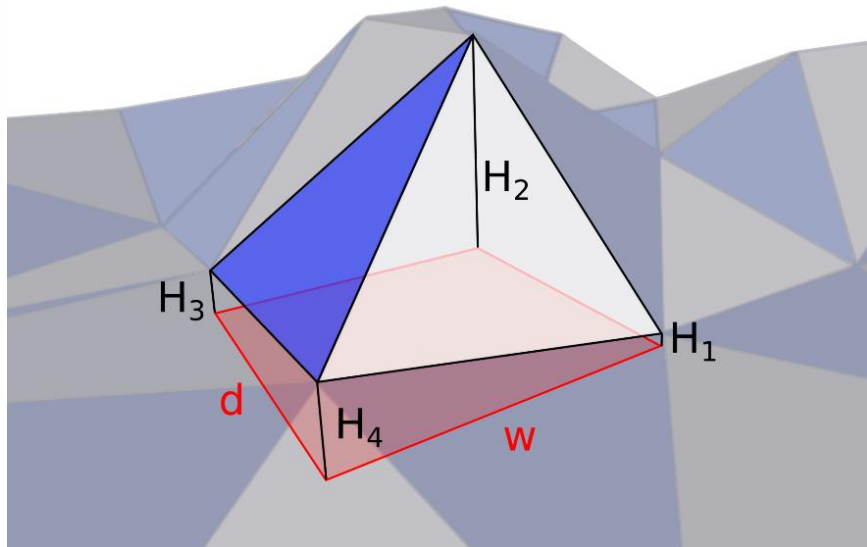
negative slopes



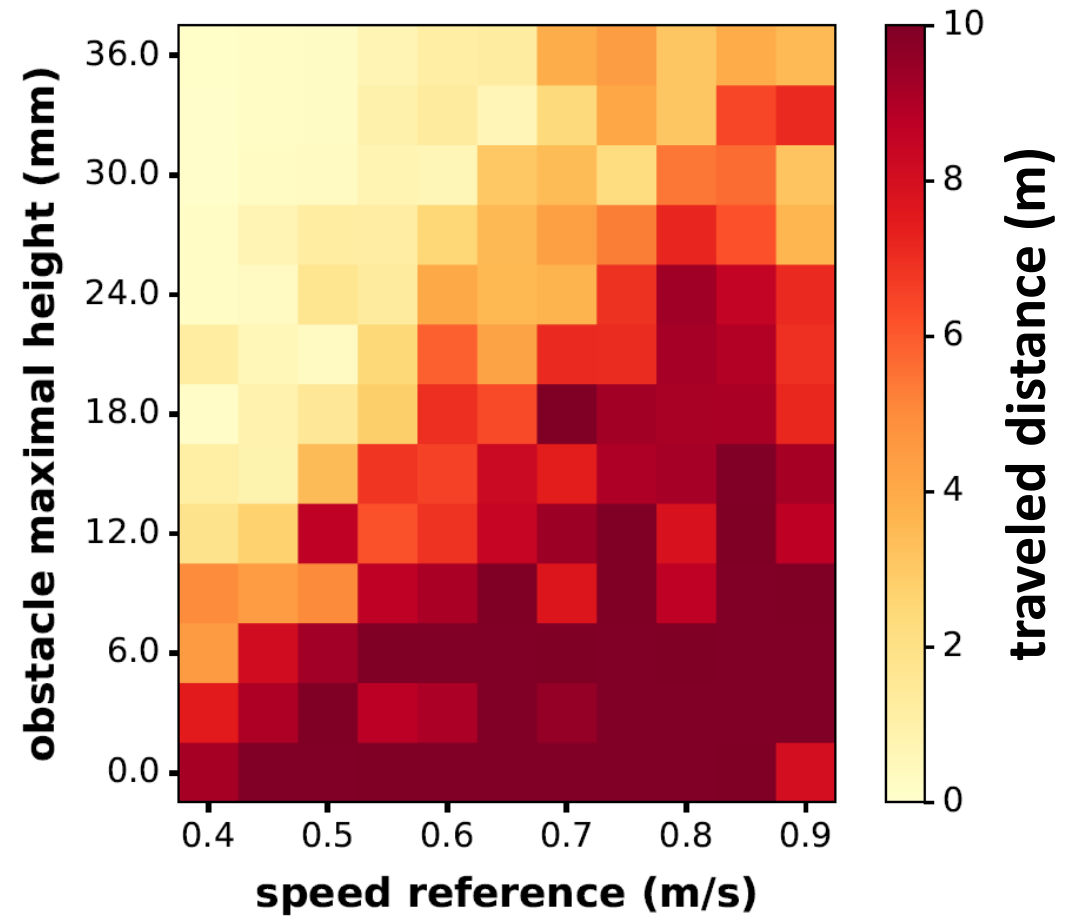
positive slopes



Robustness: blind walking on irregular ground

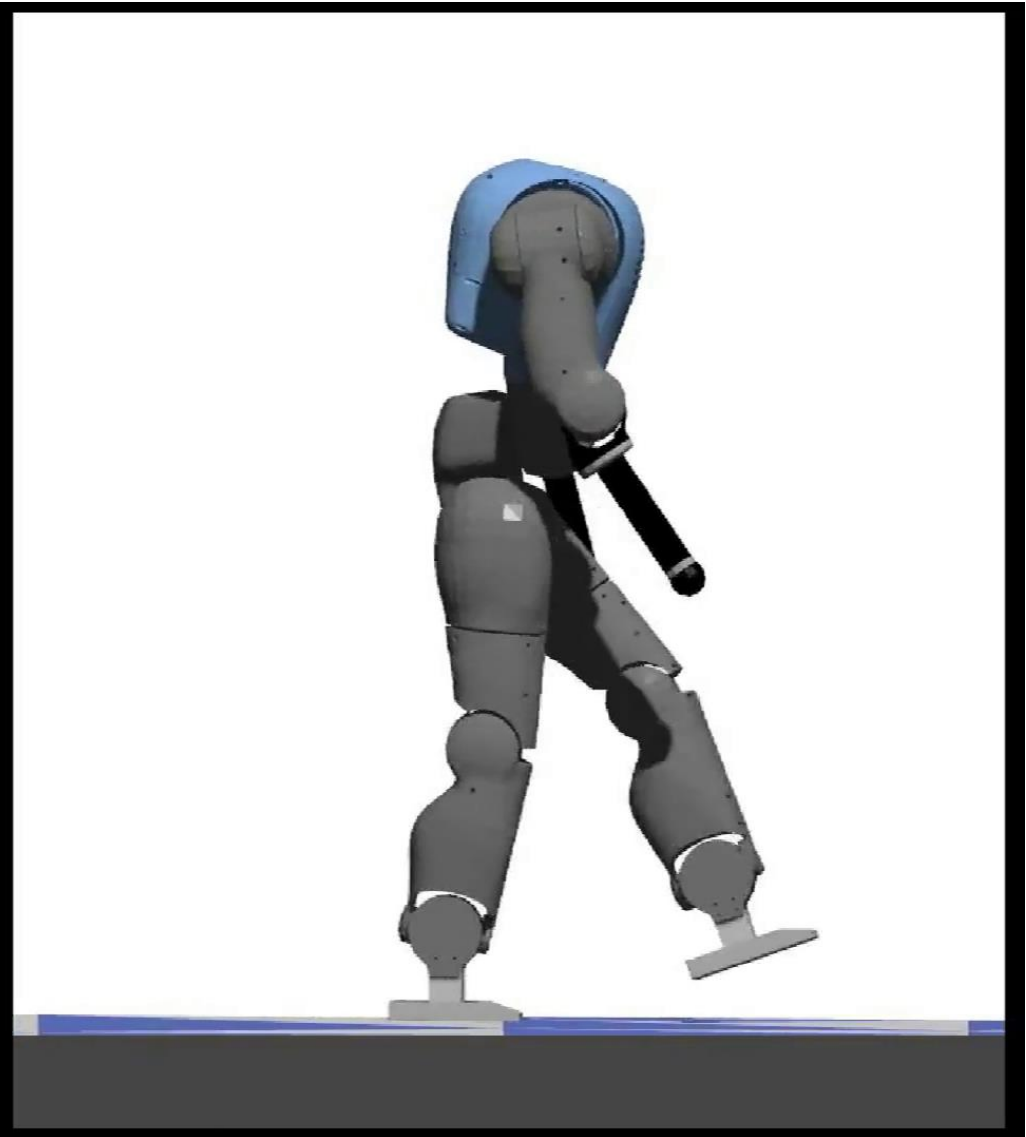
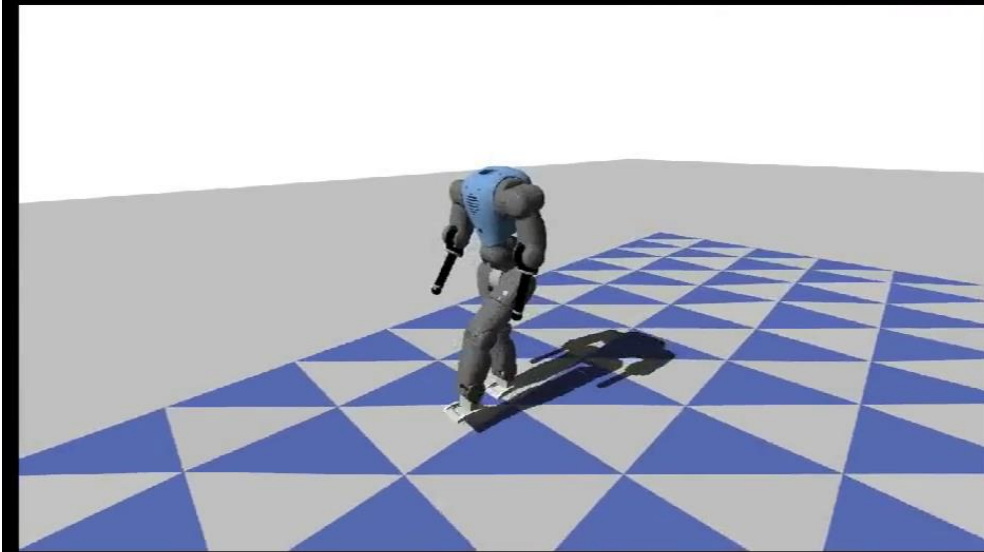
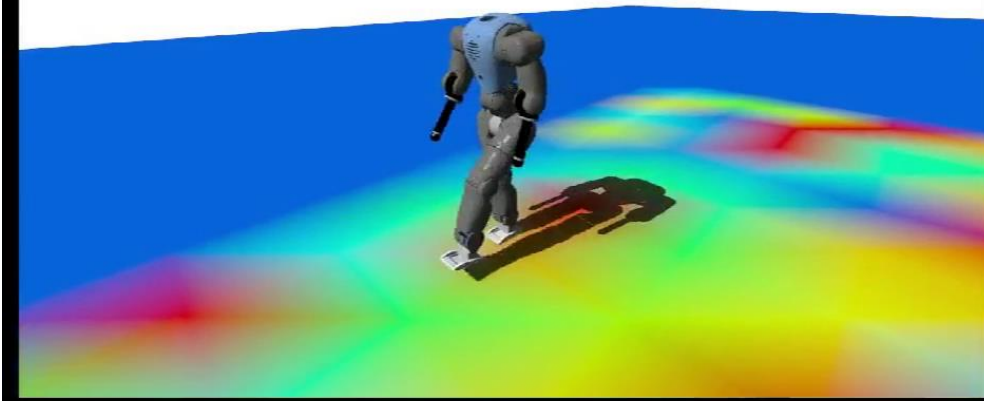


ground description



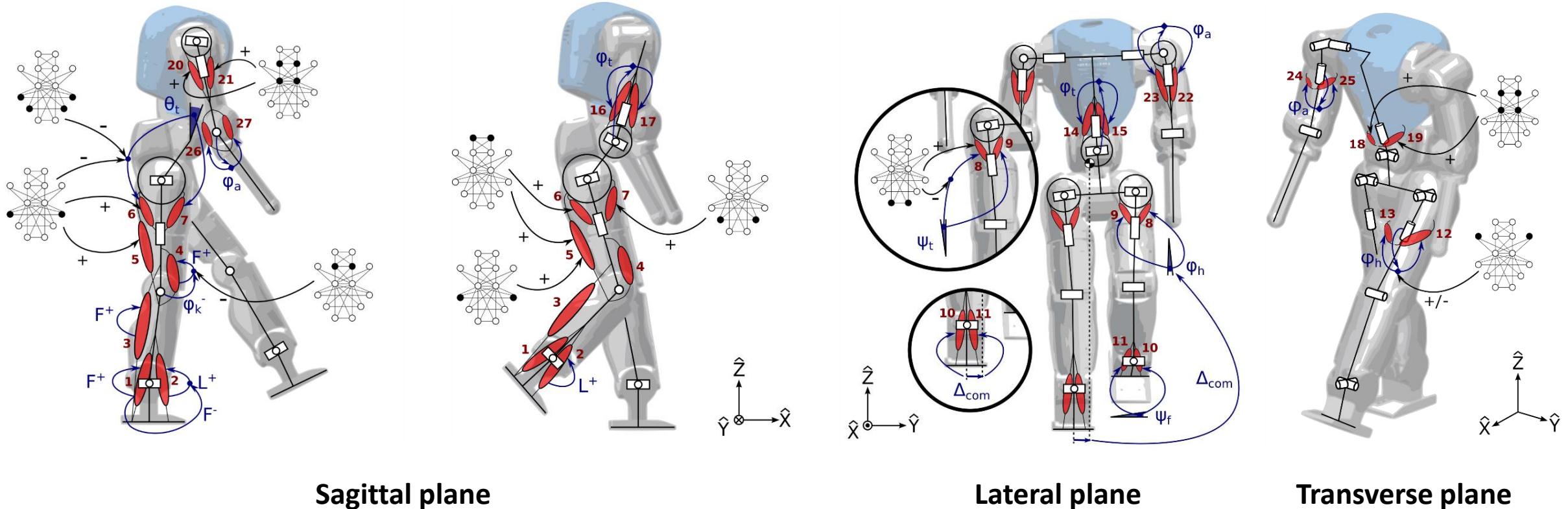
Blind walking on irregular ground

In this panel, warmer colors indicate higher grounds.



Full 3D control

- New virtual **muscles** (in all the planes)
- New **reflex** signals
- **CPG** structure incremented

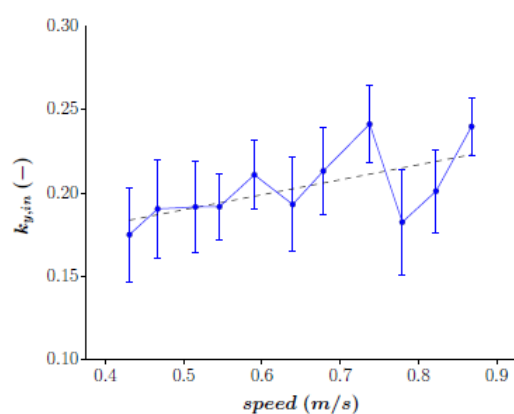


Sagittal plane

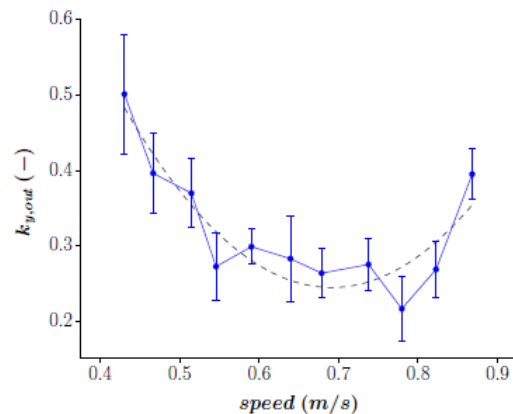
Lateral plane

Transverse plane

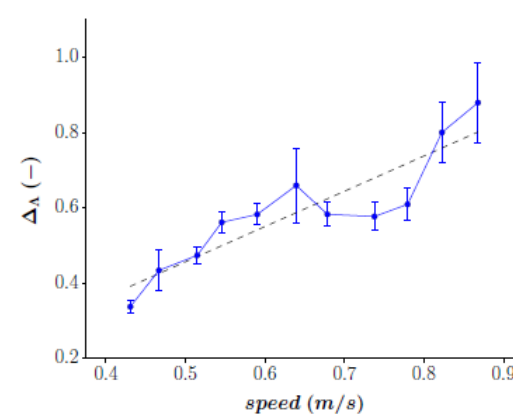
Heading control: speed parameters



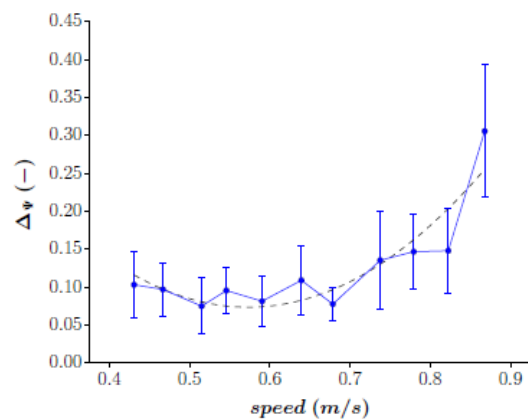
(a) Transverse gain $k_{y,in}$



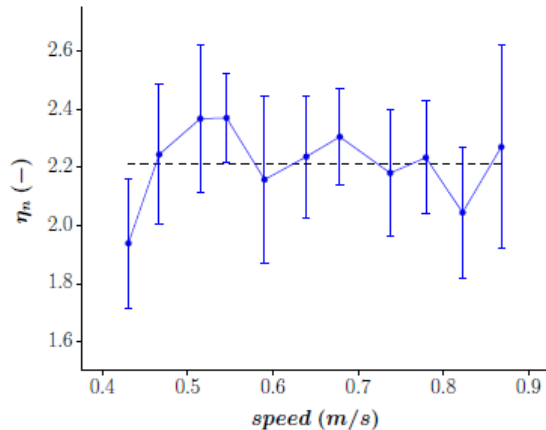
(b) Transverse gain $k_{y,out}$



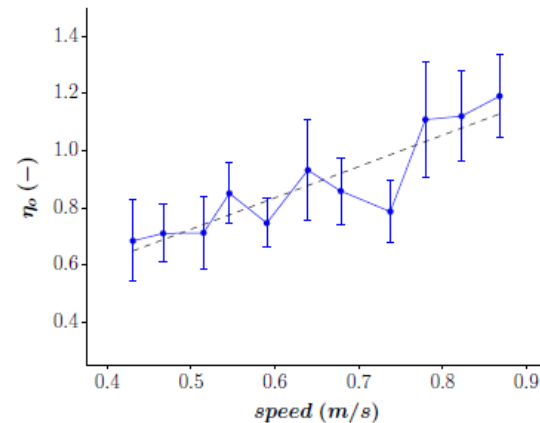
(c) COM modulation Δ_{Λ}



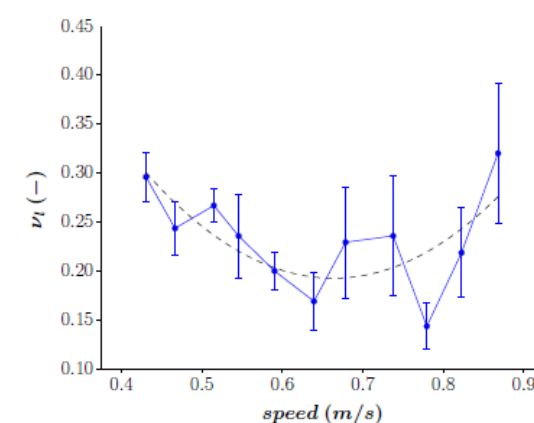
(d) Hip modulation Δ_{Ψ}



(e) CPG connexion η_n

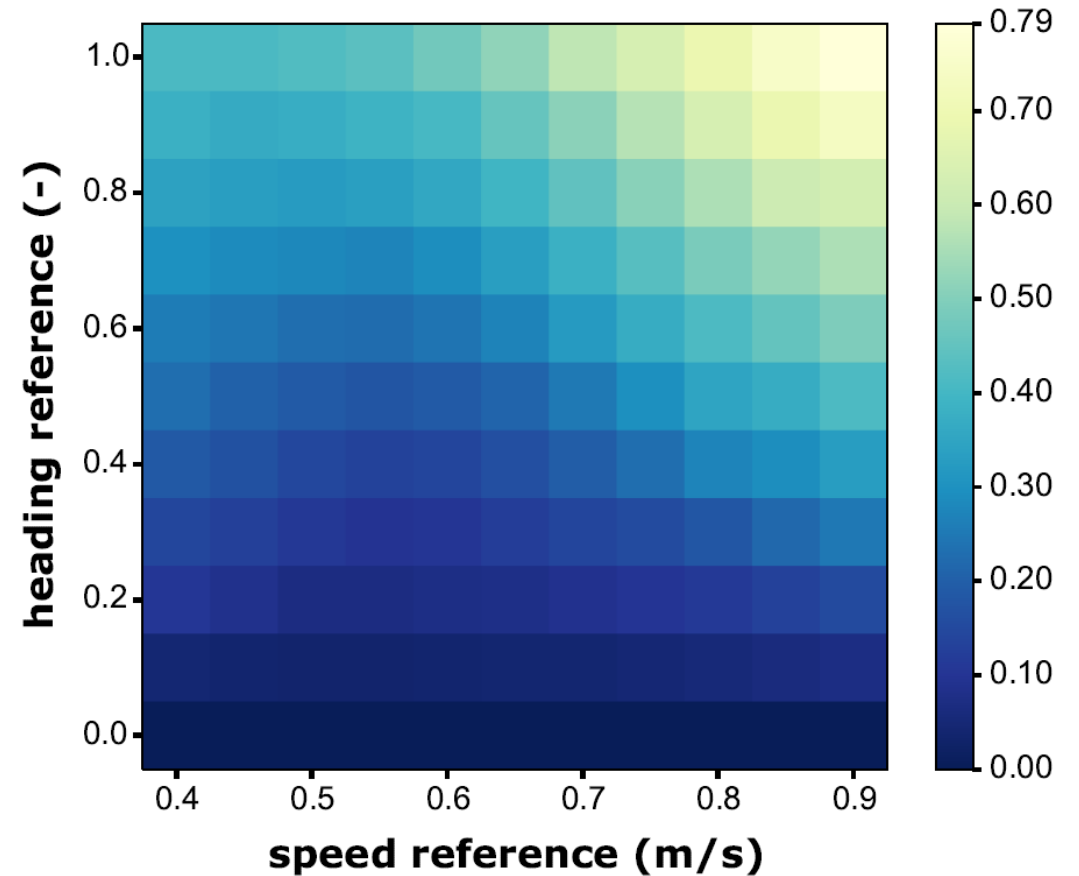
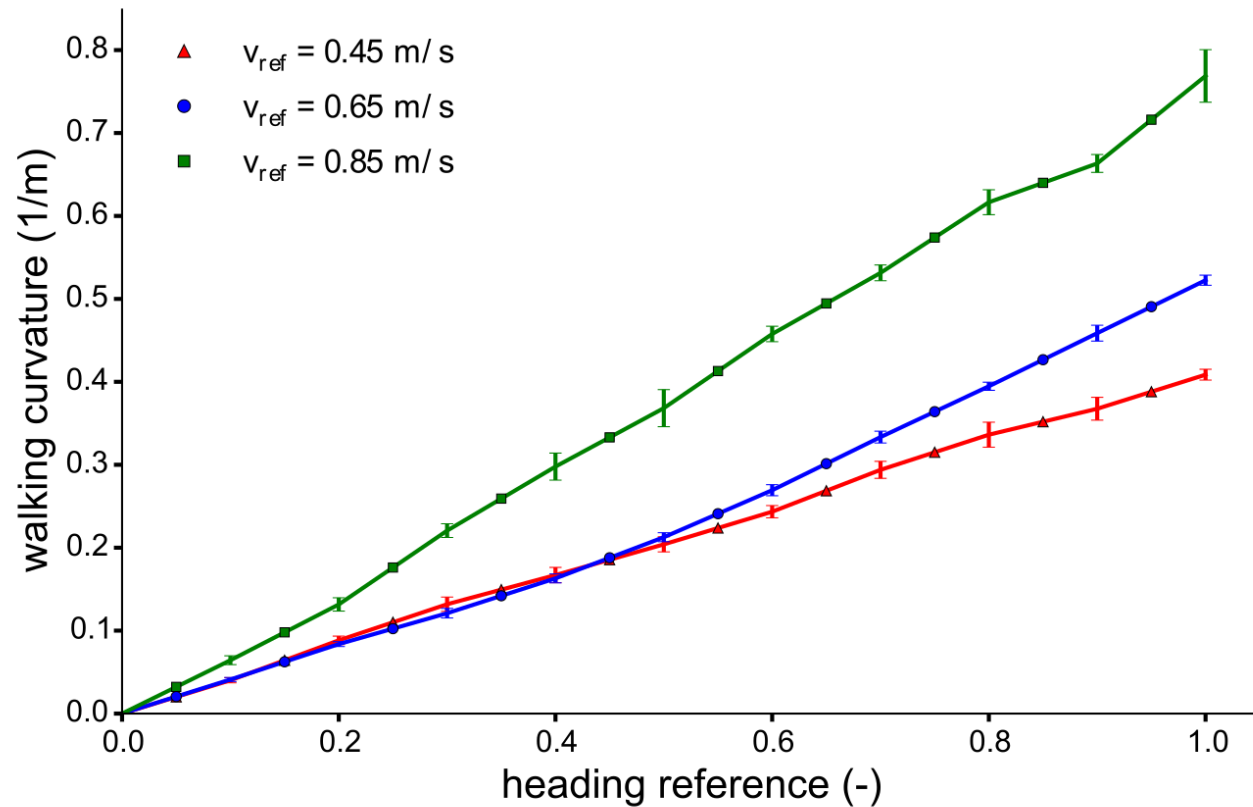


(f) CPG connexion η_o

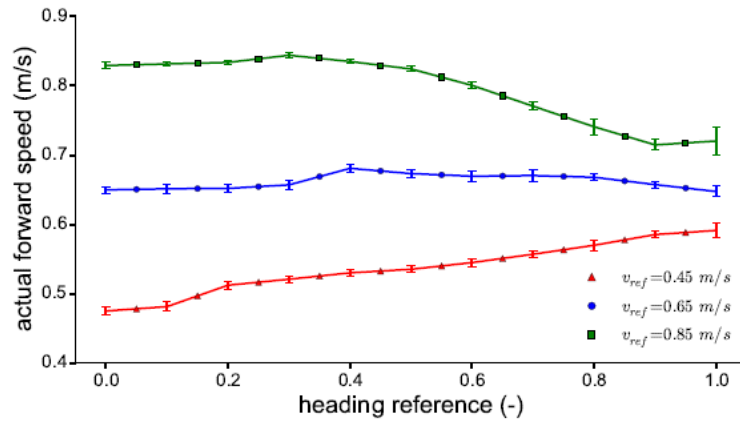


(g) Lateral excitation v_l

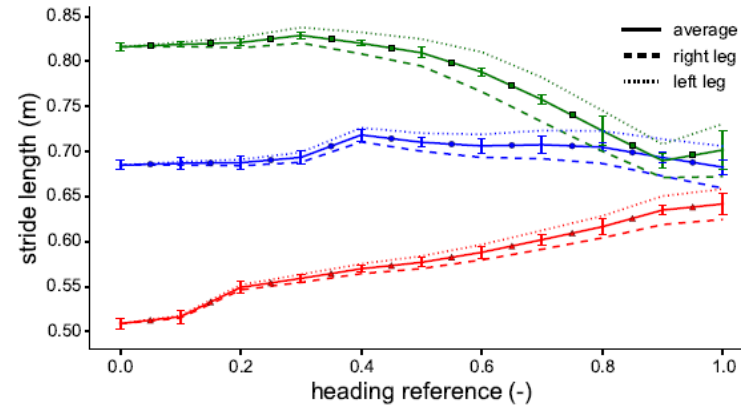
Walking curvature



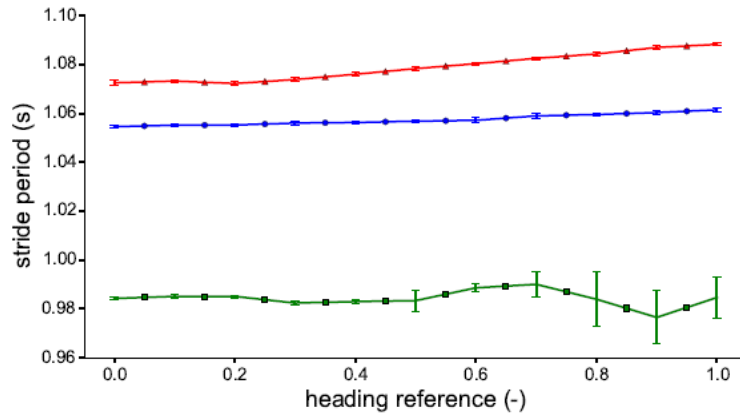
Steering characteristics



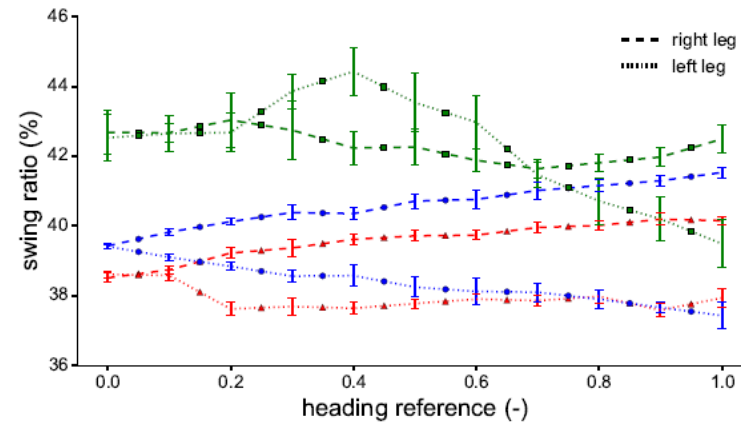
(a) real speed



(b) stride length

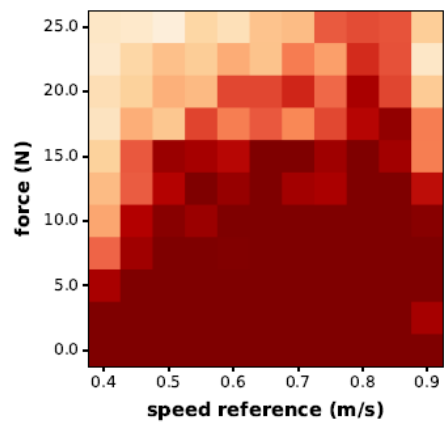


(c) stride period

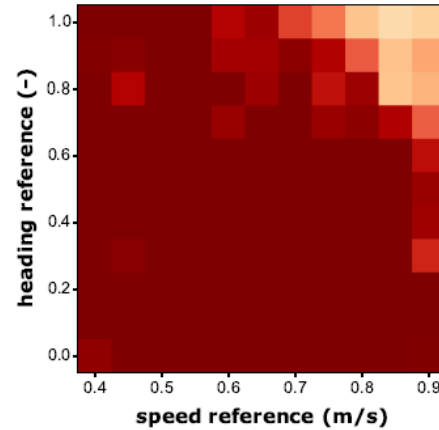


(d) swing ratio

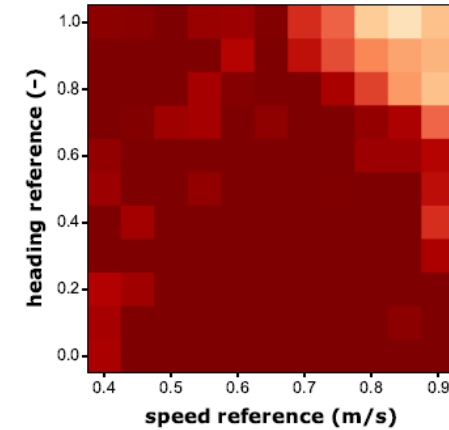
Steering robustness



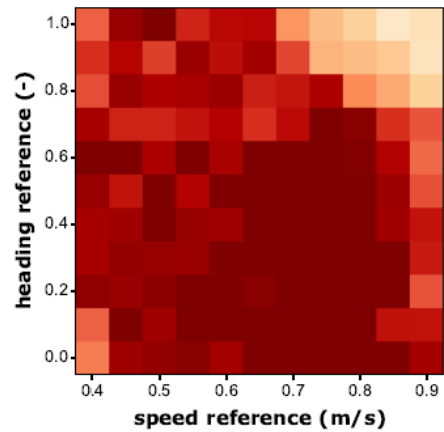
(a) straight walking, forces: 0 – 25 N



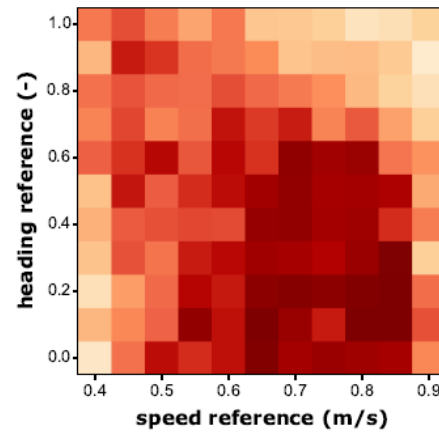
(b) right steering, force: 0 N



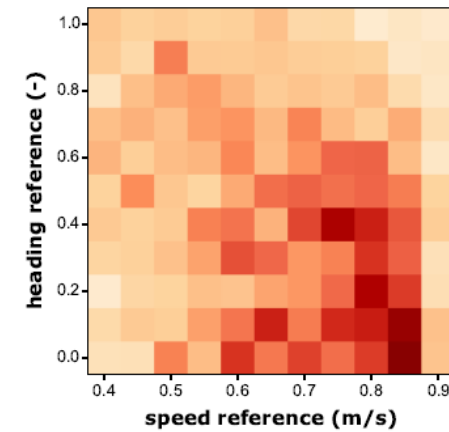
(c) right steering, force: 5 N



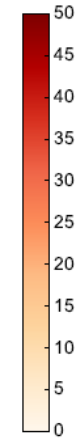
(d) right steering, force: 10 N



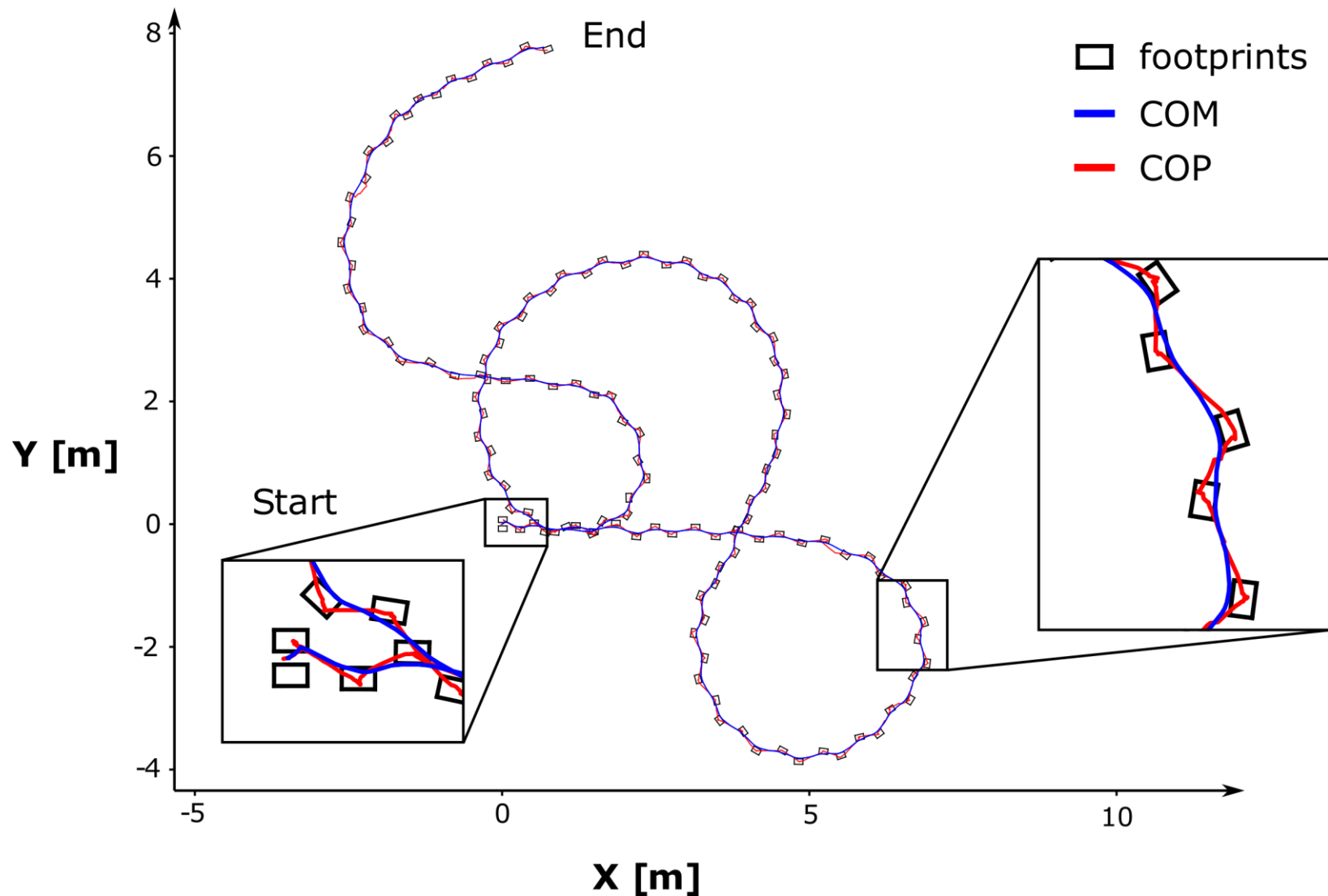
(e) right steering, force: 15 N



(f) right steering, force: 20 N



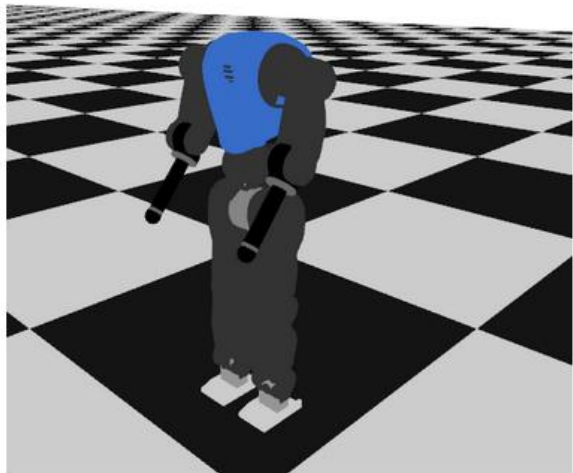
Footprints during steering



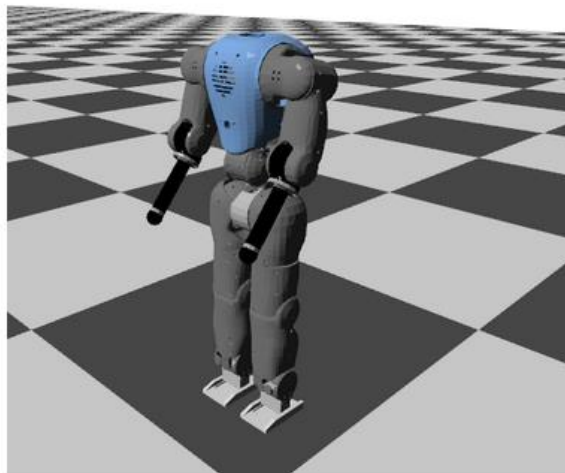
Robotran: real-time features

The image displays two windows from the Robotran software. The left window, titled "OpenGL visualization", shows a 3D model of a humanoid robot in a walking posture. To the left of the robot, the text "go back in time to visualize past events" is displayed. The right window, titled "Real-time graph", shows a line graph with three data series: "HAM stim" (blue), "TA stim" (red), and "SOL stim" (green). The y-axis ranges from -0.20 to 1.20, and the x-axis has labels from 2844 to 4644. The graph shows periodic, high-frequency oscillations for all three muscles. Below the graph is a control panel with various icons and text: "k:", "i:", "u:", "y:", "j:", "h:", "x axis: [26.44 ; 46.44]", "y axis: [-0.20 ; 1.20]", "speed: 0.25x", "time: 77% (46.4/60)", and "q:", "l:", "m:".

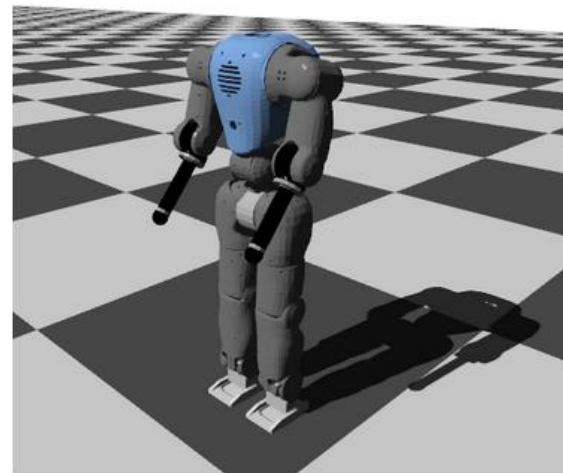
OpenGL features



basic shader



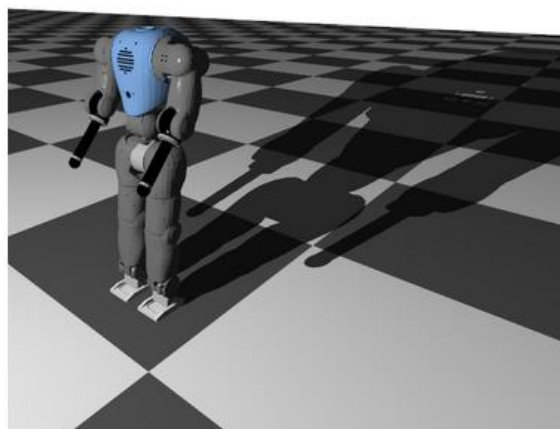
shader with lights



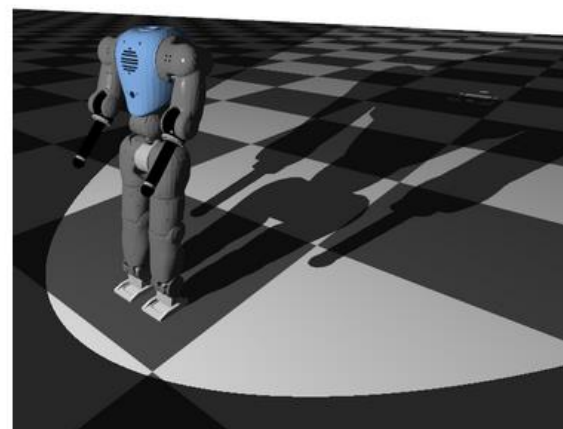
shader with lights and shadows



directional light

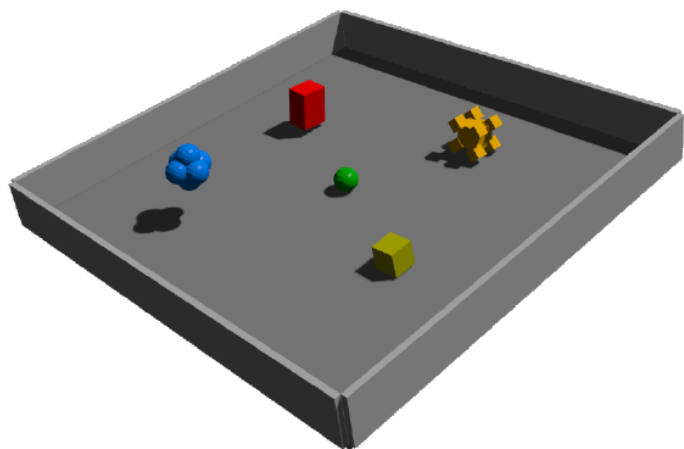


point light

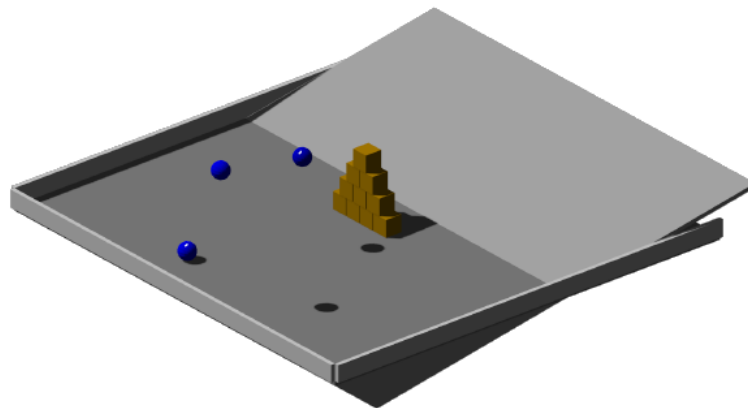


spot light

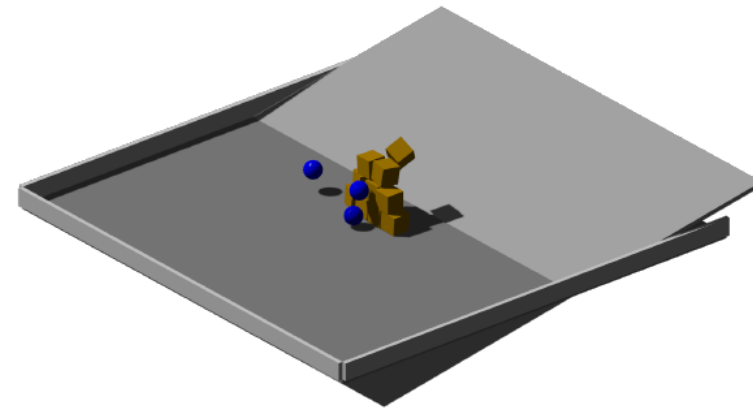
Primitive shapes contact model



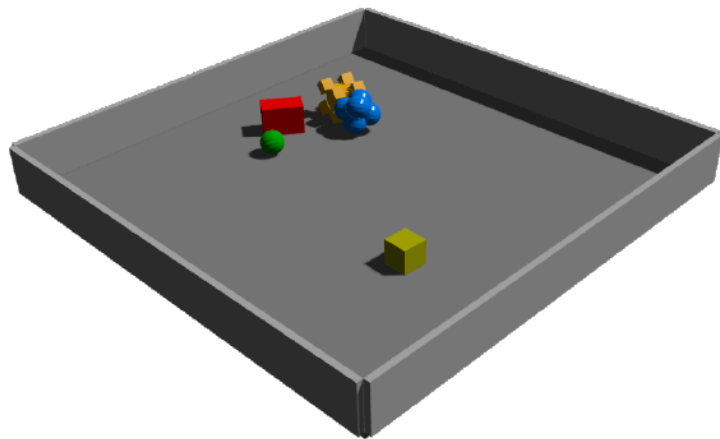
(a) objects released on the moving plane



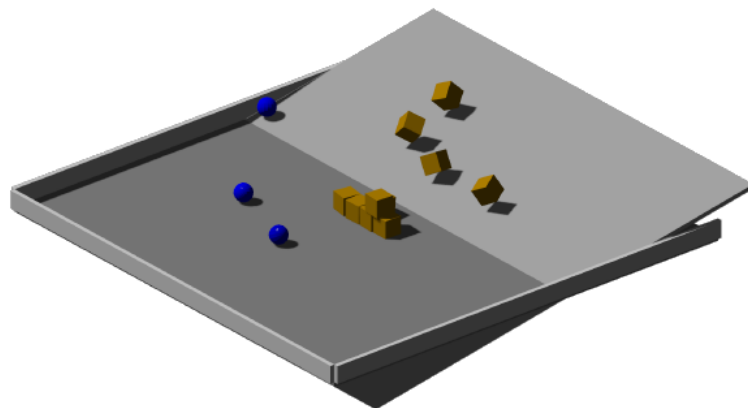
(a) before impacts



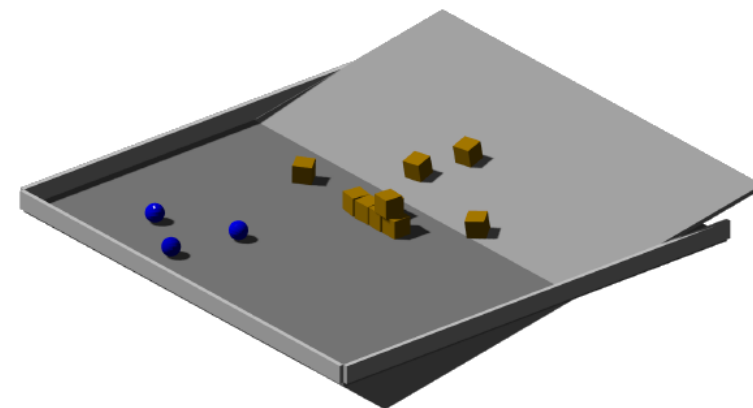
(b) during impacts



(b) positions of the objects after after a few seconds

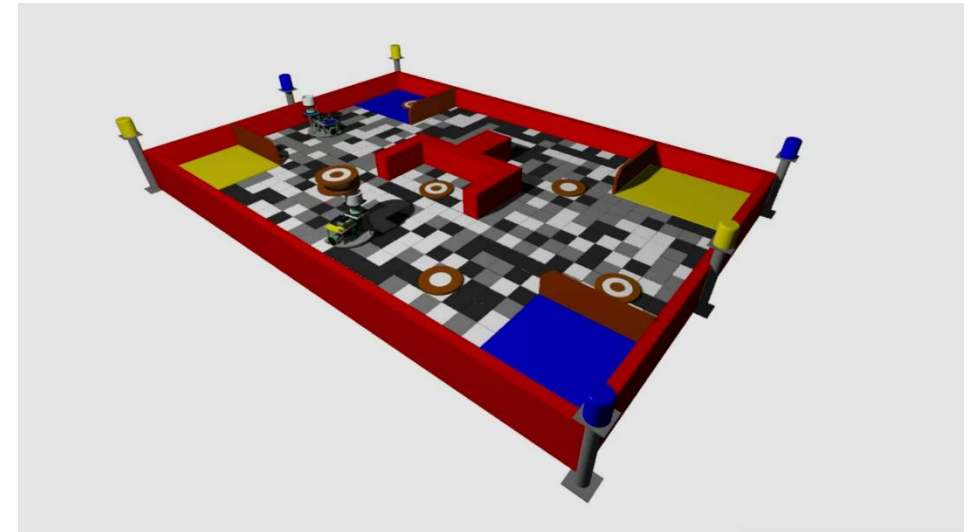
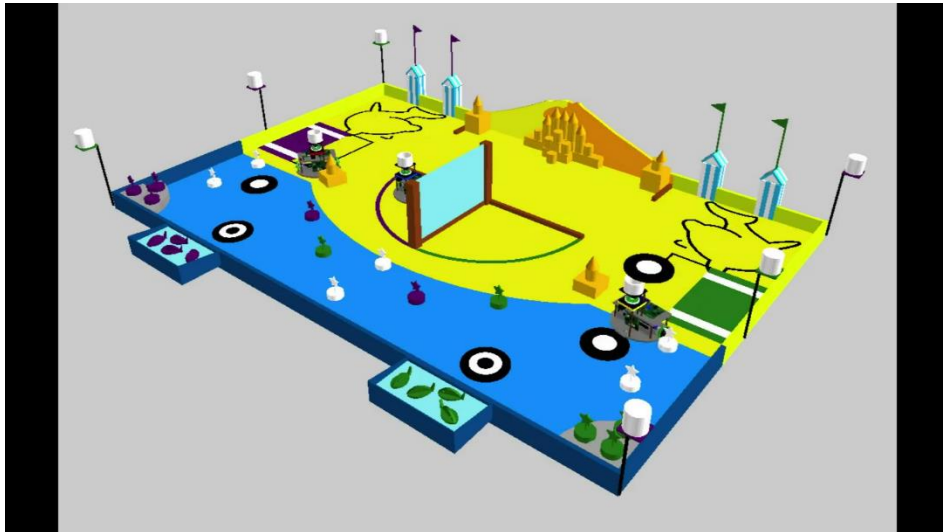
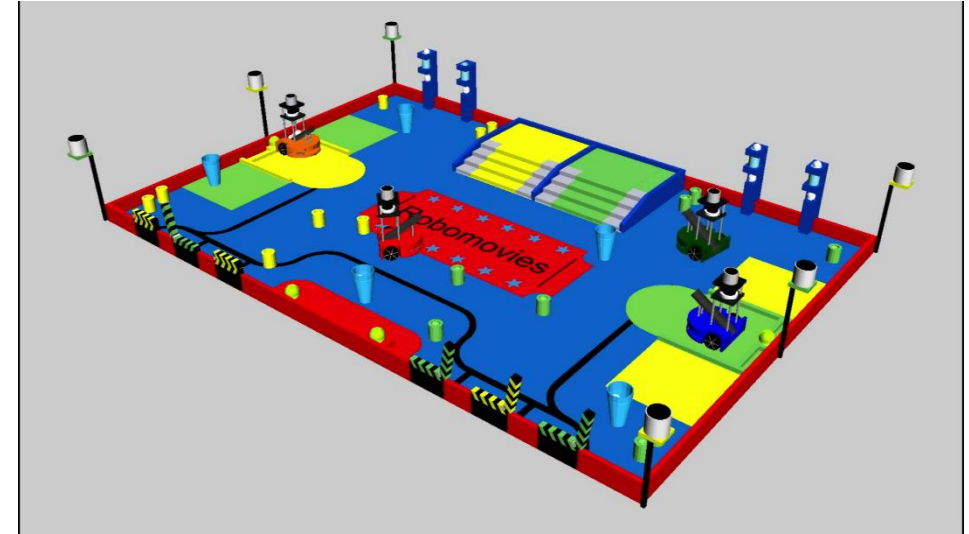


(c) after impacts

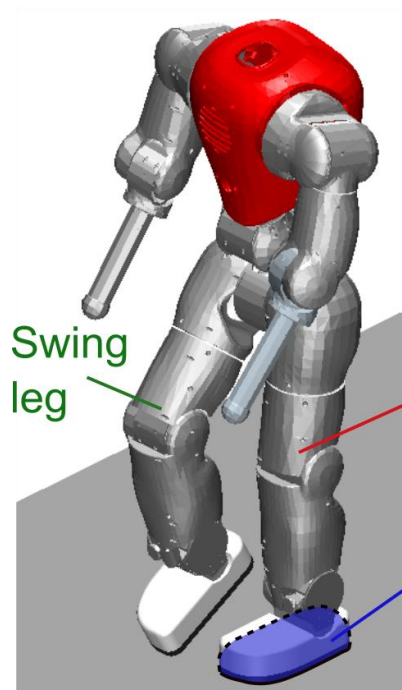
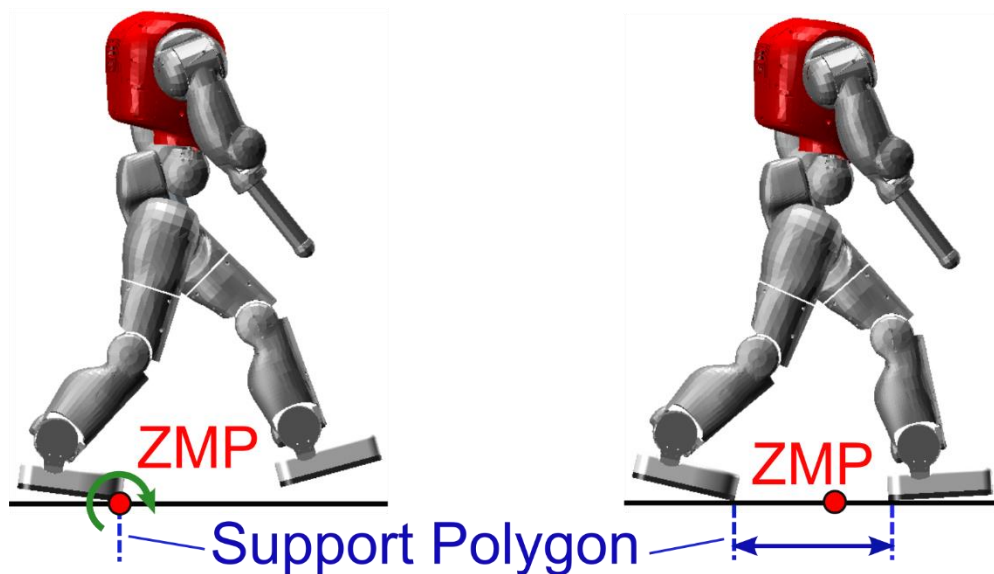
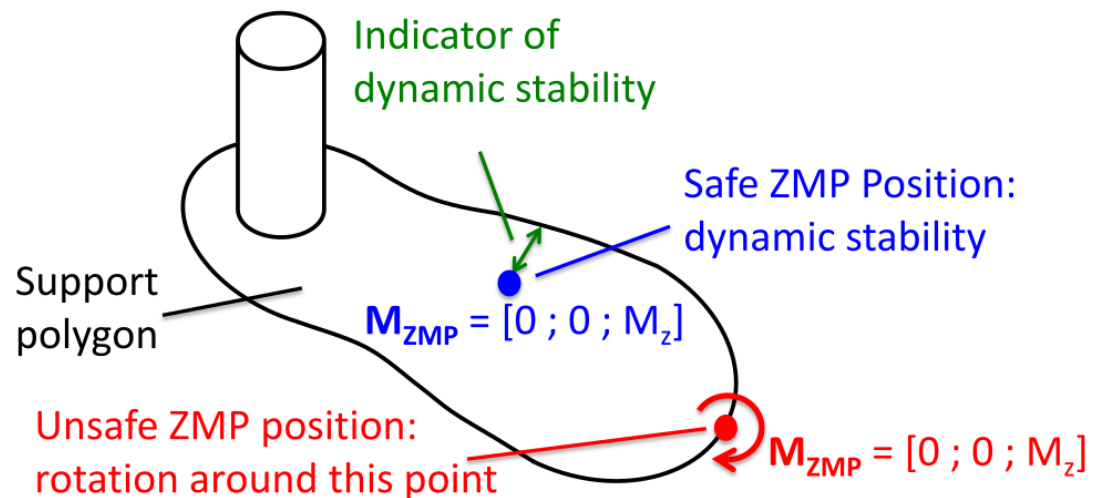


(d) boxes in standstill position

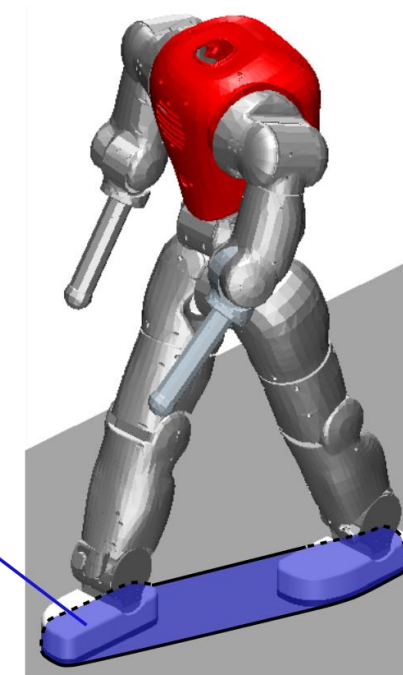
LMECA 2732 (UCL) & MICRO-452 (EPFL) courses



Zero-moment point

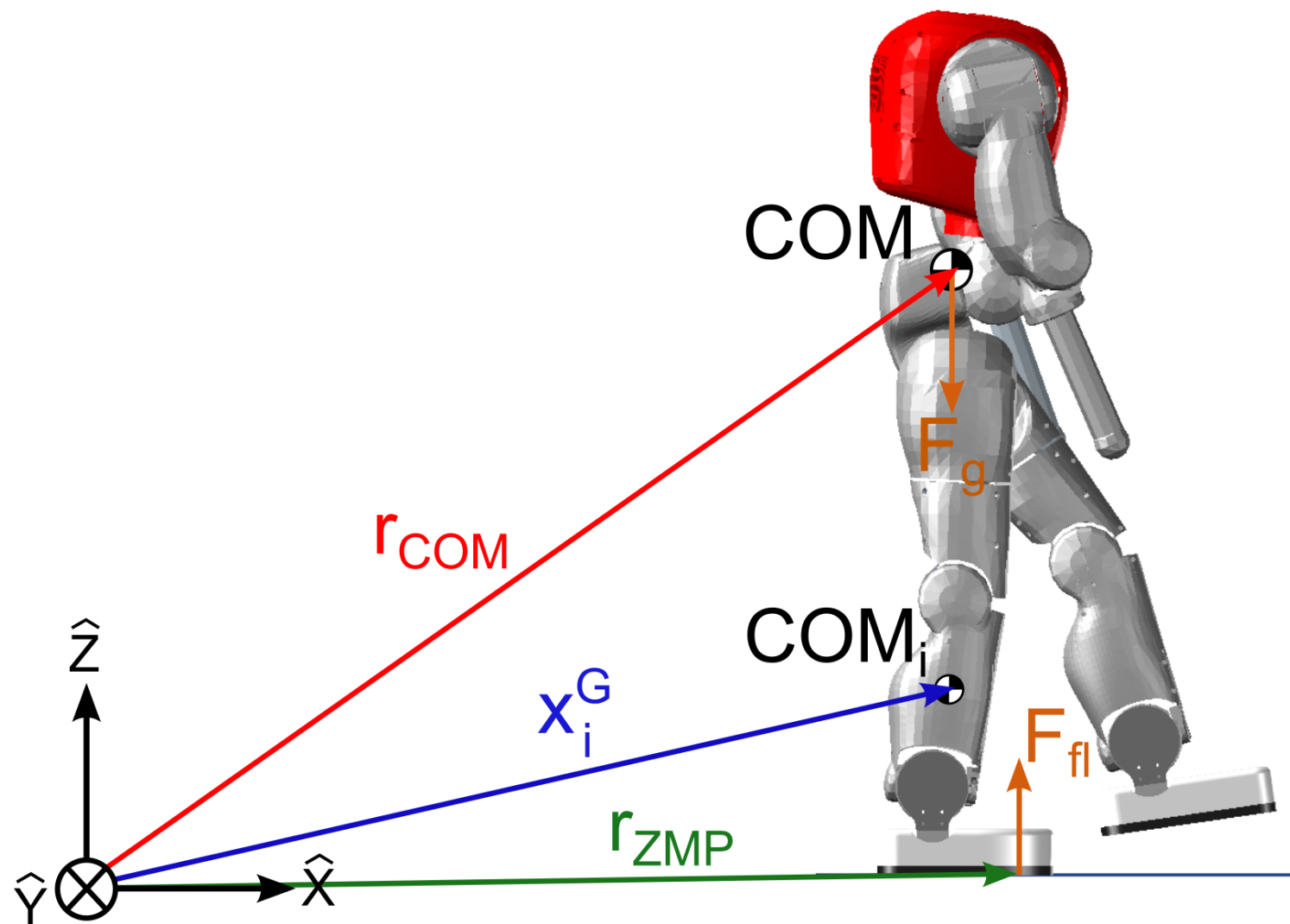


Single Support

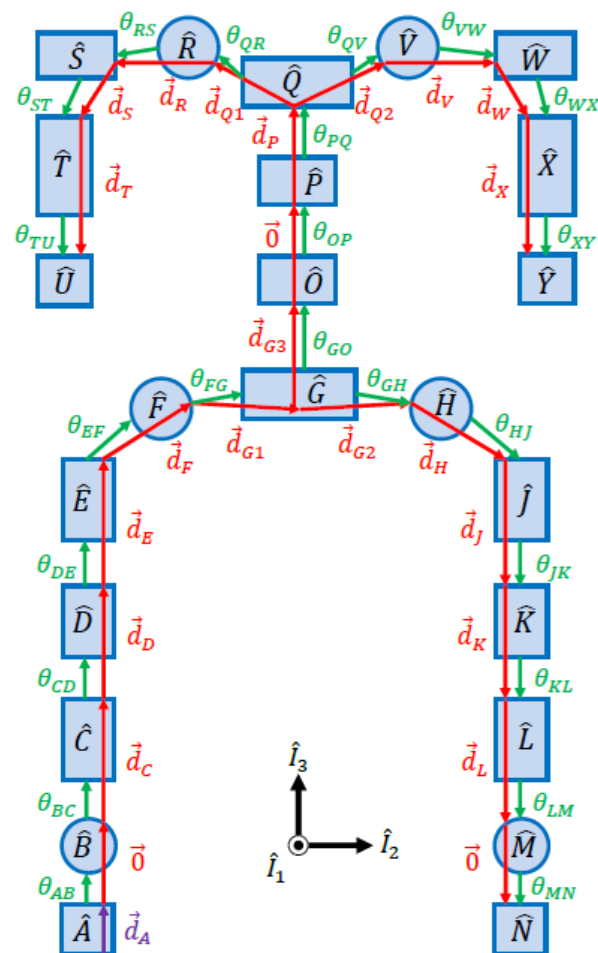


Double Support

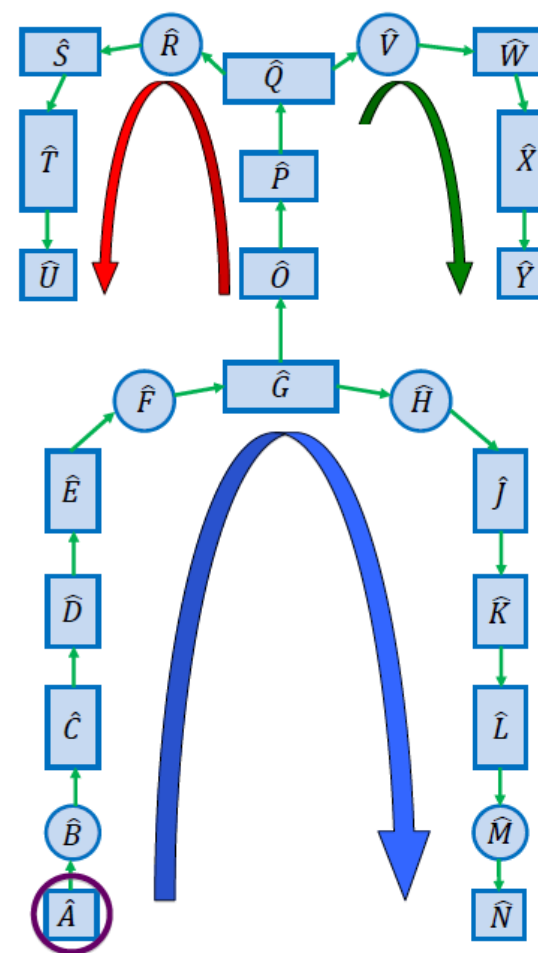
Zero-moment point computation



Zero-moment point: recursion



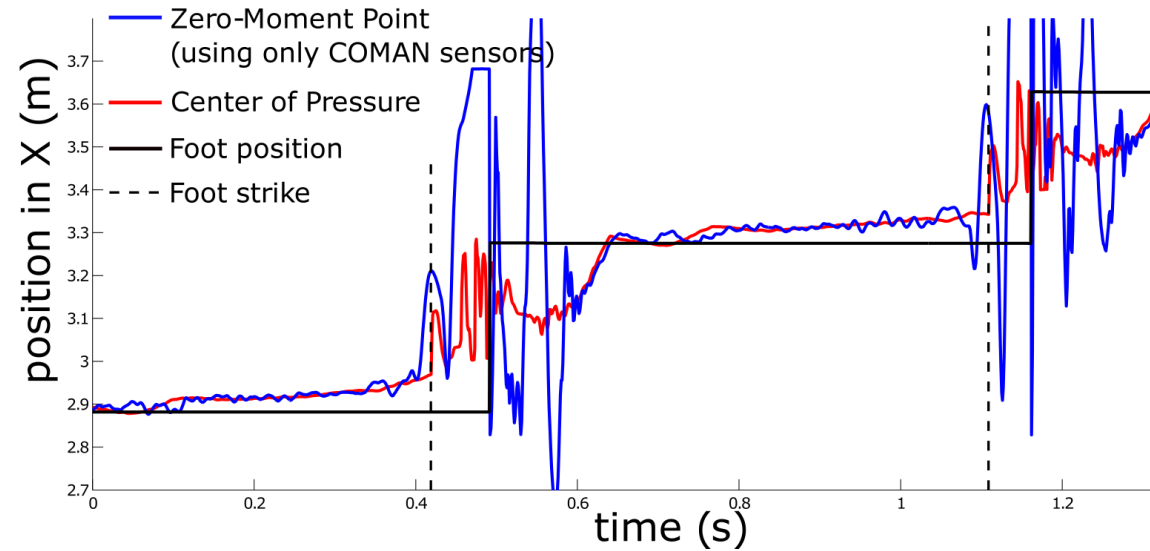
(a) Joint and positions



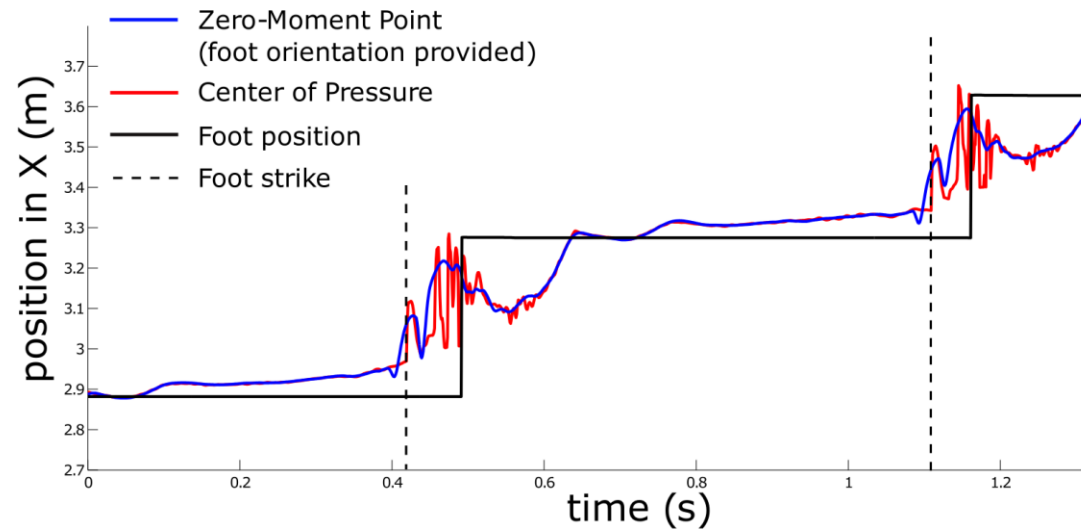
(b) Forward kinematics path

Zero-moment point results: 2D walking

No foot information,
no post-process filtering

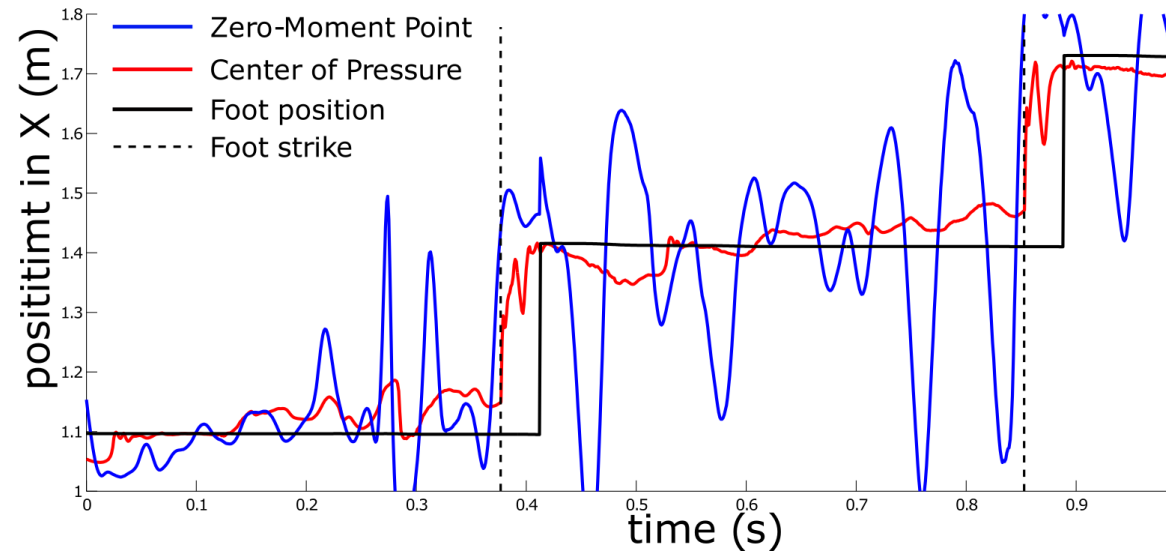


Foot orientation provided,
no post-process filtering



Zero-moment point results: 3D walking

Foot orientation provided,
no post-process filtering



Foot orientation provided,
100 ms running-average

